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State-of-Power Estimation of Li-ion Battery Considering Battery Surface Temperature

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Abstract: The State-of-Power (SOP) of Li-ion battery (LIB) is an important evaluation index for security control and energy recovery of electric vehicles. Major state estimation methods are only applicable to fixed room temperature at 20°C. Actually, the battery capacity and resistance vary dramatically with the change of battery surface temperature in the working process of the battery, which causes significant errors in state estimation if only room temperature is assumed. The inaccurate state may cause further excessive current at high or low temperatures to affect security and life cycle of the battery. Therefore, a novel state estimation method applicable to various battery surface temperatures is developed in this paper. This method establishes Capacity-Temperature relations and Resistance-Temperature relations from experimental data to predict more accurately battery capacity and resistance in the full temperature range, then applies the Extend Kalman Filter technique to estimate the State of Charge, and an algorithm with multi-parameters constrained to estimate the SOP of LIB. Simulation and experimental results show that the

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21 proposed method can obtain accurate SOP results at different temperatures.

22 **Keywords:** Li-ion battery; State-of-Power; Temperature model; Temperature rising
23 characteristic; algorithm with multi-parameters constrained

24 **1 Introduction**

25 In recent years, electric vehicle (EV) technology has been developed quickly because of
26 increasingly serious energy supply shortage and environmental concerns. As the main power source
27 of EVs, Li-ion battery (LIB) has attracted intensive research. State-of-Power (SOP) is an important
28 evaluation index to characterize the charging or discharging peak power of LIB. SOP is used to
29 evaluate whether the battery pack has sufficient power to meet the starting or acceleration demand of
30 EVs. At the braking state, SOP can help to determine the maximum energy recovered by the battery
31 and thus avoid overcharging. Moreover, accurate SOP estimation result can benefit vehicle
32 performance control by optimizing battery capacity and size [1,2,3]. Therefore, it is important to
33 estimate SOP accurately, and this paper aims to develop a new SOP estimation method which will
34 have a satisfactory accuracy under various temperatures.

35 SOP of LIB is related to battery capacity, resistance, State-of-Charge (SOC) and ambient
36 temperature amongst others [4], and the estimation of SOP needs to consider all these factors. In Ref.
37 [5], Hybrid Pulse Power Characterization (HPPC) method is applied to estimate SOP. This method
38 uses internal resistance, open-circuit voltage (OCV) and cut-off voltage to obtain the peak power of
39 the battery. Another SOP estimation method based on SOC limits (MSL) is introduced in Ref. [6],
40 where discharging peak current is obtained by the current SOC and minimum SOC limit over a
41 given time period. In Ref. [1], a SOP estimation method based on voltage limit is proposed, in which

42 complex but more accurate battery models, such as an Equivalent Circuit Model (ECM) or
43 Combined Model (CM), are applied to build the state-space equations of LIB. The peak current at
44 the voltage limit is obtained to calculate the SOP of the battery.

45 In the above methods, the HPPC method and the MSL are unable to describe the characteristics
46 of lithium batteries accurately due to the inaccurate models used, while the method based on voltage
47 limit ignores the SOC limits and the maximum current provided by the manufacturer. Therefore,
48 these three methods often cause the estimated SOP greater than the actual peak power, and the
49 battery controlled by such an over-estimated SOP will suffer from over-charging, over-discharging
50 or over-current and thus a shortened battery life period.

51 To improve the accuracy of the SOP estimation, some researchers propose the neural network
52 method [7] and Algorithm with Multi-Parameters Constrained (AMPC) [2,3,8,9]. Neural network
53 method is suitable for state estimation of LIB with a high accuracy degree. However, this method
54 relies on a lot of training data and a proper training technique, otherwise its accuracy will be
55 compromised. The AMPC compares the maximum current provided by the manufacturer with the
56 peak currents obtained from two methods: the one based on SOC limit and the one based on voltage
57 limit. Then it chooses the minimum one in order not to exceed the allowed current and power limit.
58 Thevenin equivalent circuit model is used in AMPC to estimate the SOP in Ref. [8]. The
59 electro-chemical polarization battery model is used in [2,3,9] to estimate the peak current at voltage
60 limits, and then the SOP is estimated by AMPC.

61 Major battery state estimation methods are always applied at fixed room temperature (FRT) at
62 20°C, and the parameters of battery capacity and resistance are set as constants. Some methods are

63 applied at fix ambient temperature (FAT) which is equal to the initial battery surface temperature,
64 and the parameters of battery capacity and resistance are set as functions varying with the ambient
65 temperature but not the battery surface temperature. However, significant surface temperature
66 change is inevitable in EV batteries because of the heat generated by the battery itself. Actually,
67 these parameters of LIB change against SOC and battery surface temperatures. And particularly the
68 change of battery temperature will cause sharp fluctuations in those parameters. When the battery
69 surface temperature decreases, the slow kinetics of reactions and the reduced ionic conductivity of
70 electrolyte result in lower capacity and higher resistance of battery [10,11]. Battery impedance online
71 estimation and adaptive power prediction are studied considering such a battery surface temperature
72 problem in [12], however, it studies only the temperature at 10°C.

73 Targeting at these problems, a state estimation method considering battery dynamic surface
74 temperature is proposed in this paper. The effect of battery temperature on the parameters of LIB is
75 studied. The capacity and resistance of the LIB are tested at different temperature to build the
76 temperature models which can help to identify how the parameters of LIB vary against battery
77 temperature. The battery performance model is optimized with the aid of temperature models to
78 describe the dynamic characteristics of the LIB at different temperatures. The Extend Kalman Filter
79 (EKF) technique at DBT is applied to estimate the battery SOC, and then an AMPC at DBT with the
80 constraints from SOC and other parameters is applied for the estimation of battery SOP which will
81 ensure the safe operation and energy recovery efficiency of the battery. Finally Dynamic Stress Test
82 (DST) [13] is carried out under different temperatures to verify the accuracy of the temperature
83 models and SOP estimation algorithm. Compared with existing methods, this new method achieves

84 the complete SOP estimation in the full temperature range with high accuracy. Moreover, this
85 method is simple and suitable for practical application.

86 This paper is organized as follows. Temperature rising characteristic of LIB and temperature
87 models of capacity and resistance are shown in Section 2. An SOP estimation model considering
88 battery temperature is presented in Section 3. The experiments and simulation results are reported in
89 Section 4. The conclusions are presented in Section 5.

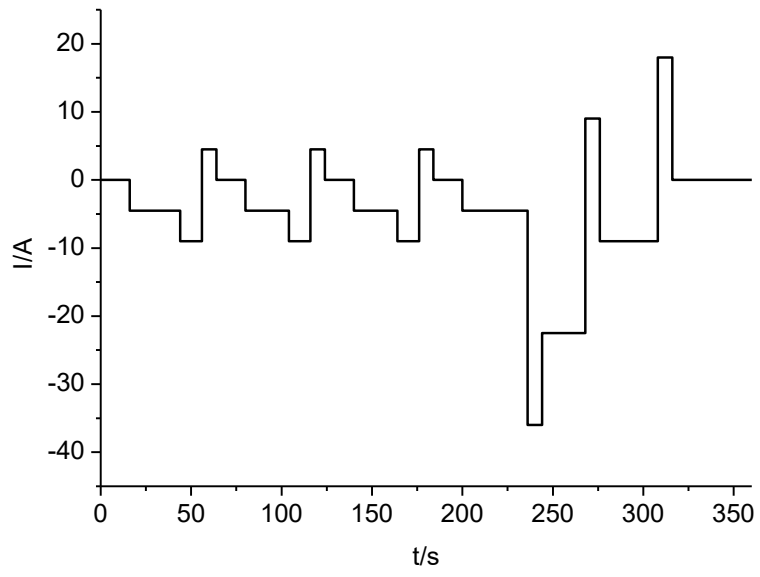
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91 **2 Building the dynamic model of LIB**

92 Since this paper targets to develop a new SOP estimation method applicable to all temperatures,
93 it is necessary to study first how the relevant battery parameters change against temperature. Based
94 on experimental data, this section establishes the relation between temperature, battery resistance
95 and capacity, and then a dynamic model of LIB is built.

96 **2.1 Temperature characteristics of LIB**

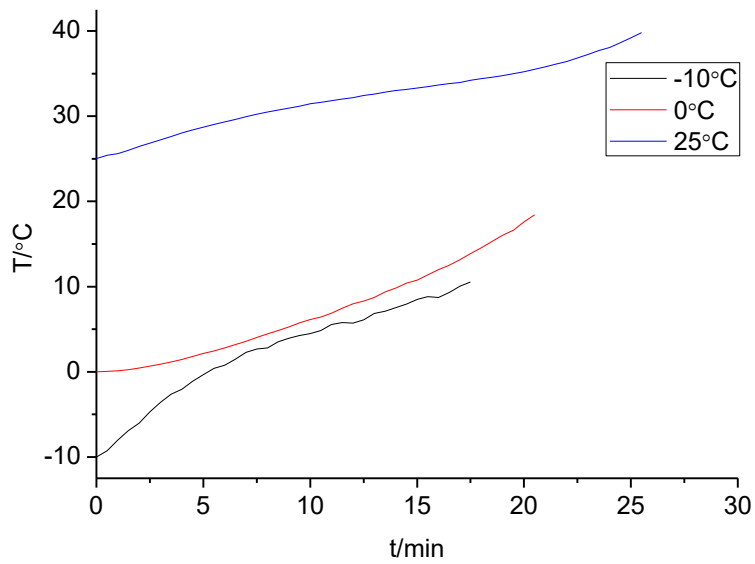
97 The cylindrical LIB of type IFP3213100EA manufactured by Guoxuan High-Tech Power is
98 chose to study its temperature characteristics, and the rated capacity is 9AH. The LIB is placed in an
99 incubator, and ambient temperature in the incubator is set as -10°C, 0°C and 25°C respectively. Then
100 the constant current discharge test of 2C and Dynamic Stress Test (DST) [13] are conducted to
101 observe the temperature rising of the battery, where 2C represents two times of rated battery
102 current. . The DST curve and temperature rising results are shown in Fig.1, Fig.2 and Fig.3:



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Fig.1 Working condition of a single DST



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Fig.2 Surface temperature rising in constant current discharge test of 2C

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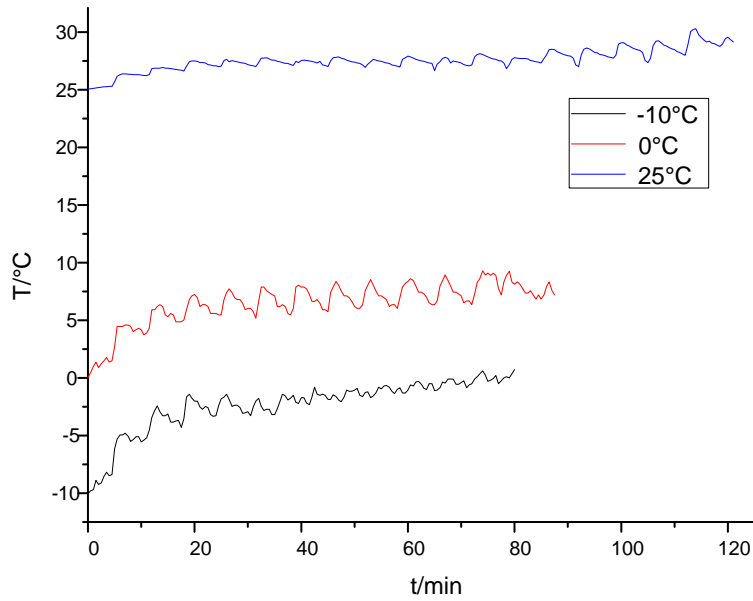


Fig.3 Surface temperature rising of DST

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110 Fig. 1 illustrates the test conditions of a single DST, where the current (in Amperes) at different
 111 time instant is given. Fig.2 and Fig.3 show the surface temperature rising of LIB at different ambient
 112 temperature in constant current discharge test and DST. And the temperature increases significantly
 113 at the discharging process as shown in Table 1:

114

115 Table 1 Results of Battery Surface Temperature Rising at Different Working Condition

Working Condition	Ambient Temperature	Surface Temperature	Temperature increased	Working Time
Constant Current Test	-10°C	10.55°C	20.55°C	17.5 min
	0°C	18.42°C	18.42°C	20.5 min
	25°C	39.81°C	14.81°C	25.5 min
DST	-10°C	0.81°C	10.81°C	80 min
	0°C	8.73°C	8.73°C	91.5 min
	25°C	30.06°C	5.06°C	121 min

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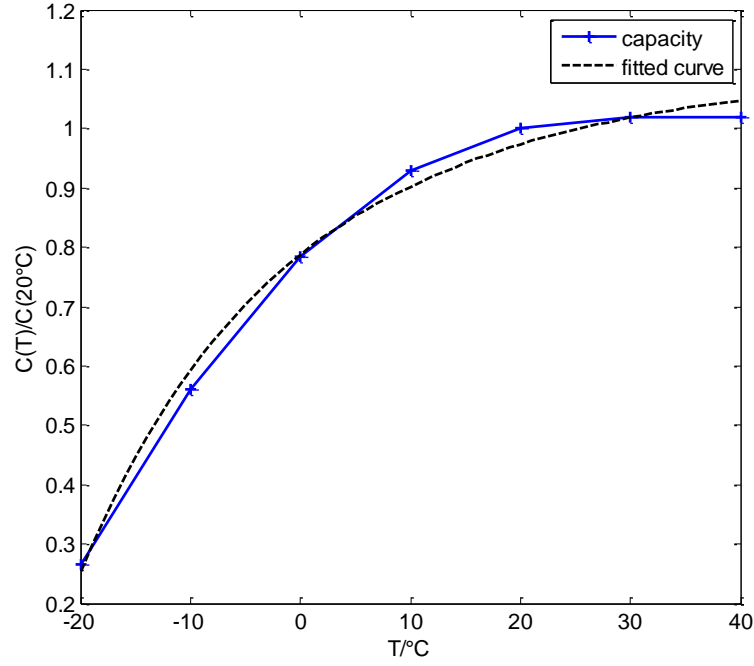
117 The ambient temperature, the battery surface temperature and the temperature increased after
 118 the whole discharging process from 100% SOC to the protection voltage, the continuous working

119 time are shown in Table 1. Fig.2, Fig.3 and Table 1 show that the temperature rises quickly at low
120 ambient temperatures. If we compare the results at the same time interval, the conclusion is more
121 obvious. The heat at the battery discharge process consists of the heat from resistance and the heat
122 from chemistry reactions, where the heat from resistance occupies the majority of the heat [14]. So
123 the underlying reason of the quick temperature rise is that the resistance is higher at low
124 temperatures, and thus low ambient temperature has a more significant impact on state estimation of
125 LIB.

126

127 **2.2 Temperature model of battery capacity**

128 In order to find out how the battery usable capacity changes at different temperatures, a fully
129 charged battery is discharged with constant current at different temperatures in an incubator. To
130 avoid the impact of temperature rising on capacity test, the discharging current is set as 0.1C, and
131 the surface temperature is detected in real time to ensure that the battery temperature rises within a
132 permitted range. The ambient temperature is set as -20°C, -10°C, 0°C, 10°C, 20°C, 30°C and 40°C
133 in turn. The measured LIB usable capacities under different temperatures are shown in Fig. 4.



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Fig.4 Usable capacities of LIB under different temperatures

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In Fig.4, the vertical axis is the ratio of capacity under the current temperature and usable capacity under room temperature (20°C), the horizontal axis is the ambient temperature. The figure shows that the LIB usable capacity decreases fast at lower ambient temperatures. At -20 °C, the capacity is only about 30% of the rated capacity which is measured at room temperature (20°C). As the temperature rises, the change rate of the usable capacity gradually reduces. At 40°C, the capacity is about 105% of the rated capacity.

Capacity temperature compensation coefficient $\lambda_C = C_T / C_0$ is defined to characterize the effect of temperature on LIB capacity, where C_T is the capacity at temperature T , C_0 is the capacity at 20°C. The curve is fitted by the Arrhenius equation [15], and λ_C can be expressed as:

$$\lambda_C = C_T / C_0 = B_C * e^{-E_a^C / RT} + A_C \quad (1)$$

where B_C is the pre-exponential factor, E_a^C is the activation energy, R is the gas constant, T is the absolute ambient temperature, A_C is Arrhenius correction factor. The fitted curve is shown as the

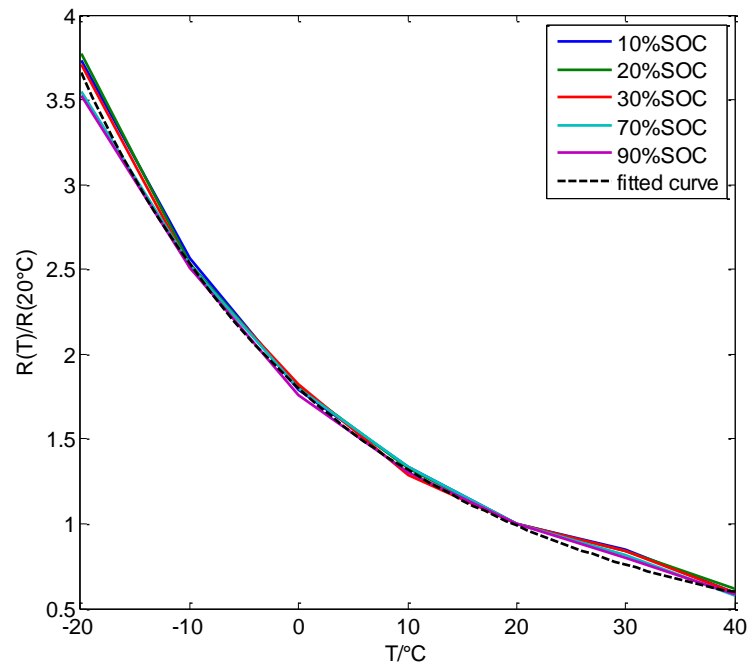
148 dashed line in Fig. 4, which is close to the measured capacity points.

149

150 2.3 Temperature model of battery resistance

151 In order to find out how the battery resistance changes at different temperatures and SOC, the
152 Hybrid Pulse Power Characteristic (HPPC) [16] test is conducted, where the resistance refers to the
153 total battery resistance. Firstly, a fully charged battery is put in the incubator of 40°C and discharged
154 with constant current of 1/3C to the SOC of 90%, 70%, 50%, 30% and 10% successively, and the
155 HPPC tests are conducted at each SOC to obtain the resistance of the LIB. Then, change the
156 incubator temperature to 30°C, 20°C, 10°C, 0°C, -10°C and -20°C, repeat the above steps, and
157 measure the battery resistance.

158



159

160 Fig.5 Resistance of LIB under different temperatures and SOC

161 Fig.5 shows how the resistance varies at different temperatures and SOC. The vertical axis is
162 the ratio of resistance at the current temperature to the resistance at 20°C, and the horizontal axis is

163 the ambient temperature. The dashed line is the fitted curve. The figure shows that the resistance
 164 changes fast at low ambient temperatures. Furthermore, the resistances at different SOCs (higher
 165 than 10%) remain almost the same when temperature is fixed. Therefore, the impact of SOC on
 166 resistance can be ignored when the battery SOC is higher than 10%. As shown in Ref. [11], the
 167 resistance of the battery changes fast when SOC is lower than 10%, so the effect of SOC on
 168 resistance cannot be ignored when SOC is lower than 10%.

169 Resistance temperature compensation coefficient $\lambda_R=R_T/R_0$ is defined to characterize the
 170 effect of temperature on the LIB resistance, where R_T is the resistance at temperature T , R_0 is the
 171 resistance at 20°C. The curve is fitted by Arrhenius equation, and λ_R can be expressed as:

$$172 \quad \lambda_R=R_T/R_0=B_R * e^{-E_a^R/RT} + A_R \quad (2)$$

173 where B_R is the pre-exponential factor, E_a^R is the activation energy, R is the gas constant, T is
 174 the absolute ambient temperature, A_R is Arrhenius correction factor. The fitted curve is shown as the
 175 dashed line in Fig.5, which is close to the measured resistance points.

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177 **2.4 Dynamic model of LIB**

178 In order to estimate the SOP of LIB accurately, the battery model should be built first. Widely
 179 used battery models are electrochemical model [17], equivalent circuit model [18, 19] and neural
 180 network model [20]. The electrochemical reaction mechanism of LIB is very complex. Therefore,
 181 the simplified electrochemical model such as the Shepherd, Unnewehr, Nernst model is used to
 182 describe the battery characteristics. Equivalent circuit model in [18, 19] describes the LIB from
 183 external electrical characteristics and PNGV, Thevenin and Rint model are typical equivalent circuit
 184 models. The calculation of neural network model in [20] is too complicated, and the estimation error

185 will be affected by the training data and training methods. Thus the combined electrochemical
 186 model (CM) from [1, 21, 22] is used in this paper. This CM consists of the Shepherd, Unnewehr and
 187 Nernst model, which solves the problem that the three models only match partially the LIB voltage
 188 characteristic: For example, the Shepherd model only considers the end of battery charge and
 189 discharge, and the Unnewehr model cannot express the voltage platform. Thus the CM model can
 190 provide better fitting in the whole charge and discharge interval. However, the effect of temperature
 191 on battery parameters is ignored which will lead to the poor accuracy at low temperatures. Therefore,
 192 the above temperature models are merged to this combined electrochemical model to describe the
 193 dynamic behavior of LIB at various temperatures. Details are given below:

$$194 \quad \text{SOC}(t) = \text{SOC}(0) - \int_0^t \eta i(t) dt / (\lambda_C C_0) \quad (3)$$

$$195 \quad \begin{aligned} E(t) = & E_0 - \lambda_R R_0 i(t) - K_0 / \text{SOC}(t) - K_1 \text{SOC}(t) \\ & + K_2 \ln(\text{SOC}(t)) + K_3 \ln(1 - \text{SOC}(t)) \end{aligned} \quad (4)$$

196 where $\text{SOC}(t)$ is the instantaneous SOC at time t , $\text{SOC}(0)$ is the initial SOC, η is the
 197 charging/discharging efficiency, $i(t)$ is the current at time t , C_0 is the capacity at room
 198 temperature, $E(t)$ is the terminal voltage at time t , E_0 is the OCV of the fully charged battery,
 199 R_0 is the resistance at room temperature, K_0 , K_1 , K_2 and K_3 are constants. λ_C and λ_R are
 200 capacity and resistance temperature compensation coefficient respectively.

201 **3 SOP estimation considering battery temperature**

202 **3.1 SOC estimation method**

203 Extended Kalman Filter (EKF) is a popular algorithm to solve the nonlinear system state
 204 estimation problem [22]. Now Eq. (3) and Eq. (4) are discretized to obtain the state-space model of
 205 LIB. Let $x_k = \text{SOC}_k$, $y_k = E_k$, $u_k = i_k$, then:

$$x_k = f(x_{k-1}, u_{k-1}) + w_k = x_{k-1} - \eta u_{k-1} \Delta t / (\lambda_C C_0) + w_k \quad (5)$$

$$y_k = g(x_k, u_k) + v_k = E_0 - \lambda_R R_0 u_k - K_0 / x_k - K_1 x_k + K_2 \ln(x_k) + K_3 \ln(1-x_k) + v_k \quad (6)$$

Linearizing Eq. (6) and Eq. (7), and we will obtain:

$$\begin{cases} x_k = Ax_{k-1} + Bu_{k-1} + w_k \\ y_k = Cx_k + Du_k + E + v_k \end{cases} \quad (7)$$

$$\text{where } A = \frac{\partial f(x_{k-1}, u_{k-1})}{\partial x_{k-1}} \Big|_{x_{k-1} = \hat{x}_{k-1} = 1},$$

$$B = -\eta \Delta t / (\lambda_C C_0),$$

$$C = \frac{\partial g(x_k, u_k)}{\partial x_k} \Big|_{x_k = \hat{x}_k} = \frac{K_0}{(\hat{x}_k)^2} - K_1 + \frac{K_2}{\hat{x}_k} - \frac{K_3}{1 - \hat{x}_k},$$

$$D = -\lambda_R R_0,$$

$$E = V_0 \frac{2K_0}{\hat{x}_k} + K_2 (\ln \hat{x}_k - 1) + K_3 (\ln(1 - \hat{x}_k) + \frac{\hat{x}_k}{1 - \hat{x}_k}).$$

In EKF estimation method, SOC is calculated with AH integral method, and put into the observation equation to calculate the Kalman gain of each step. It reflects the residuals on the state variable weights of SOC, and then the optimal SOC estimation is obtained from the updated state estimation equation.

219

3.2 SOP estimation with AMPC

In order to ensure the accuracy of the SOP estimation, the AMPC is combined with EKF to estimate the SOP of LIB. Within a short time duration Δt , the battery can be assumed to be discharged at a constant current, and after the short time Δt about 10 seconds [13,24], $\text{SOC}(t+\Delta t) = \text{SOC}_{\min}$ or $V(t+\Delta t) = V_{\min}$. Then the discharge peak power is

$$\text{SOP}(t) = i_{\max}(t) E(t, i_{\max}(t)) \quad (8)$$

226 where $SOP(t)$ is the instantaneous state of charge at time t , $i_{\max}(t)$ is the estimated peak current at
 227 time t , $E(t, i_{\max}(t))$ is the terminal voltage at time t when the current is $i_{\max}(t)$.

228 Based on the above models, the peak current can be calculated from SOC limit, which is
 229 denoted by u_{\max}^{SOC} and equals:

$$230 \quad u_{\max}^{\text{SOC}} = B^{-1}(x_k - x_{\min}) \quad (9)$$

231 This peak current can also be calculated from voltage limit, which is represented by u_{\max}^{volt} and
 232 equals:

$$233 \quad u_{\max}^{\text{volt}} = D^{-1}(y_{\min} - Cx_k - E) \quad (10)$$

234 Note also that manufacturers also provide the rated battery maximum current, which is denoted
 235 by u_{\max} , therefore, these notations can be combined together and the following maximum allowed
 236 peak discharge current u_{\max}^{dis} is defined as

$$237 \quad u_{\max}^{\text{dis}} = \min(u_{\max}, u_{\max}^{\text{SOC}}, u_{\max}^{\text{volt}}) \quad (11)$$

238 Therefore, the maximum allowed discharge peak power is

$$239 \quad SOP_{\max}^{\text{dis}} = u_{\max}^{\text{dis}} y(k, u_{\max}^{\text{dis}}) \quad (12)$$

240 The detail SOC and SOP estimation process is shown as follows:

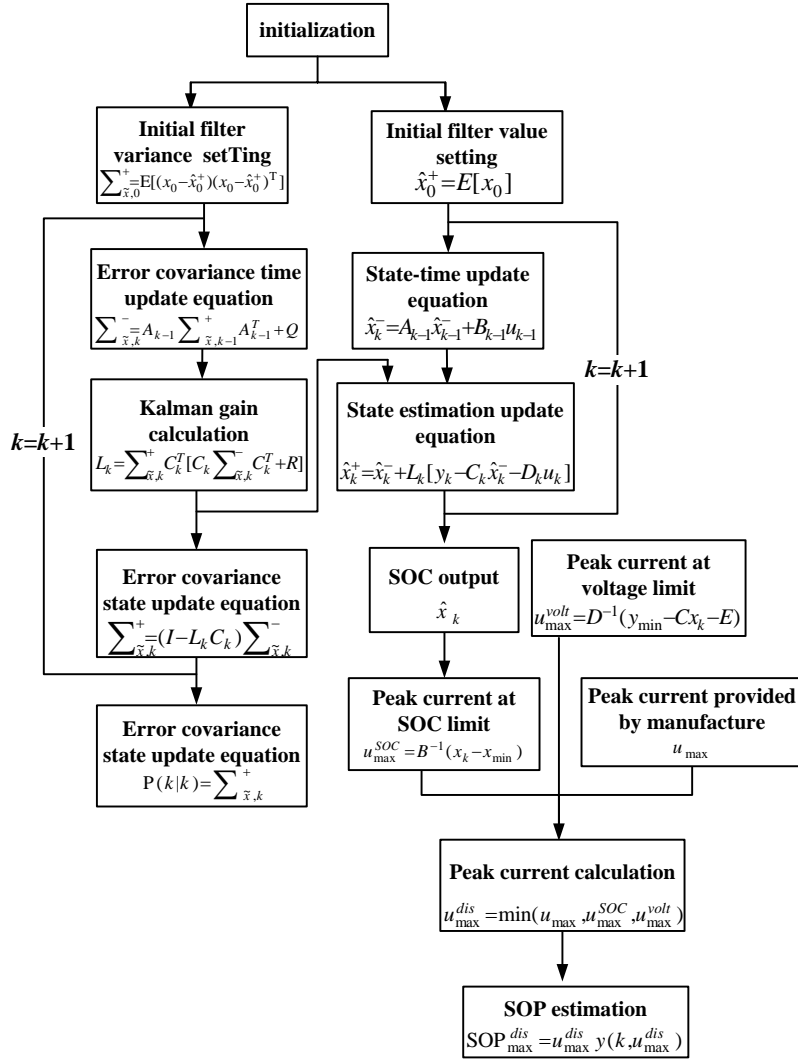


Fig.6 SOP estimation flow chart

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Form the above flow chart, we can see that the algorithm is very simple and straightforward,

and it is suitable for practical engineering applications such as Battery Management System (BMS).

In order to validate the accuracy of the estimation algorithm, the simulations and experiments are

conducted in Section 4.

4 Simulations and Experiments

4.1 Parameters identification

In order to identify the model parameters, we choose the 9Ah Lithium iron phosphate battery

250 and conduct the constant current discharge test and HPPC test. The measured data are fitted by
 251 Arrhenius equation to obtain the temperature models of capacity and resistance as shown in Fig.4
 252 and Fig.5. The model parameters are identified by the least squares method, and the results of
 253 parameters for the temperature models of battery capacity and residence are shown in Table 2 and
 254 Table 3:

255 Table 2 Parameters for the temperature model of battery capacity

Parameter	B_C	E_a^C	A_C
Value	$-1.683 \cdot 10^{-6}$	$-2.77 \cdot 10^4$	1.117

257 Table 3 Parameters for the temperature model of battery residence

Parameter	B_R	E_a^R	A_R
Value	$1.861 \cdot 10^{-4}$	$-2.08 \cdot 10^4$	$5.23 \cdot 10^{-2}$

259 4.2 The Dynamic Battery Model Validation

260 In order to validate the dynamic model in Eq. (4), a single LiFePO₄ cell with a nominal capacity
 261 of 9Ah is chosen to be tested in an incubator with the temperature of -10°C, 0°C and 25°C
 262 successively. The battery is fully charged and the DST curve is chosen as the discharge curve which
 263 is provided in “USABC Electric vehicle battery test procedures manual” [13]. And the comparison
 264 between the voltage response curve of the dynamic model, the voltage response of the initial model
 265 and the test voltage is shown as follows.

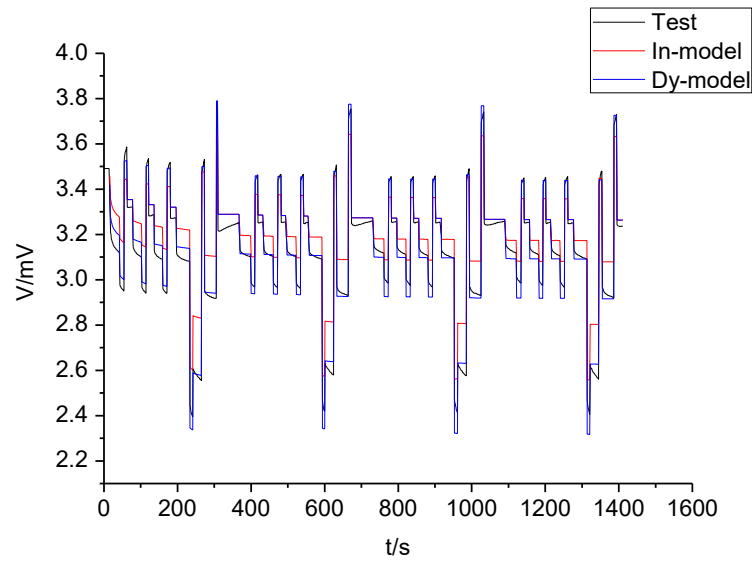


Fig.7 The validation of dynamic model

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268 In Fig.7 the voltage response curve of the dynamic model (Dy-model), the voltage response of
 269 the initial model (In-model) and the test voltage (Test) are shown respectively. The proposed
 270 dynamic battery model is obviously better than the initial model.

271 4.3 SOC Estimation Validation

272 The single LiFePO_4 cell with a nominal capacity of 9Ah is chosen to be tested in an incubator
 273 with the temperature of -10°C , 0°C and 25°C successively. The battery is fully charged and the DST
 274 curve is chosen as the discharge curve which is provided in “USABC Electric vehicle battery test
 275 procedures manual” [13]. The SOC at fixed room temperature (SOC at FRT), the SOC at fixed
 276 ambient temperature (SOC at FAT), the SOC at dynamic battery temperature (SOC at DBT) and the
 277 real SOC are shown as follows:

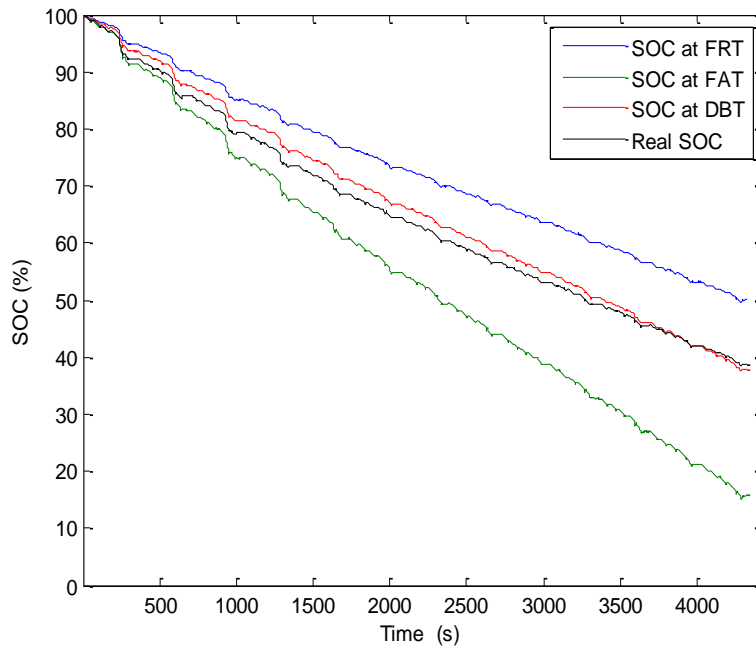


Fig.8 SOC estimation result at -10°C

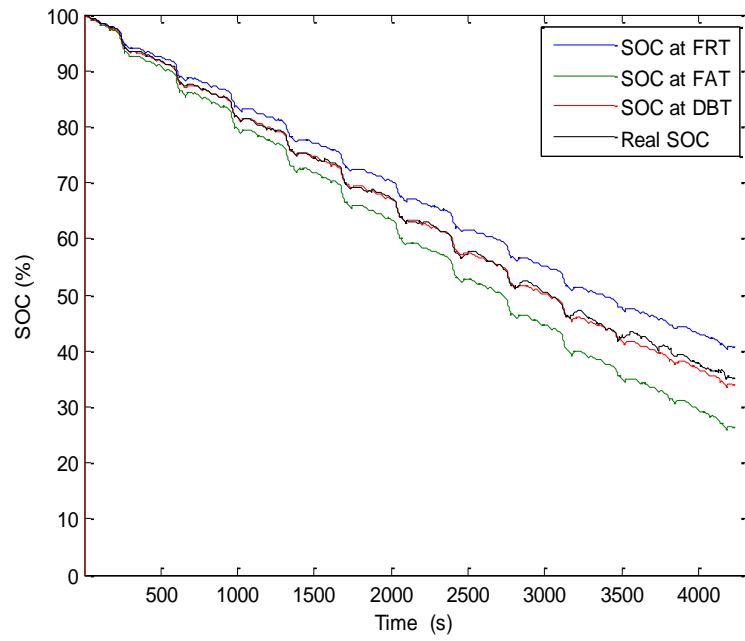


Fig.9 SOC estimation result at 0°C

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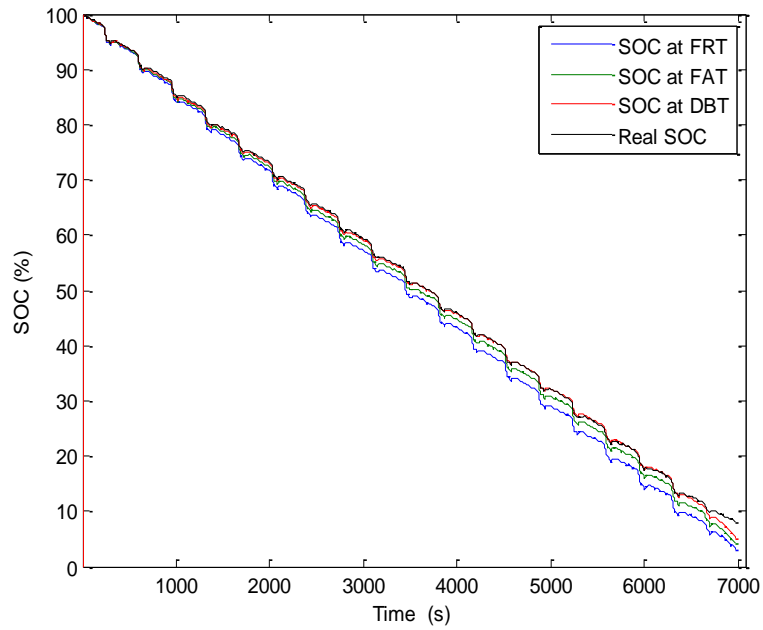


Fig.10 SOC estimation result at 25°C

In Fig.8, Fig.9 and Fig.10, the SOC estimation curves after DST at temperature of -10°C, 0°C and 25°C are shown respectively. And the maximum errors are shown in Table 4:

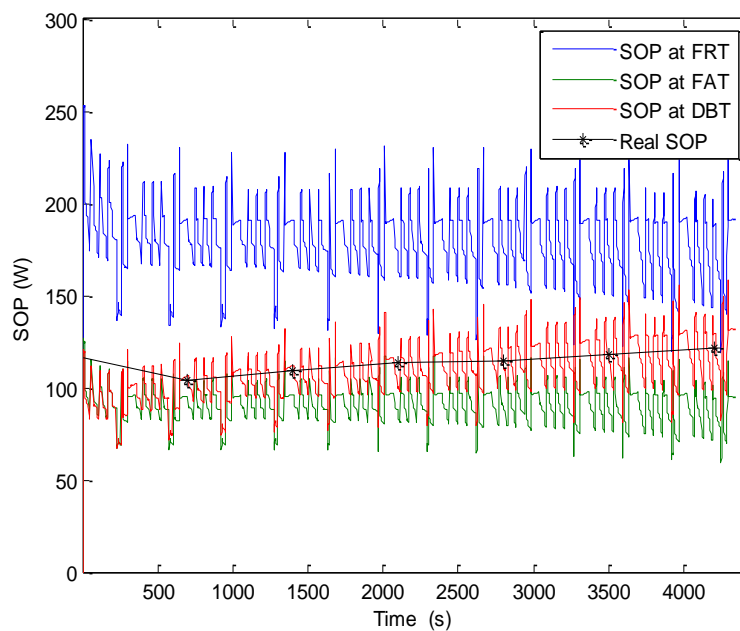
Table 4 Maximum Errors of SOC Estimation at FRT, FAT and DBT

Ambient Temperature	Max-error of FRT	Max-error of FAT	Max-error of DBT
-10°C	11.89%	22.40%	3.66%
0°C	5.92%	9.61%	2.07%
25°C	4.91%	3.93%	2.94%

From Table 4, we can see that the error of SOC at DBT is smaller than SOC at FRT and SOC at FAT, especially at low temperature. The reason is that the resistance of LIB is higher at low temperatures, so the battery temperature rises higher at DST. Besides, same temperature variation has a bigger impact on the parameters at low temperature as shown in Fig. 4 and Fig. 5. These reasons cause a poor performance of SOC estimation methods which do not consider temperature impact.

295 **4.4 SOP Estimation Validation**

296 In order to verify the SOP estimation algorithm, the real SOP of the battery at different
297 temperature needs to be tested. The test method recommended in [24] is adopted in this paper. The
298 battery is discharged and charged alternatively with the current of 1C, 2C, 5C and 10C at certain
299 SOC and temperature shown in Fig.2 and Fig. 3. In this process, the voltage of the battery is
300 recorded and fitted to obtain the maximum current at the cut-off voltage. Then the peak power of the
301 battery at any SOC and temperature point is the multiplication of the cut-off voltage and maximum
302 current. The SOP at fixed room temperature (SOP at FRT), the SOP at fixed ambient temperature
303 (SOP at FAT), the SOP at dynamic battery temperature (SOP at DBT) and the real SOP are shown as
304 follows:



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Fig.11 SOP estimation result at -10°C

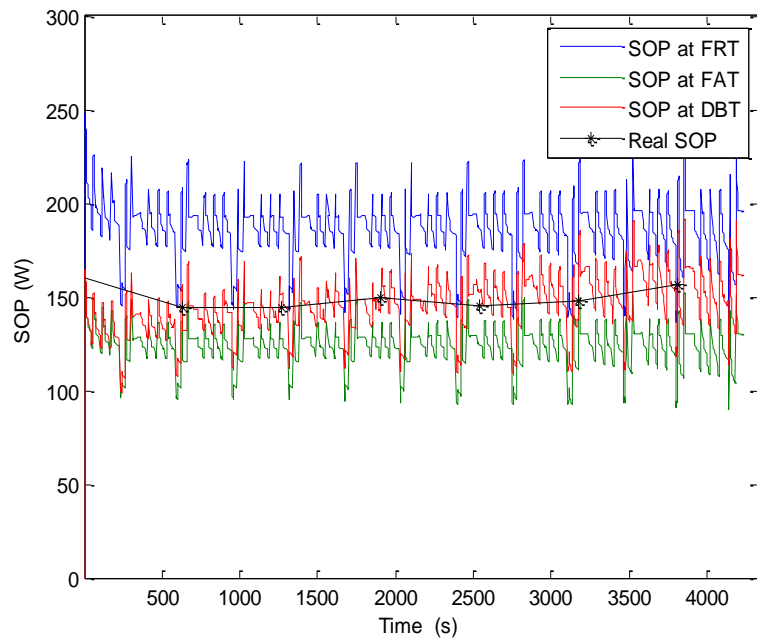


Fig.12 SOP estimation result at 0°C

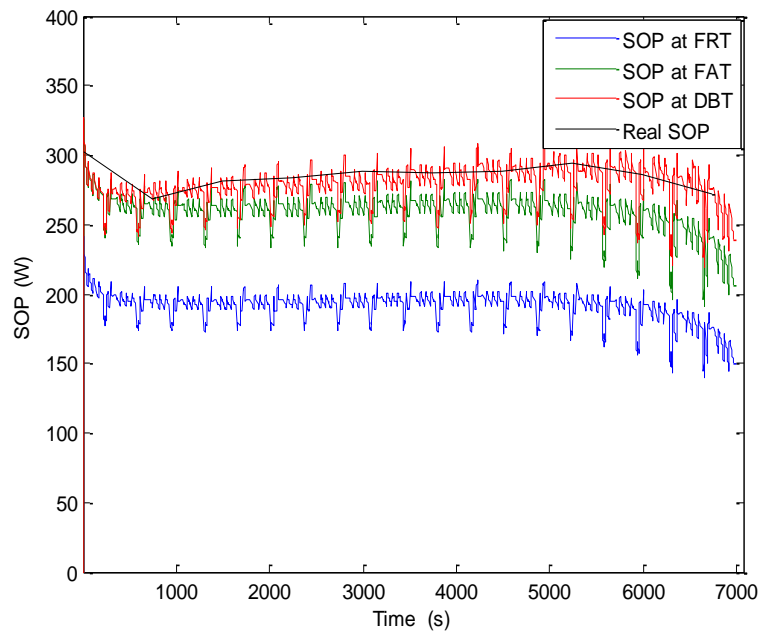


Fig.13 SOP estimation result at 25°C

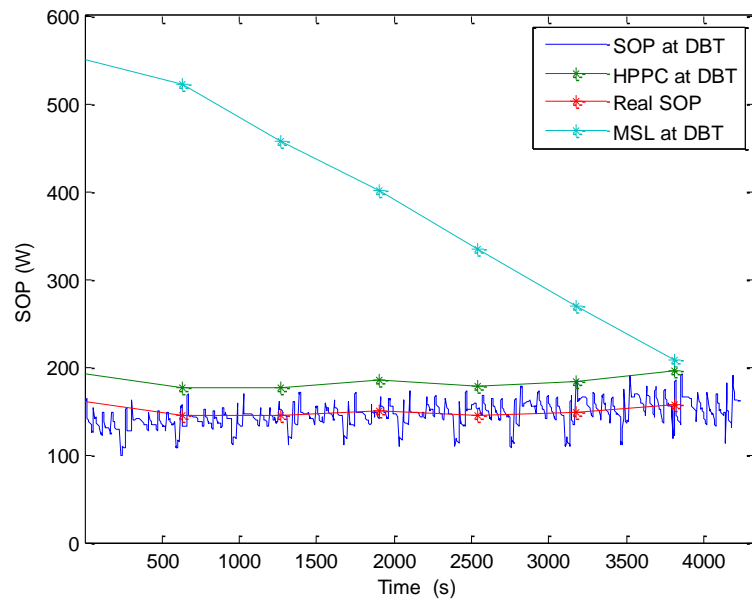
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312 In Fig.11, Fig.12 and Fig.13, the SOP estimation curves after DST and the real SOP at
313 temperature of -10°C, 0°C and 25°C are shown respectively. In these figures, SOP at DBT which is
314 nearer to the real SOP curve performs better than SOP at FRT and SOP at FAT. Comparing the three

315 SOP curves, we will see that the result of SOP at FRT is higher than the results of SOP at FAT and
 316 DBT at low temperatures; but it is lower at high temperatures. The reason is that the battery
 317 resistance is higher at low temperatures and lower at high temperatures. When comparing SOP at
 318 FAT and DBT, the result of DBT is nearly the same with the result of FAT at the initial discharging
 319 process. The results of SOP at DBT increase quicker than SOP at FAT because the battery capacity
 320 increases and resistance decreases due to the rising temperature. Thus, the SOP at FRT will lead to
 321 higher peak power which exceeds the one withstood by the battery at lower temperatures, and the
 322 SOP at FAT will lead to lower peak power which cannot ensure effectively battery performance.

323 When compared to the HPPC method and the method based on SOC limits (MSL) at dynamic
 324 battery temperatures, the following Fig. 14 is obtained.



325

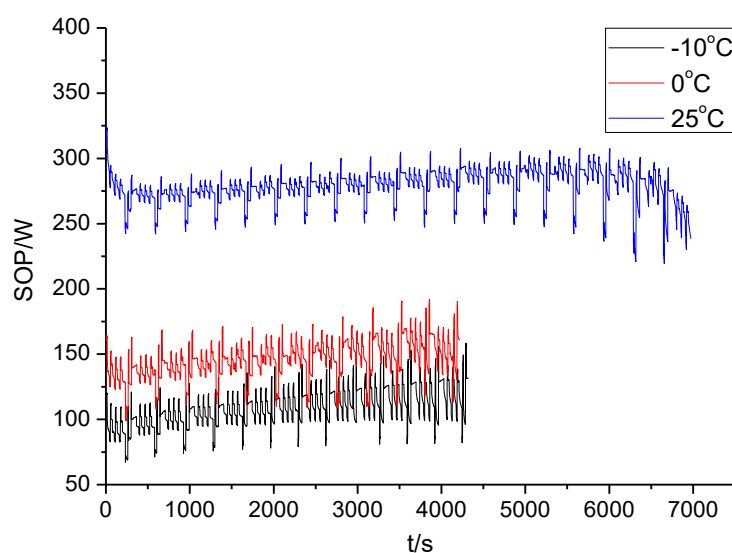
326

Fig.14 SOP estimation result at 0°C

327 In Fig.14, the SOP estimation curves with different methods after DST and the real SOP at
 328 temperature 0°C are shown respectively. As analyzed in Section 1, the SOP with HPPC and MSL
 329 method are high than the proposed methods (SOP at DBT). Especially, the results of MSL methods

330 is much high than the Real SOP.

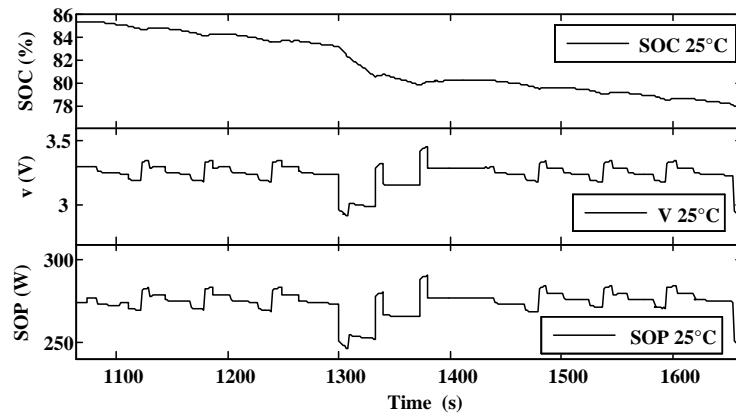
331 Analyzing the SOP estimation results at different temperature further in Fig. 15, it is found that
332 the peak discharge currents are around 3.62C, 5.42C and 10.13C at temperature of -10°C, 0°C and
333 25°C respectively, which means that the LIB is unable to achieve a high discharging rate and cannot
334 meet the demands of starting or acceleration of the electric vehicle at low temperature. Thus, heating
335 equipment and thermal insulations must be added to the LIB pack to meet the driving demand at low
336 temperatures.



337

338 Fig.15 SOP estimation results at different ambient temperature

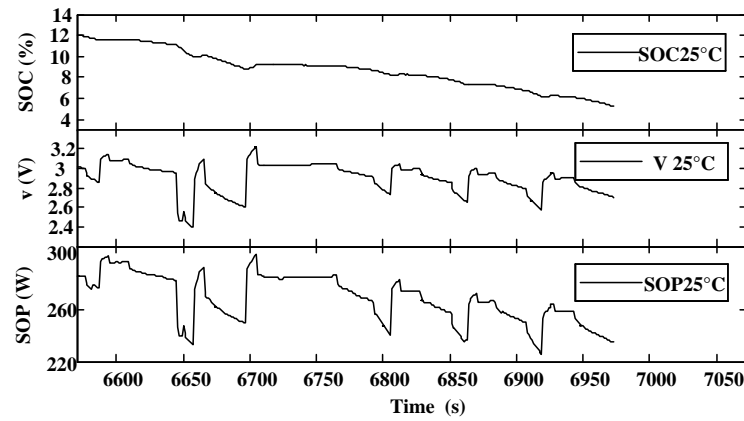
339 The battery SOP, SOC and terminal voltage are compared at the discharge platform of the LIB
340 and the end of discharge at 25°C in Fig. 14 and Fig. 15. The SOC intervals are 77.23%~85.41% and
341 5.12%~12.03% respectively.



342

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Fig.16 Comparison of SOC, terminal voltage and SOP of LIB at voltage platform



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Fig.17 Comparison of SOC, terminal voltage and SOP of LIB at the end of discharge

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As shown in Fig.16 and Fig.17, the SOP changing trend is nearly the same with the terminal voltage at the discharge platform, and the impact of SOC to SOP is minor. Therefore, battery terminal voltage can reflect the peak power to certain extent. However, at the end of the discharge, the SOP decreases faster than the battery terminal voltage due to a rapid increase in battery resistance where the SOC is lower than 10%. So the battery will have to withstand a greater impulse current if only the terminal voltage is used as the control parameter, and this might damage the system security and battery life.

353 **5 Conclusions**

354 At low temperatures, key LIB characteristic parameters, such as battery capacity and resistance,
355 change significantly when the ambient temperature is low. In this paper, a new SOP estimation
356 method is developed, which includes the establishment of battery temperature, capacity and
357 resistance based on experimental data, and also a combination of the AMPC method and the EKF
358 technique to study the impact of temperature to SOP. The following conclusions can be obtained
359 after analyzing the SOP estimation results:

360 1) The newly proposed SOP estimation algorithm performs better than the algorithm at fixed
361 room temperature and the algorithm at fixed ambient temperature. And also the proposed method
362 shows high accuracy when compared to the existing method at dynamic battery temperatures.

363 2) The SOP curve shows the same trend with the terminal voltage of the discharge platform,
364 and decreases faster at the end of discharge. Thus, system security and battery life will be damaged
365 if the terminal voltage at the end of discharge is used as the only control parameter.

366 3) The peak power of LIB decreases with the decreasing temperature. The peak current of the
367 voltage platform is only 3.62C at the temperature of -10°C and cannot meet the demands of vehicle
368 starting and acceleration. Thus, heating equipment and thermal insulations must be added to the LIB
369 pack at low temperature.

370

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374

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