Magnetic properties of stoichiometric and defective Co_9S_8

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In this paper, we present a detailed study of the stoichiometric and reduced Co_9S_8 pentlandite magnetic properties, based on density functional theory. We analyze both its geometry and electronic properties and show that only by the inclusion of the Hubbard term it is possible to correctly describe d-d splitting, which is necessary to accurately characterize the Co_9S_8 spin configuration and its antiferromagnetic nature. We also analyze the effect of sulfur vacancies and predict the formation of ferromagnetic clusters that give local ferromagnetic character to non-stoichiometric Co_9S_8 , which may explain the contradictory experimental results reported in the literature.

I. INTRODUCTION

Transition metal sulfide (TM-S) nanomaterials have attracted much attention due to their excellent properties and promising applications in electronic, optical, and optoelectronic devices as well as in spintronics.¹ The production of novel TM-S structures with the desired magnetic properties is crucial for the fabrication of innovative technological devices.¹⁻³ In particular, TM-S compounds with antiferromagnetic (AFM) properties are attractive due to the numerous features they offer compared to more common ferromagnetic (FM) compounds. These features include a stable coupled moment when exposed to external magnetic fields, stability in multiple magnetic configurations, and higher magnetic ordering temperatures. Furthermore, AFM characteristics typically appear in insulating materials, with only few examples of AFM metals, which makes the investigation of such systems attractive.

Cobalt sulfide is present in several phases with different stoichiometries. The magnetic susceptibility measurements of various phases of cobalt sulfides reveal that CoS and Co₄S₃ exhibit temperature-independent paramagnetism, Co₃S₄ has AFM characteristics, and CoS₂ is ferromagnetic with a Curie temperature of 116 K.^{4,5} However, observation of a high magnetic-ordering temperature in transition metal sulfides is uncommon.⁶

Metallic Co_9S_8 has been investigated for its catalytic properties, however its magnetic properties have only been partially analyzed, and the literature reports contradictory results.^{4,6,7} In particular, the paper by Heidelberg *et al.*,⁷ which is based on susceptibility measurement, suggests an AFM character occuring below the Néel temperature of 300 K, which was also reported by Lai *et al.*.⁴ On the other hand, Kumar *et al.*⁶ concluded that Co_9S_8 exhibits the magnetic hysteresis typical of a ferromagnet at room temperature, with a magnetization peak at low temperature, Luo *et al.*⁸ observed a paramagnetic character in Co_9S_8 microspheres at room temperature, whereas Pasquariello *et al.* reported an observed a ferromagnetism resulting from the formation of a small amount of cobalt metal during synthesis.⁹ Furthermore, computational-theoretical studies report no magnetic order, and classify this material as non-magnetic.^{10,11}

These contradictory results in the literature suggest that the measured magnetic nature of Co_9S_8 may be due to the specific experimental conditions. The local stoichiometry of the crystal, in particular, could play a fundamental role in the measured macroscopic properties, as reported for similar crystals.^{12–16}

Here we describe our first-principles investigation, to elucidate the magnetic nature of Co_9S_8 . We analyse the geometries, energetics and electronic structure of stoichiometric and defective Co_9S_8 , with a focus on the role of sulfur vacancies in the magnetic order of this crystal.

II. CALCULATION METHODS

We performed the calculations presented in this work using Density Functional Theory (DFT), within the Generalized Gradient Approximation (GGA) using the Perdew-Burke-Ernzerhof functional (PBE) for the exchange-correlation term.¹⁷ To describe the d-d splitting in a way that is consistent with experimental results, we must include a Hubbard correction with $U_{\text{eff}}(\text{Co}_{3d})$ between 2 eV and 5 eV. Here, we use $U_{\text{eff}}(\text{Co}_{3d})=5$ eV, in line with Assadi *et al.*, and $U(\text{Co}_{3d})=0$ eV to measure the effect of the d - d splitting on the calculated magnetic order.^{18–20}. We use periodic boundary conditions and a plane waves basis set as implemented in the simulation package VASP, wherein the core-valence interaction is described by Projector Augmented Wave Pseudopotential.²¹⁻²⁴ We use a cut-off energy for the valence electrons of 500 eV, and use a $3 \times 3 \times 3$ k-point mesh for the primitive cells consisting of 17 atoms, and for the super-cell consisting of 34 atoms constructed by merging two primitive cell along the x direction. We performed full geometry optimization including spin polarization, with the convergence criteria for the energy and forces being 10^{-6} eV and 10^{-2} eV/Å, respectively.

III. RESULTS

A. Geometry and Electronic Structure of Stoichiometric Co_9S_8

 Co_9S_8 crystalyzes in a Fm3m pentlandite structure with a measured lattice constant of 9.92 Å.^{25,26} After geometry optimization, we obtained a small distortion of the primitive cell from the perfect trigonal structurea lattice and a lattice constant of a=10.20Å, which is larger than the one reported in other computational studies due to the different magnetic order obtained and the effect of the Hubbard correction, and also larger the experimental value in line with other computational works that adopt a similar methodology.^{2710,11,28–30} Primitive cell of Co_9S_8 pentlandite can be thought of as a packing of four Co atoms bonded to S atoms in tetrahedral coordination (Co^{tetra}), forming two Co_4S_4 complexes, which are connected through a Co site in a octahedral coordination (Co^{octa}) , as schematically depicted in Fig.1. Six coordinated Co atoms have symmetry O_h , and four coordinated Co are trigonally distorted with local C_{3v} symmetry, with one short and three longer Co-S distances. The two non equivalent sulfur sites (S1 and S2) are either shared by Co^{octa} and Co^{tetra} , with calculated bond lengths for Co^{octa} -S1 of 2.52 Å and for Co^{tetra} -S1 of 2.37 Å, or shared only by Co^{tetra} with a 2.33 Å Co^{tetra} -S2 distance.

We start with an intuitive consideration of the possible magnetic nature of $\mathrm{Co}_9\mathrm{S}_8$ within crystal field theory (CFT), while also considering that the formal oxidation states approach does not consider the mixed nature of the atomic bonding in real crystals. CFT predicts the splitting of the 3d electrons of Co, which depends only on atomic coordination. For example, in the more common cobalt oxide Co_3S_4 , the Co(II)/Co(III) ions are considered to occupy the tetrahedral and octahedral sites, respectively. However, the description of the oxidation state of Co_0S_8 may differ from the more common phases, due to the unusually low oxidation state of octahedral Co. The low concentration of S anions, indicates that Co atoms are in a low oxidation state with a mix of Co^{tetra} in d^7 , and possibly that the uncommon Co^{octa} species are also in low oxidation state d^7 , with a density of 8/9 Co^{tetra} and 1/9 Co^{octa} . Here, the stability of the Co in the $3d^74s^0$ configuration for fourfold tetrahedral coordinated sites is expected, having been demonstrated in symilar crystals by Walsh *et al.*.¹⁸

The local crystal field splits the tetrahedral Co 3d states into low energy e_g and high energy t_{2g} with a d-d energy split of the order of 1.5-2.0 eV, which results in a high spin configuration $(e_g^4 t_{2g}^3)$ with a local magnetic moment $\mu_B \sim 3.^{31}$

On the other hand, octahedral Co splits 3d levels into high energy e_g and low energy t_{2g} that, given the d-denergy split, favour a low spin configuration with no magnetic moment for the common d^6 electron configuration. However, since Co in a low oxidation state, the electronic



FIG. 1. (Color online) Schematic representation of the Co_9S_8 bulk unit cell employed in our calculations. Blue and yellow spheres represent cobalt and sulfur atoms, respectively.

configuration of this specific crystal, may present a significant deviation from this analysis. Our results consistently show that for each of the energetically favourable and stable structures, tetrahedral Co favours a high spin configuration with a magnetic moment $\sim 2.65 \mu_B$. However, the calculated octahedral Co magnetic moment is $\sim 1.68 \mu_B$, suggesting that Co^{octa} is forced into a d^7 configuration, as shown in schematic in Fig.2.



FIG. 2. (Color online) Schematic representation of d-d splitting, as described within Crystal Field Theory, for Co_9S_8 octahedral and tetrahedral Co in the d^7 configuration.

The calculated energies for the unit cell in different spin configuration, i.e. FM and three AFM. favour an AFM character, with an energy gain of $\Delta_{E_{AFM}-E_{FM}} = 0.4$ eV per unit formula, as reported in Tab.3. Figure 3 shows the favourable spin configuration AFM2, together with the other configurations used in our calculations. The magnetic moment at Co^{tetra} is 2.65 μ_B and that at Co^{octa} is 1.68 μ_B , which gives a good description of the predicted spin configuration of Co(II) under different coordination. Also, the Bader analysis confirms the oxidation state predicted by the d^7 configuration for both the Co sites (see Fig. 2), predicting a total charge of 8.04 valence electrons for $\operatorname{Co}^{tetra}$ with ~ 7.02 electrons in d states, and 8.35 valence electrons for Co^{octa} with ${\sim}7.20$ electrons in d states.

TABLE I. Energy per formula unit and magnetic moment at Co sites of non-magnetic (NM), ferromomagnetic (FM) and antiferromagnetic (AFM) configurations, calculated for U = 5 eV.

$\overline{\mathrm{Conf}}$	Energy (eV)	$\mathrm{Co}^{octa}(\mu_B)$	$\operatorname{Co}^{tetra}(\mu_B)$
NM	-65.98	_	_
\mathbf{FM}	-80.51	1.69	2.65
AFM1	-80.91	1.80	2.61
AFM2	-80.92	1.68	2.65
AFM3	-80.89	1.63	2.58

Figure 4 shows the calculated Density of States (DOS), which reveals the AFM nature of the crystal with a metallic character, as indicated by the occupied states at the Fermi level for both spin up and spin down. The projected DOS shows that, in stoichiometric AFM, Co^{tetra} 3d states are split into the relatively sharp peaks of e_q states (green area in Fig.4b) at -6.5 eV, which then broaden into t_{2q} states (red area in Fig.4b) at ~ -4 eV, with a d - d distance of ~ 2 eV, which is in accordance with experimental value. However, t_{2q} seems to partially remove the degeneracy, due to the local distortion of the lattice at the Co^{tetra} which alters the local T_d symmetry to C_{3v} . The narrow Co^{octa} 3d e_g states are centered below the Fermi energy, at about -1.5 eV, whereas the t_{2g} has a peak at -4.5 eV, with additional peaks due to hybridization via sulfur with the tetrahedral Co 3d states at -6.5 eV. The calculated d - d splitting of ~ 3 eV is consistent with the predicted orbital configuration of Co in octahedral coordination.

Burdett et al. and Chauke at al. state that at low energies, below the Fermi energy, the Co 3d and S 3poccupied states suggest a bonding interaction. At higher energies, S p-states are present, however this range has a predominance of Co 3d states with sharp peaks, which suggests a non-bonding character. Above the Fermi energy, the character of S 3p and Co 3d states suggest an anti-bonding character, which indicates that the Fermi level lies between the non-bonding and anti-bonding states.^{32,33} To analyse the bonding nature of Co-S, we determined the crystal overlap hamiltonian population (COHP) by multiplying the DOS by the corresponding element of the Hamiltonian, which is conventionally considered to have opposite sign, and yields additional information regarding the bonding character: positive and negative values indicate bonding and antibonding interactions, respectively. Our COHP analysis, suggests that there is a bonding-antibonding transition at $\sim -4 \text{ eV}$ for Co^{tetra} with a non-bonding character around the Fermi level. On the other hand, for Co^{octa} the same transition occurs at ~ -2 eV, with non-bonding states only above the Fermi level, indicating an anti-bonding character for Co^{octa} e_q, which is consistent with theoretical considerations. The antibonding states at high energies suggest an electronic instability, that reflects, in the electronic reconfiguration, a vacancy formation that breaks the lat-



FIG. 3. (Color online) Schematic representation of three different AFM configurations in stoichiometric Co_9S_8 . From top to bottom they correspond to AFM1 AFM2 and AFM3 in Tab.I. The blue and red arrows indicate spin-up and spindown. The double arrow at Co^{octa} indicate alternating spinup and spin-down in adjacent cells used in large cell calculations.

tice symmetry.

To test the validity of our choice for the Hubbard term, we also repeated the calculations with different values of U. For a Hubbard correction U=0 eV, the results do not consistently describe a spin configuration with CFT considerations, instead favouring a non magnetic electron configuration. This is because DFT wrongly describes the d orbital energetics, with no d - d splitting, as shown in Fig.5(a), where the overlapping d orbitals cause a net nil magnetic moment. The same effect is obtained for values of U up to 1 eV. When U increases from 1.5 eV to 7 eV a net spin at Co^{tetra} sites is obtained, with local magnetic moment $0.70 \le \mu_B \le 2.70$, favouring an AFM configuration. Since the crystal stoichiometry is close to that of CoS, and with a high density of



FIG. 4. (Color online) a) Total Density of States, b) projected Density of States of the Co^{octa} (blue and yellow) and $\operatorname{Co}^{tetra}$ (red and green), c) Crystal Overlap Hamiltonian Population of the Co^{octa} -S (yellow line) $\operatorname{Co}^{tetra}$ -S (black line) bonds in stoichiometric Co_9S_8 , corresponding to the AFM2 configuration in Tab.I.

Co sites in tetrahedral coordination, we expect from basic consideration to have an electronic configuration that is close to that of tetrahedral Co(II), with a theoretical spin $\mu_B = \sqrt[2]{4S(S+1)} \approx 3.87$, and with a total magnetization $\mu_B = \sqrt[2]{4S(S+1) + L(L+1)} \approx 4.58$. This value measured in similar structures is $\mu_B \sim 4.20$, which confirms that the spin at Co^{tetra} is close to the theoretical one. The presence of Co^{octa} , will generate a deviation from this scenario, which however should be relatively small due to the low density of octahedral sites. We obtain a spin configuration close to the ideal tetrahedral Co(II) with values of U equal or above 5 eV, as shown in Fig.5(b). However, value of U higher than 5 eV will result in a non nil a bang gap for spin up that indicate a half metallic character, which is not in line with experimental observations (see Figs.5(c)).⁶

Assuming the second-nearest model, within mean-field



FIG. 5. (Color online) a) projected Density of States of the Co^{octa} (blue t_{2g} and yellow e_g) and $\operatorname{Co}^{tetra}$ (red t_{2g} and green e_g) calculated using the Hubbard correction U = 0. b) $\operatorname{Co}^{tetra}$ magnetic moment as a function of the Hubbard correction. c) Total Density of States of stoichiometric Co_9S_8 calculated with U=6 eV.

theory, we can calculate the Néel Temperature (T_n) as follows:

$$T_n = \frac{S(S+1)}{3k_B} \sum_{l=1,2} J_l \quad , \tag{1}$$

where S is the total spin, k_B is the Boltzmann's constant, and J_l is the exchange coupling that runs over the nearest- and next-nearest-neighbors. J_1 and J_2 can be extrapolated from energies reported in Tab.I.^{34–36}

We can write each AFM energy as a sum of a contribution to the total energy with respect to the FM con-

TABLE II. Number of nearest-neighbours (n) and nextnearest-neighbours (m) for stoichiometric AFM configurations, in antiferromagnetic coupling with respect to FM.

Conf	n	m
AFM1	2	0
AFM2	2	2
AFM3	1	3

figuration (E_0) , and a term that include the exchange integrals with respect to the n_i nearest-neighbour and the m_i next-nearest-neighbour (Tab.II), as follows:

$$AFM_i = E_0 + S(S+1) \left[-n_i J_1 - m_i J_2 \right] \quad . \tag{2}$$

Our calculations give values of $J_1=35$ meV and $J_2=5$ meV, and predict $T_n=116$ K. However, the estimated T_n value strongly depends on the value of the Coulomb parameter.³⁷

B. Geometry and Electronic Structure of Defective $$\mathrm{Co_9S_8}$$

Two non equivalent sulfur vacancies can form in the super-cell, V_{S1} and V_{S2} , due to fourfold and fivefold coordinated sites, respectively, where S1 forms bonds with Co^{octa} and Co^{tetra} , whereas S2 forms bonds only with Co^{tetra} (see Fig.1). We calculated the vacancy formation energy to be 6.69 eV for V_{S1} and 6.64 eV for V_{S2} , which indicates that, below T_n and in thermodynamic conditions, the vacancy density is extremely low. However, vacancy density may also be affected by the specific synthesis process, and could therefore be high enough to influence the crystal properties. Upon V_{S1} formation, the broken symmetry leaves Co^{octa} in a square pyramidal configuration, removing the e_g degeneration and splitting the t_{2g} into two levels. Yet, due to the d^7 electron configuration, no significant change occurs in the magnetic moment of Co^{octa} . The four Co^{tetra} atoms neighbouring V_{S1} , are arranged in a square planar geometry, with a bond length Co^{tetra}-S of 2.40 Å. Our calculations point to a change in the local magnetic order, with a favourable FM configuration, as shown in Fig. 6 and reported in Tab.III.

Our pDOS analysis results indicate the magnetic character of the Co cluster (see Fig.7). Co^{tetra} d peaks with a shift in energy for spin up and down of 1 eV and 2 eV, respectively. Our COHP analysis results suggest the formation of Co-Co bonding states, that together with occupation at the Fermi level, confirm the formation of a Co cluster with FM character.

On the other hand, upon V_{S2} formation, Co^{tetra} -S bond lengths at the vacancy site are 2.39 Å and 2.43 Å, which breaks the local T_d symmetry of the crystal. The local magnetic moment, shown in Fig.6 and reported in

TABLE III. Energy per formula unit and magnetic moment at Co sites for ferromomagnetic (FM) and antiferromagnetic (AFM) configurations upon vacancy formation, calculated for U = 5 eV.

Conf	Energy (eV)	$\mathrm{Co}^{octa}(\mu_{\mathrm{B}})$	$\mathrm{Co}^{tetra}(\mu_{\mathrm{B}})$
VS1 FM1	-73.21	1.65	2.65
VS1 AFM1	-73.06	0.97	1.90/2.63
VS1 AFM2	-73.05	1.04	1.96/2.60
VS2 FM2	-73.30	0.90	1.90/2.65
VS2 AFM1	-73.20	0.91	1.92/2.61
VS2 AFM2	-72.26	1.10	1.80/2.60



FIG. 6. (Color online) Schematic representation of local FM configurations upon the formation of a sulfur vacancy (V_{S1} and V_{S2}), which correspond to FM1 (top) and FM2 (bottom) of Tab.III. Bond distances and magnetic moments at each site are indicated. Blue and yellow spheres represent cobalt and sulfur atoms, respectively.

Tab.III, indicates the crystal's local ferromagnetic character, with magnetic moments of 1.90 and 2.65 μ_B , which suggests a charge transfer, and which is confirmed by the Co^{octa} magnetic moment change to $0.90\mu_B$. Our pDOS analysis results confirm the FM order of the Co cluster, with a Co^{tetra} and Co^{octa} d peaks distance of ~3 eV for both spin-up and spin-down (see Fig.8). However, the COHP analysis results suggest the formation of Co-Co bonding and anti-bonding states in the range -3 eV to 0 eV. The antibonding states close to Fermi level, indicates an internal stress in the lattice, which is in accordance with the calculated distorted local geometry. Also, the magnetic moment of the stable V_{S2} configuration FM2, showing that Co^{octa} loses a fraction of electron in favour of Co^{tetra}, confirmed by the Bader



FIG. 7. (Color online) a) Total Density of States , b) projected Density of States of the Co^{tetra} (red and green), c) Crystal Overlap Hamiltonian Population of the Co^{tetra} - Co^{tetra} bond in non stoichiometric Co_9S_8 , corresponding to the FM1 configuration in Tab.III.



FIG. 8. (Color online) a) Total Density of States , b) projected Density of States of the Co^{tetra} (red and green), c) Crystal Overlap Hamiltonian Population of the Co^{tetra} -Co^{tetra} bond in non stoichiometric Co_9S_8 , corresponding to the FM2 configuration in Tab.III.

IV. CONCLUSIONS

In this paper we analysed the geometry and electronic structure of stoichiometric and reduced Co_9S_8 pentlandite. We compared the results using DFT and DFT+U, and show that DFT incorrectly describe the d-d orbital splitting, which is an essential factor in the correct prediction of the magnetic order of Co_9S_8 . We calculated a favourable AFM order with a metallic character for the stoichiometric form with a gain of ~0.4 eV as compared to the FM configuration, we estimate exchange parameters and predict the Neél temperature to be 116 K. However, in non-stoichiometric Co_9S_8 , we predicted the formation of Co FM clusters, which may explain the contradictory experimental results reported in the literature.

analysis that shows an electron transfer of 0.6 electrons, with the orbitals alignment consistent with theoretical considerations. The electron transfer results in a lower magnetic moment for both species, since e_g occupation in Co^{octa} decreases and the half full t_{2g} states in Co^{tetra} increases, with a resulting reduction of the total spin for both configurations. The results regarding the magnetic order of non-stoichiometric Co_9S_8 show how this crystal could in principle have either AFM or ferrimagnetic (FiM) character, depending on the specific stoichiometry and density of sulfur vacancies. However, although we calculated a very low vacancy concentration in thermodynamic conditions, the synthesis technique may significantly affect the stoichiometry, which may explain the different measurements reported in the literature.

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