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Application of Buoyancy-Power Generator for Compressed Air Energy Storage Using a Fluid-Air Displacement System

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Abstract

This study proposes a gravity power generator based on the fluid-air displacement system using Compressed Air Energy Storage from renewable energy sources to increase the solar and wind power system penetration in the power network. A computer model was applied to estimate the performance of the fluid-air displacement system, taking into account the effects of key design and operating parameters. Analysis of the system was performed to calculate the net energy generation as the difference between the energy input and the energy output. Simulation results indicated that the round-trip efficiency of the fluid-air displacement system was between 47% and 60%, assuming 80% compressor efficiency. Results also showed that a system generating the maximum energy density should have a speed of cylinders movement of 0.65 m/s, a cylinder-wall distance of $0.25 \times$ diameter of the cylinder and a gap distance between centers of two tandem cylinders is equal to 1.25. Furthermore, a sensitivity analysis conducted on the main parameters of the system identified that the gap ratio and the buckets moving speed were the highly sensitive parameters to the design and operation of the proposed system. This study also demonstrates the feasibility of using the fluid-displacement system in energy storage from renewable energy technologies.

Key Words: energy storage system, renewable energy, fluid-air displacement system, compressed air energy storage, gravity energy system

| Nomenclatures | | Unit |
|---------------|---|--------------------------------|
| F_f | total drag force | N |
| C_d | drag coefficient | -- |
| U_o | reference velocity (cylinder moving speed) | m/s |
| A | reference area | m ² |
| D | diameter of cylinder | m |
| B | length of cylinder | m |
| G | gap distance between the cylinder and wall | m |
| L | center-to-center spacing of two tandem cylinders | m |
| Q_a | normal demand of air discharge | m ³ /s |
| u_i | total velocity | m/s |
| \bar{u}_i | mean velocity | m/s |
| \acute{u}_i | fluctuating velocity | m/s |
| μ_t | turbulent viscosity | kg/m.s |
| δ_{ij} | Kroenecker delta function | -- |
| k | turbulent kinetic energy | m ² /s ² |
| ρ | fluid density | kg/m ³ |
| P_1 | absolute initial atmospheric pressure | Pa |
| P_2 | absolute final pressure after compression | Pa |
| P_s | the highest maximum pressure required in compressor | Pa |
| γ_f | fluid unit weight | N/m ³ |
| H | the height of the fluid column | m |
| P_w | required compressor power | W |
| V | volume flow of compressed air at atmospheric pressure | m ³ |
| γ | ratio of specific heats | -- |
| N | number of compression stages | -- |
| η_c | overall compressor efficiency | -- |
| $S_{i,j}$ | Sensitivity coefficients | -- |
| $y_i(p)$ | model output | -- |
| RTE | round trip efficiency | -- |

1. Introduction

Energy storage has many benefits in a power network, it is an important component in the energy management system and facilitates to reduce energy wastage and increase the energy utilization efficiency of process systems. Storage of secondary energy forms such as heat and electricity helps to reduce the number of primary energy forms (fossil fuels) consumed to generate them. This in turn not only decreases CO₂ and other greenhouse gas emissions together with the associated global warming but also assists to conserve fossil fuels, which are believed to be exhaustible [1]. It can also play a crucial role in increasing the penetration of renewable, clean and intermittent energy resources such as wind energy, solar energy, and marine tidal current to the grid as well as help in load shifting [2]. Energy storage improves power system planning, operation and frequency regulation. It facilitates to maintain the energy system stability, improve power quality in micro-

1 grid systems as well as match demand with supply [3]. Therefore, there is a need for efficient
2 engineering processes to recover the stored energy and convert into useful work.

3 Several energy storage technologies have been developed, which are classified into four main
4 groups, including mechanical, electrical, thermal and chemical energy storage. Compressed air
5 energy storage (CAES) and pumped-hydro energy storage are two options of the mechanical
6 energy storage which are the most popular form of energy storage in the worldwide [4-5]. The
7 CAES system operates on a similar principle to pumped hydro, only using air instead of water [5].
8 Energy savings in the compressed air systems are possible in production and treatment of
9 compressed air, compressed air networks, end-use devices, overall system design and operation.
10 Initially, energy is stored in the form of high-pressure compressed air that will be recovered when
11 the compressed air is released to generate energy. In principles, CAES system has the ability to
12 provide significant energy storage at relatively low costs, fast start-up, and low environmental
13 pollution. Compressed air systems consist of the following key components: intake air filters, inter-
14 stage coolers, after-coolers, air-dryers, moisture drain traps, receivers, piping network, filters,
15 regulators and lubricators and pneumatic tools and equipment [6]. During the periods of low power
16 demand, the surplus electricity drives a reversible motor/generator unit to run a chain of
17 compressors for injecting air into a storage vessel, which is either an underground cavern or over
18 ground tanks [7]. The underground CAES system requires 10 to 30 MPa to store the compressed
19 gas. Deformation of the rock mass should be insignificant to maintain the integrity of the lining
20 and if the rock is not adequately stiff buckling of steel lining becomes more serious. Furthermore,
21 underground CAES storage system can be designed for large storage capacities and long period
22 discharge times.

23 He et al. [8] suggested CAES-wind turbine hybrid system in order to reduce the fluctuation in
24 power output. The study presented 2 MW wind turbine coupled with a small-scale CAES system
25 using a dynamic modeling approach. With CAES system, fluctuation in power output was reduced
26 by 38% and hence extending the stable operation period to 3 hours. A hybrid energy storage system
27 composed of adiabatic CAES and flywheel energy storage system (FESS) was proposed to
28 mitigate fluctuation in the power output of wind turbine [9]. The adiabatic CAES and FESS are
29 able to cope with low and high frequencies in wind power fluctuations, respectively. The study
30 revealed that the wind power with fluctuation between 0 and 49.2 MW was stabilized to a steady
31 power output of 24.18 MW and the loss of wind power was 6.6% only. In a separate study,
32 Ramadan et al.[10] evaluated the economic feasibility of adding a CAES system to a renewable
33 energy plant. A computer model was developed and simulation results showed that the addition of
34 a CAES system would increase the profitability of the wind energy systems but neither technical
35 evaluation nor process optimization of the CAES system was performed.

36 Combining CAES and buoyancy energy storage have been addressed in the previous literature.
37 Alami [11] evaluated the CAES system and buoyancy work energy storage (BWES) for off-shore
38 wind power storage. The study identified the main design challenges in the large-scale system to

1 be the heat generated due to air compression and the large friction drag affecting the buoys.
2 Unfortunately, the study did not investigate the development and optimization of a buoyancy
3 system to reduce the effect of drag force. Bassett et al. [12] investigated the integration of 1 MWh
4 buoyancy energy storage system with a utility-scale wind turbine. The study calculated the
5 efficiency of a round trip based on drag losses to calculate the efficiency of the buoyancy storage
6 system but did not perform the system design optimization. An underwater buoyancy battery
7 energy storage (BBES) utilizes a simple pulley, reel and float mechanism in energy storage for an
8 indefinite period of time. Maintenance and operation of such an underwater system, however, is
9 rather problematic and would increase the overall cost of the energy generation. A study by Alami
10 [13] proposed a method of energy storage using the work of buoyancy force. The study found that
11 the efficiency of the experimental work exceeded the theoretical estimation due to the material
12 properties of the buoys. There are several advantages offered by the buoyancy storage system such
13 as a compact design, high energy density retrieval, and high efficiencies. Another example of a
14 basic principle of buoyant energy is floating hydraulic energy storage, which is quite similar to
15 that of pumped hydropower storage plants [14].

16 Research into the uses of buoyancy force for storing energy is still under development. Recently,
17 a buoyancy-powered generator (BPG) has been experimentally applied to the usage of the
18 compressed air energy for electricity production [15]. The basic concept of this method is
19 associated with a plurality of submerged cylinders in a tank filled by a fluid such as water that the
20 cylinders are installed on a rotational sprocket wheel. The cylinders on the vertically upwardly
21 moving side are filled by an air injector and the cylinders on the vertically downwardly moving
22 side are filled by the ambient fluid and different in the cylinder's buoyancy force causes the system
23 to work [16]. One of the most important issues in a buoyancy force system is the accurate
24 prediction of energy losses and drag forces, which is usually done using numerical models. The
25 family of Reynolds-Averaged Navier-Stokes (RANS) models is the most widely used turbulence
26 modeling approach [20].

27 Yet, there are limited studies on the BPG system for power generation to reduce the load on the
28 national grids during peak hours. In this study, the BPG system was evaluated for power generation
29 to increase the penetration level of wind and solar power in the supply network. We assumed that
30 CAES is available to provide compressed air for the operation of the BPG system. BPG system
31 has several advantages such as the capability of scaling-up, constructed from components that can
32 be easily recycled at end-of-life, easy to operate and maintain.

33 Although battery storage is widely proposed for energy storage from renewable resources, this
34 method causes a major source of environmental pollution. New environmental-friendly
35 technologies such as air-displacement system could replace chemical-based processes to achieve
36 this goal. The system uses buoyancy force for power generation instead of chemical reactions in
37 battery storage technology. The other advantage of the air-displacement system is that it can be
38 constructed from recyclable materials that reduce the environmental pollution when disposed of.

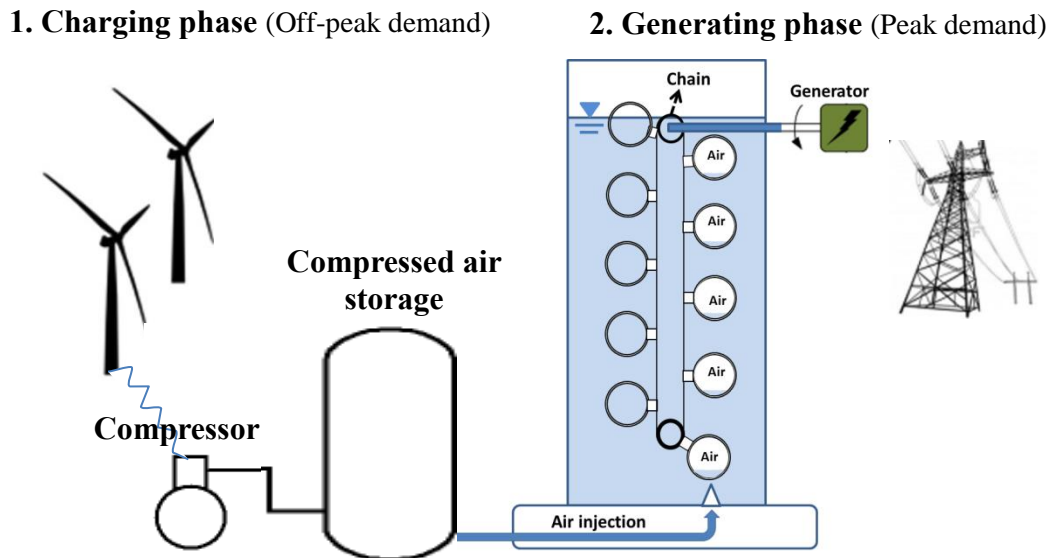
1 Finally, air-displacement is a modular system, which can be coupled with small and large energy
2 storage systems.

3 This study evaluates a fluid-air system for regenerating of energy stored from renewable resources
4 by an air compressed system. The system is modular and easy to couple with a compressed air
5 technology. Several designs and operating parameters such as system physical dimensions and
6 hydrodynamic properties were investigated in this study and their impact on the system
7 performance is highlighted. The main advantages of the buoyancy-power generator are that
8 minimal water is required in comparison with pumped hydro storage and has insignificant
9 environmental impacts in comparison with batteries and thermal energy storage methods. Water
10 was suggested as the working solution in this study because it is a standard solution and its low
11 dynamic viscosity (0.001 Ns/m^2) that reduces the friction force around the moving buckets.

12 2. Theory and Methods

13 2.1. Conceptual CAES/BPG hybrid system

14 This study evaluates the buoyancy-powered generator (BPG) with a combination of compressed
15 air energy storage (CASE), briefly called CAES/BPG, like a new electrical energy storage (EES)
16 strategy, in order to increase the penetration level of renewable energy in a power network. The
17 CAES/BPG system includes two main parts, the vessels that function as the buoyancy-powered
18 generator and an air pump/compressor, which converts electricity generated from wind or solar
19 power at an off-peak time to a compressed air for using to operate the buoyancy-powered generator
20 at peak time, as depicted in Fig.1.



21

22

Fig. 1. Basic principle of using CAES/BPG algorithm for power storage

1 **2.2. Buoyancy-Power Generator Definition**

2 The present study concentrates on using buoyant energy based on the fluid-air displacement
3 concept as a Buoyancy-Powered Generator (BPG). The overall concept of the generator in its most
4 simple form where lightweight rigid buckets are used to capture the rising air from the air pump
5 as shown in Fig.2. The BPG system can be constructed with two horizontal shafts, two upper
6 sprocket wheels, two lower sprocket wheels and two chain loops submerged in the water which
7 each shaft has one sprocket wheel mounted on it which all components are placed in a water tank.
8 Each of these sprocket wheels engages with a continuous chain loop, which also engages with the
9 sprocket wheel that is positioned vertically above it. These vertical chain loops form belt-style
10 support for a series of identical buckets. On one side, of the vertical belt, the buckets have their
11 open face upwards and on the other side the bucket openings are facing downwards. An air pump
12 is positioned directly underneath the set of buckets, which have the bucket openings facing
13 downwards. The air pump generates an upward-moving stream of air, which collects in the rising
14 buckets, displacing the water filling the bucket. Each bucket with a substantial amount of air in it
15 will create a very significant upward force due to buoyancy, the air being about one thousand times
16 lighter than water. This results in a powerful upward thrust caused by the buoyancy of that bucket,
17 and the thrust causes the bucket to move upwards, rotating both horizontal shafts and bringing
18 another water-filled bucket into position above the air pump. An alternative to air pumps is to use
19 tanks of compressed, non-polluting gas, possibly air. The surface of the liquid, is indicated to
20 illustrate the fact that a bucket, which is in the process of turning over at the top of its orbital
21 motion, is positioned so that one edge of the bucket is above the surface of the water, which allows
22 the air which was trapped inside the bucket to escape into the atmosphere and the water fill the
23 entire bucket causing only a very minor turbulence when doing so. Accordingly, in this system, in
24 the process of the buckets turning over at the top of its orbital motion, when a bucket at the right
25 side of the tank is positioned at the above of the surface of the water the air trapped will escape
26 into the atmosphere and the water will fill the entire bucket at the left of the tank. At this time the
27 bucket positioned at the bottom level will face to the air injection from downward and the air will
28 fill the entire bucket at the right of the tank. Because the bucket movement through the water is
29 relatively slow, a gearing system transfers the rotation torque created to a generator that produces
30 electricity for general purpose uses. Movement of buckets through the water is offset by gearing
31 between the output drive shaft and the generator's input shaft. Therefore, the speed of the buckets
32 can be regulated by the gearing system and the flow rate produced by the air compressor/pump
33 can be used. The power output of the system can be increased by adding more buckets in the
34 vertical chain and increasing the depth of water. Other methods to increase the power output
35 include increasing the volume inside each bucket and/or increasing the flow rate produced by the
36 air pump or used pumps. In this system, different bucket shapes could be used, including flexible
37 membrane types or alternatively, hinged-plate, which have reduced resistance to moving through

1 the water in the collapsed state in the downward movement. The weight of the buckets is equal on
2 each side of the chain using lightweight buckets to reduce the inertial mass of the moving parts.
3 Several parameters affects the efficiency of the system, such as rotating speed of the chain, the
4 buckets moving speed, size and shape of the buckets, the number of buckets, drag and friction
5 force due to movement of buckets and chain to water body of the tank, discharge of air venting to
6 fill the buckets, the gap ratio and the spacing ratio. These parameters should be taken into account
7 in the design and operation of the system coupling air pump/compressor with the buoyancy-
8 powered generator composes an energy storage system for wind and solar power. In this study, the
9 analysis of a BPG system has been carried out using various assumptions and simplifications,
10 including:

- 11
- 12 a) Friction in the sprocket wheel and chain are assumed to be negligible;
 - 13 b) Drag and friction force due to movement of buckets to water body of the tank can be
14 determined using numerical modeling;
 - 15 c) The shape of the bucket is a circular cylinder with a diameter (D) of, 0.2 m and a length
16 (B) of 1 m.

17

18 In this research, a gap ratio, $G^*=G/D$, between 0.125 and 1 and spacing ratio, $L^*=L/D$, between
19 1.25 and 2 are used in the design of the BPG system, where G is the gap distance between the
20 cylinder and wall and L is the center-to-center spacing of two tandem cylinders.

21

22 Furthermore, the buckets moving speed, U_o , is between 0.1 and 1.3 m/s. The efficiency of the
23 gearbox may vary in a wide range, depending on the type of gear set [17]. Some types of gear
24 technology such as bevel gears are designed to operate at 98% efficiency (used on right-angle
25 drives). Spur and helical gears have 97%-99.5% efficiency while face gears and beveloids
26 efficiency is about 95%. In this study, the efficiency of the gearbox is assumed 90 %. The Reynolds
27 numbers based on the cylinder diameter change from 2×10^4 to 2.6×10^5 , which is completely
28 classified in turbulent flow regime.

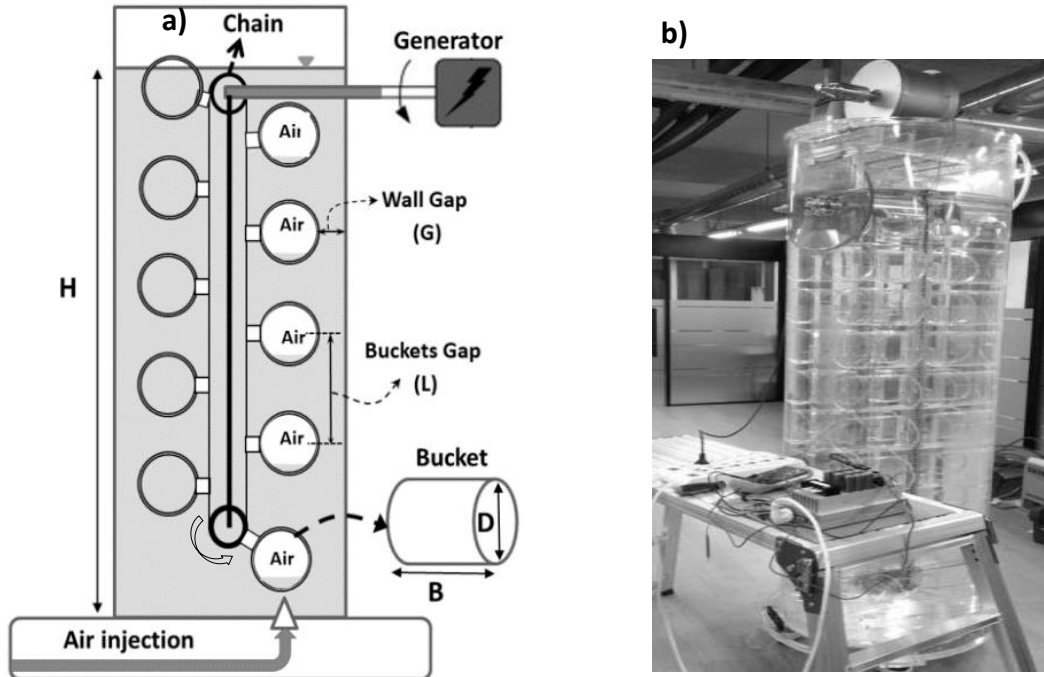


Fig.2.a) Schematic diagram of the buoyancy-power generator tank and b) a photograph of experimental setup by INFINITY SAV TEAM (after [15])

2.3. Numerical Flow Modeling

In the BPG system, moving buckets through the tank fluid body causes flow resistance, which should be determined and considered in the planning and design of the system. This resistance refers to the skin friction drag and pressure drag. The first is drag caused by the friction of a fluid against the surface of an object that is moving through it and it is directly proportional to the area of the surface that in contact with the fluid and increases with the square of the velocity. The second is the drag caused by the separation of the boundary layer from a surface and the wake created by that separation, which is primarily dependent upon the shape of the object. The total drag force is obtained by [18]:

$$F_f = 0.5 C_d \rho A U_o^2 \quad (1)$$

where F_f is the total drag force acting on the object, C_d is drag coefficient, U_o is a reference velocity and A is a reference area which for a cylinder with diameter D and length B , oriented with its axis perpendicular to the direction of flow, the reference area would be $A = D \times B$. The total drag force contains both viscous drag (arising from shear stresses exerted by the fluid on the object) and form drag (arising from normal stresses exerted by the fluid on the object).

1 In recent years, numerical solving the Navier-Stokes equations of the turbulent flow has been
 2 widely used in computational fluid dynamics (CFD) applications [19]. That is because of much
 3 expensive of physical modeling and the fast, flexibility and good accuracy of CFD models for
 4 complex geometries. The family of Reynolds-Averaged Navier-Stokes (RANS) models is the most
 5 widely used turbulence modeling approach and offers the most economic approach for computing
 6 complex turbulent industrial flows [20]. In this approach, the Navier Stokes equations are split into
 7 mean and fluctuating components. The total velocity u_i is a function of the mean velocity \bar{u}_i and
 8 the fluctuating velocity \acute{u}_i as shown in the equation below [21].

9

$$10 \quad u_i = \bar{u}_i + \acute{u}_i \quad (2)$$

11

12 The continuity and momentum equations incorporating these instantaneous flow variables are
 13 given by:

14

$$15 \quad \frac{\partial \rho}{\partial t} + \frac{\partial \rho}{\partial x_i} (\rho u_i) = 0 \quad (3)$$

$$16 \quad \frac{\partial}{\partial t} (\rho u_i) + \frac{\partial \rho}{\partial x_i} (\rho u_i u_j) = \frac{\partial \rho}{\partial x_i} + \frac{\partial}{\partial x_j} \left[\mu \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} - \frac{2}{3} \delta_{ij} \frac{\partial u_k}{\partial x_k} \right) \right] + \frac{\partial}{\partial x_i} (-\rho \overline{\acute{u}_i \acute{u}_j}) \quad (4)$$

17

18 These above equations (in Cartesian tensor form) are known as RANS equations, and the
 19 additional Reynolds stress terms $-\rho \overline{\acute{u}_i \acute{u}_j}$ need to be modeled. The Boussinesq hypothesis is
 20 applied to relate the Reynolds stress and the mean velocity:

$$21 \quad -\rho \overline{\acute{u}_i \acute{u}_j} = \mu_t \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) - \frac{2}{3} \left(\rho k + \mu_t \frac{\partial u_k}{\partial x_k} \right) \delta_{ij} \quad (5)$$

22 Where k is the turbulent kinetic energy (TKE), ρ is fluid density, μ_t is turbulent viscosity, and
 23 δ_{ij} is Kroenecker delta function.

24 The accuracy of solving RANS equations depends on the turbulence model to determine the
 25 Reynolds stress terms. The $k-\epsilon$ and $k-\omega$ are two such turbulent models, which provide a good
 26 compromise between performance and accuracy [22]. The shear-stress transport (SST) $K-\omega$ model
 27 was developed by Menter, 1994 [23] to effectively blend the robust and accurate formulation of
 28 the $K-\omega$ model in the near-wall region with the free-stream independence of the $k-\epsilon$ model in the
 29 far-field. The $K-\omega$ SST model is more accurate and reliable than the standard $k-\epsilon$ model for a wider
 30 class of flows such as adverse pressure gradient flows, airfoils, transonic shock waves [23].

1 ANSYS Fluent software solves the RANs equations based on the finite volume method [24]. This
2 software is also capable to solve the Reynolds stress terms using a wide range of turbulent models,
3 such as $k-\varepsilon$ Standard, $k-\varepsilon$ RNG, $k-\omega$ SST, $k-\omega$ Standard, Transition SST and Spalart-Allmaras
4 which are applied in this study as the common models [25, 21]. Since none of the turbulent models
5 is universal, a series of tests were performed to check which model is the most effective to capture
6 the flow behavior. The results for the case of $G^*=0.5$ and $U_o=1.1$ m/s, as illustrated in Fig.3, show
7 that difference among the drag coefficients, obtained from different turbulent models, are not
8 significant at 95% confidence interval. For selecting the appropriate turbulent model, convergence
9 criterion was used and variation of the residual values versus the number of iteration for effective
10 parameters such as continuity, Y -velocity, ω , ε and K was plotted in Figs. 4.a to 4.d. These figures
11 show that the $k-\omega$ SST turbulence model is the most appropriate model according to the amount
12 of the residual of continuity, Y -velocity, ω , ε and K parameters. It is in a good agreement with Patel
13 [25], Young and Ooi [26], Coughtrie et al. [27], Ducrocq et al. [28], Rahimzadeh et al.[29] and
14 Dogan et al. [30] that demonstrated $k-\omega$ SST model can accurately and reliably predict the drag
15 coefficient in a wide class of flows around cylinders. A Numerical study of flow past a circular
16 cylinder using different turbulence formulations showed that the $k-\omega$ SST model predicts similar
17 vortex shedding phenomenon to that for LES model [31]. Therefore, the $k-\omega$ SST turbulence model
18 was applied to calculate the drag force for all cases of the BGP vessel arrangements. A skewness
19 mesh less than 0.5 was considered in this study and different mesh sizes, from coarse to dense,
20 were generated to ensure that the simulation results were sufficiently grid-independent. As shown
21 in Fig.5, the drag coefficient, CD , became stable and remained nearly unchanged when the number
22 of mesh elements was higher than 20 nodes per cm^2 . Considering the computational efficiency, a
23 quadrilateral mesh size between 3×10^{-5} m and 3×10^{-3} m, which resulted in minimum nodes number
24 of 20 nodes per cm^2 , was used for further simulation. Furthermore, the input parameters such as
25 pressure, density and viscosity were considered at sea level conditions. The input velocity at the
26 inlet was set for the scenarios studied from 0.1 m/s to 1.3 m/s, which results in Reynolds number
27 from 2×10^4 to 2.6×10^5 . The top and bottom walls of the rectangular tank domain were assigned as
28 the inlet and the outlet and also the left and right sides of the tank are defined as moving walls
29 parallel to the inlet velocity direction with the same velocity. The turbulence intensity was set at
30 5%, according to the low-intensity range reported in reference [18]. In order to avoid calculation
31 errors, double precision was set and in order to maintain accuracy second-order discretization was
32 set for pressure, momentum and viscous terms and the convergence criterion was set at 1×10^{-5} .
33 Fig. 6 shows velocity contours pattern and boundary condition definition in case of $G^*=0.25$,
34 $L^*=1.25$ and $U_o=0.5$ m/s using $k-\omega$ SST model.

35

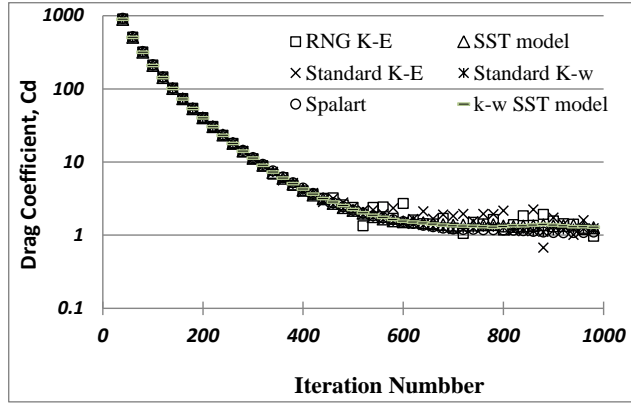


Fig.3 Drag Coefficient variation versus iteration number in case of $G^*=0.5$, $L^*=1.25$ and $U_o=1.1$ m/s

1

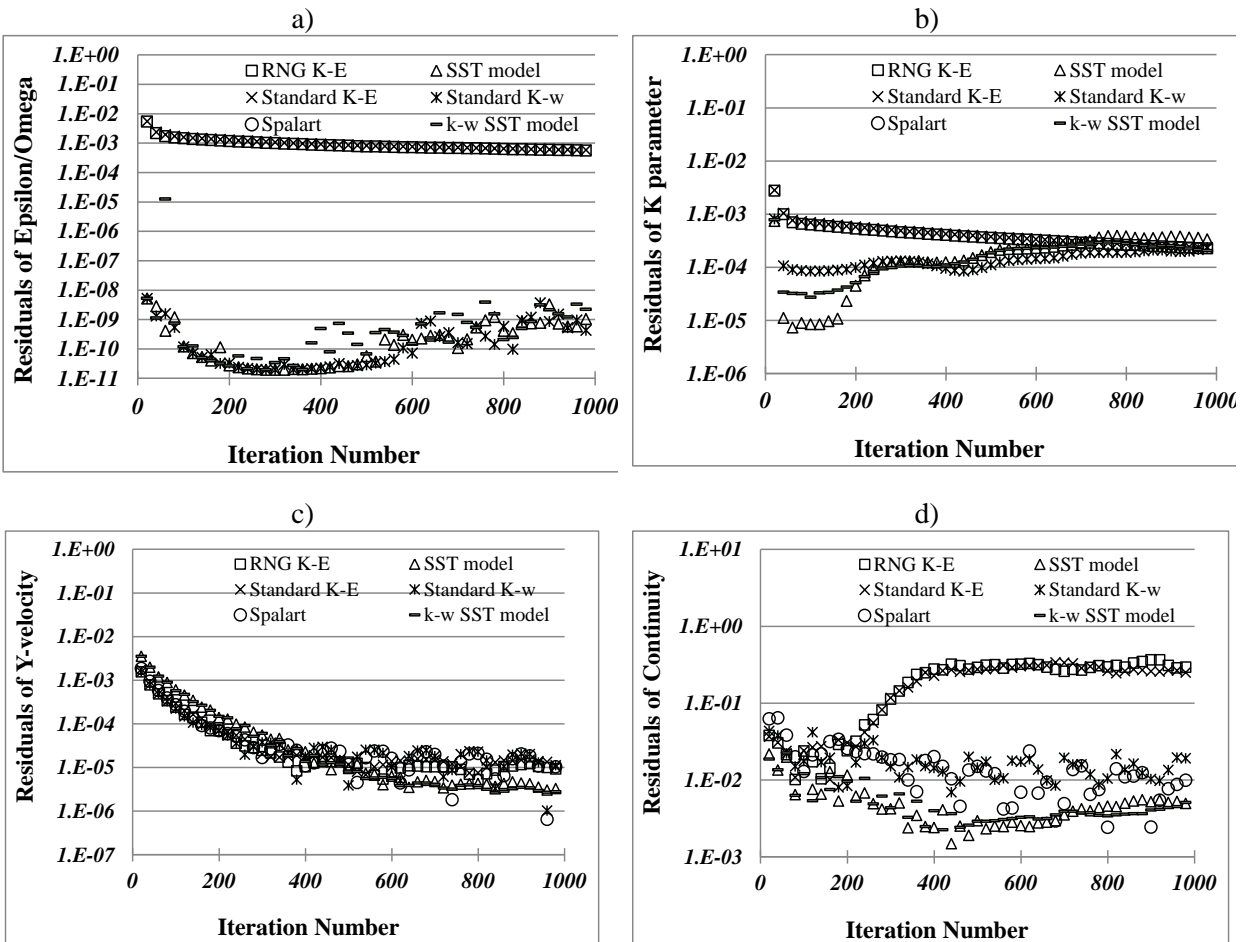


Fig.4 Residual variations versus iteration number in case of $G^*=0.5$, $L^*=1.25$ and $U_o=1.1$ m/s; a) ϵ or ω parameter, b) K parameter, c) Y -velocity, d) Continuity parameter

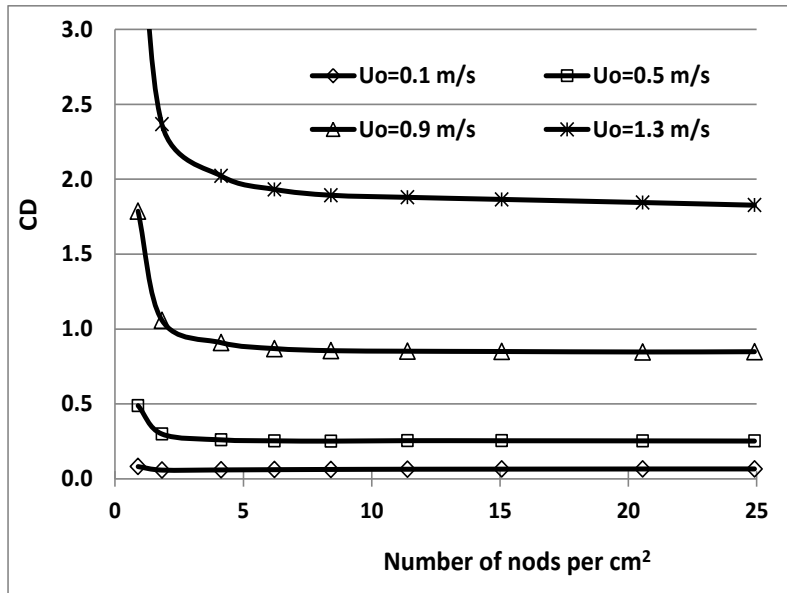


Fig. 5 Validation of mesh independency, drag coefficient vs nodes number per domain area for different buckets moving speed

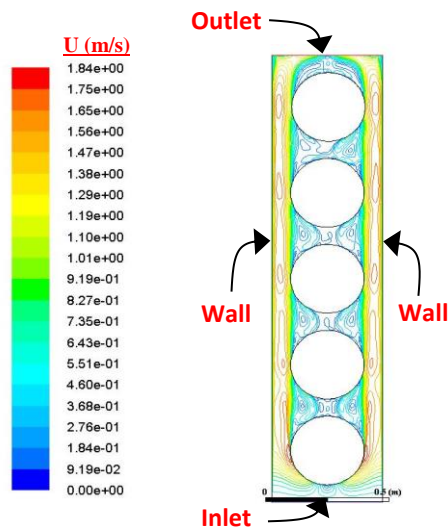


Fig. 6. Velocity contours and boundary condition definition in case of $G^*=0.25$, $L^*=1.25$ and $U_o=0.5$ m/s.

2.4. Air Compressor Considerations

There are different types of air compressors, but reciprocating compressors as positive displacement compressors, are the most widely used type for air compression. This type of compressor is characterized by a flow output that remains nearly constant over a range of discharge pressures. Reciprocating compressors are used in the capacity range of 0.014 to 2.78 m³/s, with discharge pressure up to 700 bars [32].

In order to estimate the capacity of the compressor, the normal demand of air discharge should be determined. The normal demand for air discharge (Q_a , in m³/s, at 0°C and 1 bar), based on the mass conservation law, is calculated using the following relationship in the SI system of units:

10

$$Q_a = \frac{V_a}{t}, \quad V_a = B \cdot \frac{\pi D^2}{4}, \quad t = \frac{L}{U_o} \quad (6)$$

12

where V_a is the volume of air for filling a bucket, t is time duration for filling the bucket by air, D is the cylindrical bucket diameter, B is the cylindrical bucket length, L is the gap distance between two tandem cylindrical buckets centerline and U_o is the cylindrical buckets moving speed.

In this study, the amount of Q_a varies from a minimum value of 0.01256 m³/s (in case of $G^* = 0.25$ and $U_o = 0.1$ m/s), up to a maximum value of 0.0816 m³/s (in case of $G^* = 1.5$ and $U_o = 1.3$ m/s).

The air compressor outlet pressure is another parameter used for assessing the compressor capacity. Minimum pressure outlet of the compressor should not be less than a hydrostatic pressure at the bottom of the buoyancy-power generator tank, where a nozzle delivers air to fill the cylindrical buckets. Moreover, the compressor design pressure should be the minimum pressure plus the required pressure to storage secondary energy receiving from wind or/and solar power and it depends on secondary power capacity, time of off-peak energy when the compressor consumes energy and volume of compressors storage vessel according to the following equation:

26

$$P_2 = P_s + \gamma_f \cdot H \quad (7)$$

28

Where, P_2 is the absolute final pressure after compression, which is the highest maximum pressure required in the compressor, P_s is the required absolute pressure in compressors storage vessel for storing secondary energy, γ_f is the fluid unit weight and H is the height of the fluid column in the buoyancy-power generator tank.

32

1 Finally, compressor power required to compress of free air (atmospheric pressure) to final pressure
 2 for an adiabatic condition (process without transfer of heat) can be expressed as following [18].

3

$$4 \quad P_w = \frac{N.V.\gamma.P_1}{(\gamma-1).\eta_c} \left[\left(\frac{P_2}{P_1} \right)^{\left(\frac{K-1}{N.K} \right)} - 1 \right] \quad (8)$$

5

6 where P_w is the required compressor power (watts); V is the volume flow of compressed air at
 7 atmospheric pressure (m^3/s); P_1 is the absolute initial atmospheric pressure (101325 Pa at sea
 8 level); P_2 is the absolute final pressure after compression (Pa) as formulized in equation 7; γ is the
 9 ratio of specific heats (1.4 for air at 20 °C); N is number of compression stages and η_c is overall
 10 compressor efficiency includes motor and blower efficiencies.

11 Compressor efficiencies vary with compressor type, size, and throughput. They can only be exactly
 12 determined by a compressor test, although compressor manufacturers can usually provide good
 13 estimates [33]. For planning purposes, Campbell [34] suggests the values for the overall
 14 efficiencies of compressor include gas friction within the compressor, the mechanical losses
 15 (bearings, seals, gear-box, etc.), and gear-box losses as in Table 1 [35]. Adding 3-4 % efficiency
 16 (mechanical losses) to the overall efficiencies in Table 1, will generally give a good estimate of
 17 the thermodynamic efficiency. It should be also noted that if the compressor system to be made
 18 and operated under poor management, leaks may waste up to 50% of the compressed air produced
 19 by the compressor. In this work according to table 1, an efficiency of 80% for a compressor can
 20 be assumed.

21

22

Table 1. Overall compressor efficiencies [35]

| Row | Compressor Type | Efficiency, η |
|-----|--------------------------|--------------------|
| 1 | Centrifugal | 0.70 – 0.85 |
| 2 | High Speed Reciprocating | 0.72 – 0.85 |
| 3 | Low Speed Reciprocating | 0.75 – 0.90 |
| 4 | Rotary Screw | 0.65– 0.75 |

23

24 **3. Results and Discussion**

25 **3.1. Evaluation of the Buoyancy-Power Generation**

1 The buoyancy power generation in the CAES/BPG system is defined as net buoyancy force acting
 2 on bucket movement multiple by the buckets moving speed. The net buoyancy force depends on
 3 the air-filled buckets submerged buoyancy force and the system losses which include the drag
 4 force effect, compressor losses, gearbox friction and wasting air from the buckets.

5 The total drag force is determined based on the numerical modeling results, as described in the
 6 previous section. Fig.7 shows the variation of drag force versus the buckets moving speed for
 7 different G^* and L^* . Results show that the total drag force is increased with decreased G^* and
 8 Fig.7.b shows that inverse relationship with L^* (Fig.7.a). That is because of the gap distance effects
 9 on the pressure distribution at the tandem cylinders, flow pattern and turbulence generation. Also,
 10 the results show that the total drag force in $G^*=0.125$ is significantly much higher than that of
 11 $G^*\geq 0.25$, because of the wall effects and blockage of the flow around the cylinders. For $G^*>0.5$
 12 there is not observed a significant difference in the amount of drag force. Experimental study of
 13 flow around two tandem circular cylinders conducted by Wang et al. [19] showed that when G^*
 14 increases to 0.6, the wall effects exist at a small degree and become almost negligible, such that
 15 the flow is similar to a free-standing case, at $G^*=1.4$. This result is in agreement with the present
 16 work findings.

17 Other losses due to compressor and gearbox can be estimated based on their efficiencies. By
 18 assuming the typical technologies an efficiency of 80% for the compressor and an efficiency of
 19 90% for the gearbox are considered. Besides, in order to consider the effects of wasting air from
 20 the buckets, it is assumed that 10% of air injection into the tank is not trapped into the buckets.
 21 Because of the uncertainty of these assumptions, a sensitivity analysis has been carried out in this
 22 work.

23

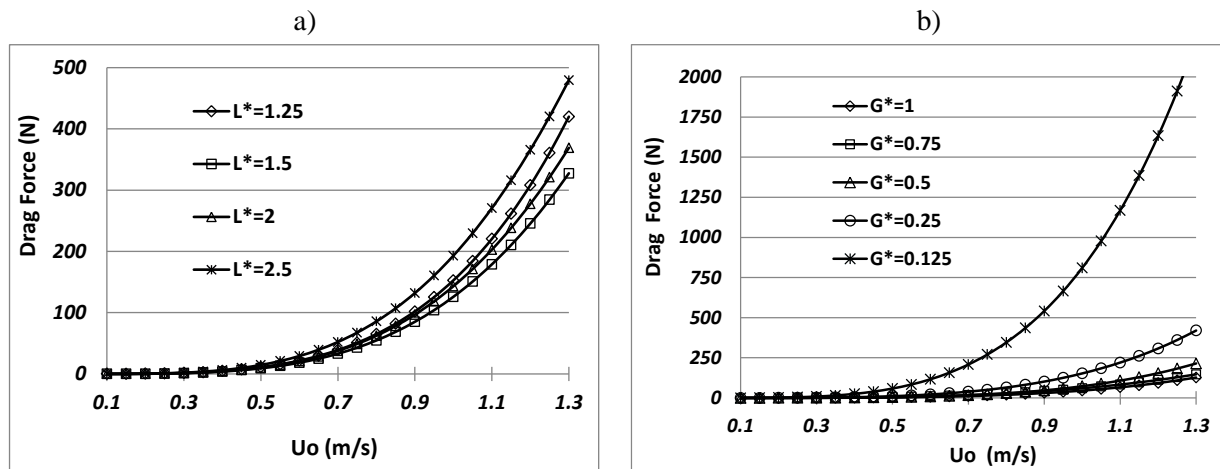


Fig.7 Drag force versus the buckets moving speed; a) for different L^* and $G^*=0.25$; b) for different G^* and $L^*=1.25$

1 In order to assess the portion of the buoyancy force, which is lost, the ratio of drag force to the
 2 buoyancy force is calculated and its variations versus the buckets moving speed are drawn in Fig.
 3 8, for different G^* and L^* . The results show that in case of $G^*=0.125$, if the buckets moving speed
 4 reaches up to 0.64 m/s the ratio of drag force to the buoyancy force would reach up to 100%. It
 5 means that the buoyancy force will be completely consumed by the system losses, therefore in
 6 design and operating the system, the buckets moving speed must be considered less than a
 7 maximum rate. From Fig. 8.a, the maximum speed of the buckets moving is obtained 1.35, 1.3,
 8 1.19 and 1 m/s for G^* equal to 1, 0.75, 0.5 and 0.25, respectively. As shown in Fig. 8.b, the
 9 corresponding values for L^* are equal to 1.25, 1.5, 2 and 2.5 are 0.99, 1.05, 1.01 and 0.93 m/s,
 10 respectively.

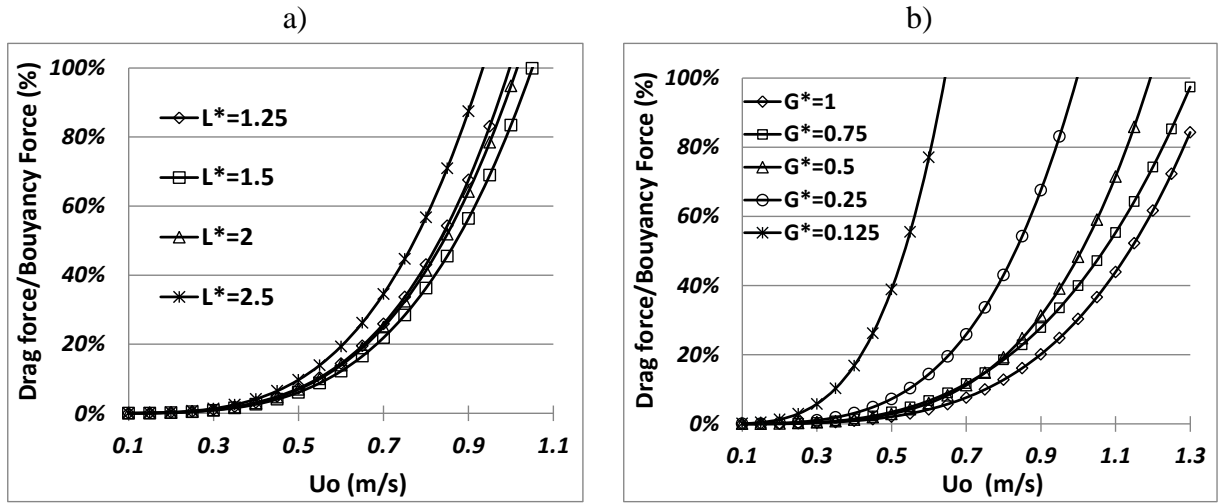


Fig. 8 Drag force per buoyancy force versus the buckets moving speed; a) for different L^* and $G^*=0.25$;
 b) for different G^* and $L^*=1.25$.

The net buoyancy power density (P_{b-Net}) was calculated as the net buoyancy force (F_{b-net}) per cubic meter volume of the tank, by using the following relationship:

$$P_{b-Net} = \frac{F_{b-net} \times U_o}{V_t} \quad (9)$$

Where V_t is the total volume of the tank, and F_{b-net} is the net buoyancy force of the buckets filled by air. Practically, buoyancy force is calculated as $F_b = V_s \times \rho_f \times g$ (F_b is the buoyancy force, V_s is the submerged volume of the object, ρ_f is the density of the fluid, and g is the gravity force). The variation of the net buoyancy power density versus U_o , as illustrated in Fig. 9, show that the net buoyancy power density reaches a maximum value at the buckets moving speed of 0.65 m/s, if L^* and G^* are selected as 0.25 and 1.25, respectively. This emphasizes the significance of the drag force effects on the performance of the BPG system. Fig. 10 shows the

optimum speed of the moving buckets versus the gap and the spacing ratios based on the maximized net buoyancy power density. The results show that the optimum speed of the moving buckets increases by increasing G^* while the optimum speed slightly decreases with increasing L^* . Fig. 10 also shows that the optimum speed is more sensitive to the gap ratios than to the spacing ratio.

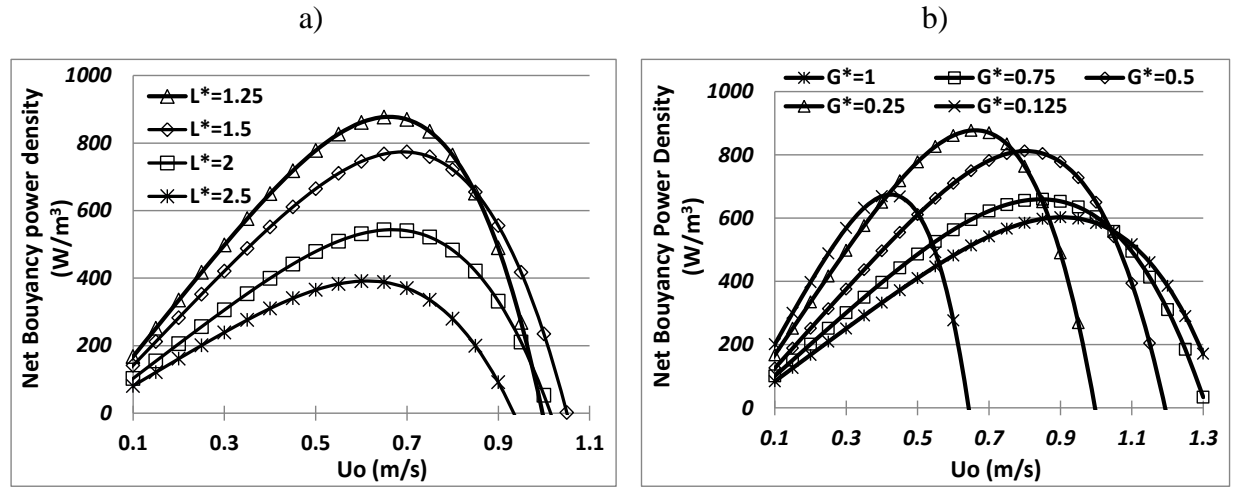


Fig. 9 Net buoyancy power density versus the buckets moving speed, a) for different L^* and $G^*=0.25$, b) for different G^* and $L^*=1.25$.

1

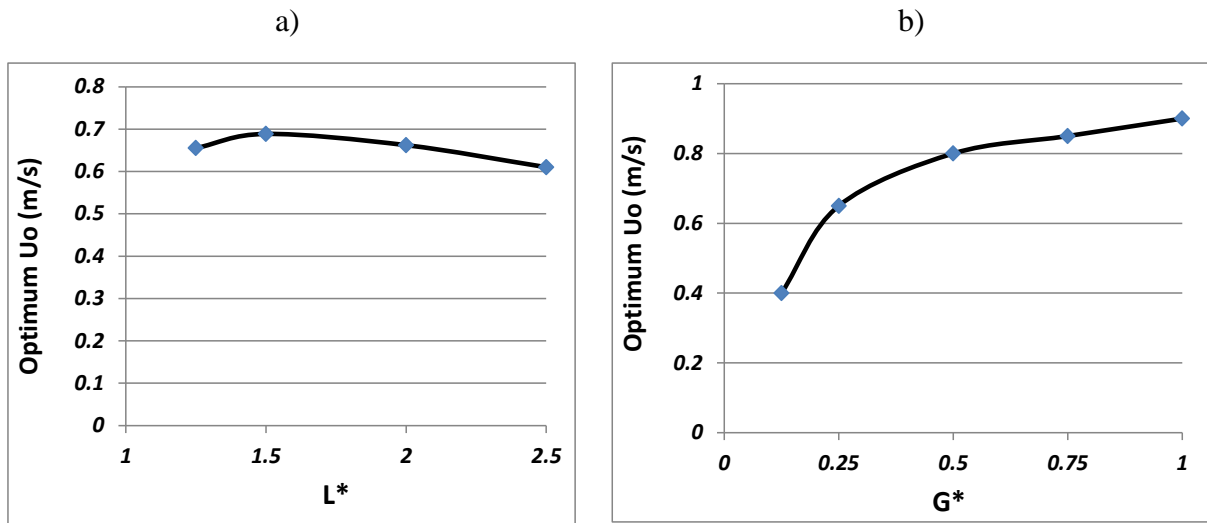


Fig. 10 The optimum speed of the buckets moving versus the gap ratios and the spacing ratios, a) for different L^* and $G^*=0.25$; b) for different G^* and $L^*=1.25$.

2

3.2. Evaluation of the Net Energy Generation

Energy consumption, called energy input, is compressor's energy required for providing pressured air to operate the fluid-air displacement system and also recovery of the other system energy losses. It is determined according to the power required calculated by Equation 8, multiple by the time duration. It can be converted to the energy density by considering the volume of the tank. In addition, energy production, called energy output, is determined according to the net buoyancy power density multiplied by the elapsed time and converted to the energy density by considering the volume of the tank. For one hour time period, Fig. 11 shows the variation of energy density consumption and production versus the buckets moving system, in case of $G^*=0.25$ and $L^*=1.25$. The energy density production versus the buckets moving speed is drawn in Fig. 11. The results show that the energy output is less than energy input because of the effects of the compressor friction, the gearbox losses, wasting of air from the buckets and resistance of the buckets movement trough the fluid. The difference between energy input and energy output has an increasing trend by increased the buckets moving speed so that the total energy input would be completely consumed by the losses in the speed up to 1 m/s. The maximum value of the energy density output occurred at the buckets moving speed of 0.65 m/s, which indicates that lower and higher speeds may negatively affect the performance of the BPG system. Practically, bucket moving speed needs to be optimized for the system to maximize the power output.

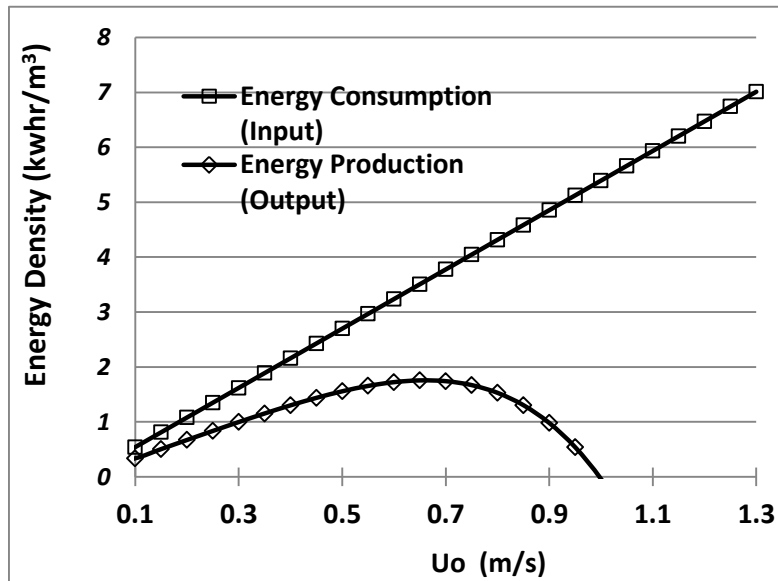


Fig. 11 Energy density production and consumption versus the buckets moving speed in case of $G^*=0.25$ and $L^*=1.25$.

19

3.3. Round Trip Efficiency and Potential Application

1 Round trip efficiency (*RTE*) is defined as the ratio of total energy storage system output (discharge)
2 divided by total energy input (charge) as measured at the interconnection point. Fig. 12 shows the
3 round trip efficiency versus the buckets moving speed with different gap ratios. It indicates that
4 increasing of the buckets moving speed causes the efficiency to decrease because of increasing the
5 system energy losses. For the bucket moving speed of 0.65 m/s and $G^*=0.25$ and $L^*=1.25$, which
6 the maximum energy density output is occurred at, the system efficiency is obtained 50.1%. By
7 increasing G^* , the efficiency will be increased so that the efficiency will be obtained up to 60%
8 for $G^*=1$. Also by reducing the bucket moving speed up to 0.25 m/s, the achieved efficiency would
9 reach 62.2%. It should be noted that at this rate, the energy density output will not reach a
10 maximum value.

11 In order to indicate energy efficiencies in the process of electricity consumption, energy generation
12 and also energy losses during its transmission, a Sankey diagram has been provided as shown in
13 Fig.13. In this figure, the wasting air refers to the air discharge from the compressed air storage
14 that would not trap into the buckets and it is assumed to be 10% in this study. It is shown that the
15 round trip efficiency of the proposed method, obtained to be between 47 and 60% for the buckets
16 moving speed of 0.65 m/s, can be considered as a comparable method with other energy storage
17 technologies, such as Hydro, Flywheels, Batteries, Electrothermal (ETES) and Compressed Air
18 (CAES) which have the round trip efficiency of 65-80%, 80-90%, 75-90%, 65-75% and 65-75%,
19 respectively [36, 37]. There are several technologies available for energy storage with different
20 operating capacities [Fig. 14]. Out of these technologies, the method used in this study,
21 BPG/CAES, has great potential for implementation as storage systems of small to average
22 capacities between 1 kW to 1 MW. BPG/CAES system is a fast response system, which does not
23 need expensive components such as turbines, heat exchanger, chemical reactions, or expensive
24 structures and can be retrofitted with an existing CAES system. Furthermore, it can be built from
25 inexpensive parts that can be, easily, recycled at the end of the service life. As an application
26 example, according to the obtained results in this study, 5 cylindrical buckets on each side of the
27 tank with a diameter of 1.1 m and a length of 4 m are required to generate 100 kW. According to
28 these assumptions, the BPG tank should be 7.5 m height and $3.3 \times 4 \text{ m}^2$ area. Air discharge
29 consumption would also be about $2 \text{ m}^3/\text{s}$ in normal conditions¹.

30

31

¹ Air temperature equal 0 °C and standard atmosphere pressure equal 101.325 KPa

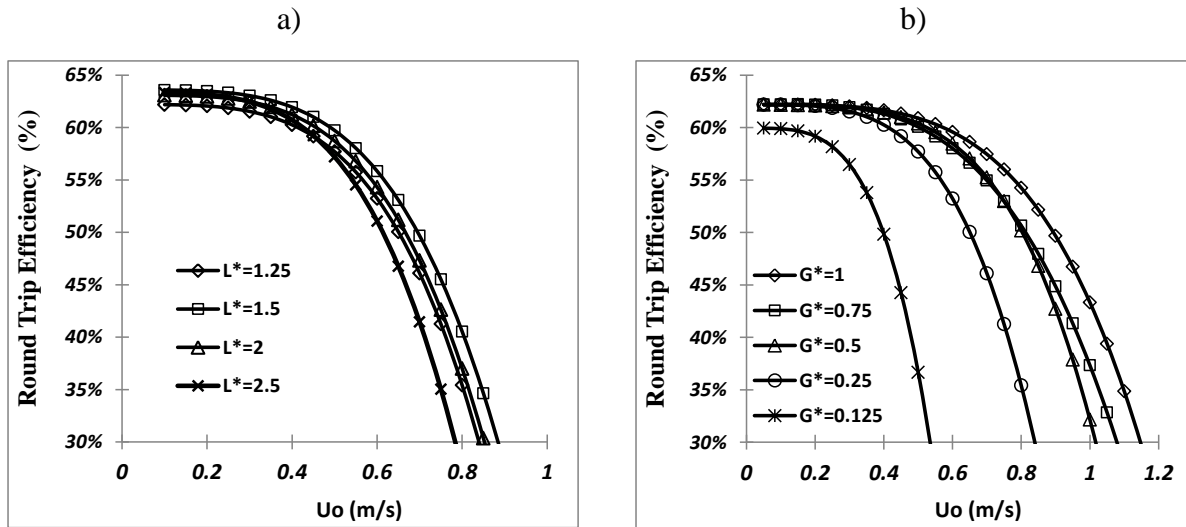
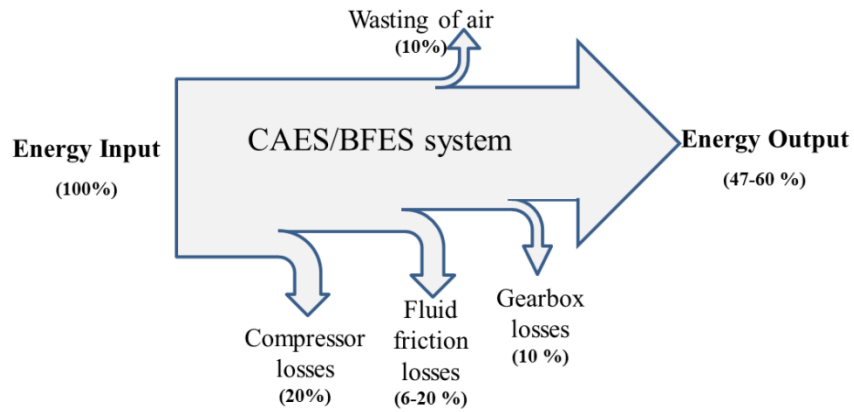


Fig.12. The round trip efficiency of energy storage versus the buckets moving speed, a) for different L^* and $G^*=0.25$; b) for different G^* and $L^*=1.25$.

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2

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Fig.13 Sankey diagram for the CAES/BPG system

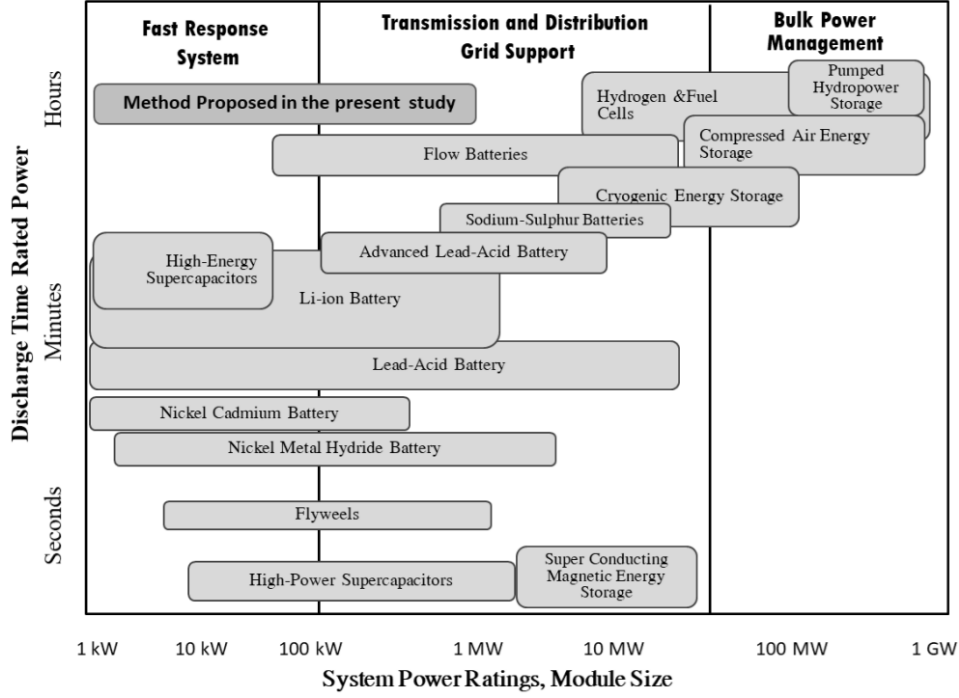


Fig. 14 Classification of the major energy storage technologies (After [37]).

3.4.Sensitivity Analysis Regarding the Round Trip Efficiency

Local sensitivity analysis investigates the influence of a parameter p on a model output $y_i(p)$ around a reference parameter set p^* . Sensitivity coefficients, $S_{i,j}$, are formally defined as first-order partial derivatives of the model output $y_i(p)$ with respect to the parameter p_j [38]:

$$S_{i,j} = \left. \frac{\partial y_i(p)}{\partial p_j} \right|_{p = p^*} \quad (10)$$

If not analytically available, $S_{i,j}$ can in the simplest case be approximated via finite differences, i.e.

$$S_{i,j} \approx \frac{y_i(p^* + \Delta p_j) - y_i(p^*)}{\Delta p_j} \quad (11)$$

In this study, the sensitivity analysis parameters were selected including the efficiency of compressor, the efficiency of gearbox, air wasting from the buckets, the buckets moving speed (U_o), the Gap ratio (G^*) and the Spacing ratio (L^*) and the effects of changing of these parameters on the changes in round trip efficiency (RTE) was evaluated. Table 3 shows the reference value of the parameters in the case of $G^*=0.25$, $L^*=1.25$ and $U_o=0.65$ which provides maximum energy density

1 production. A spider diagram used to compare relative changes in model output to relative changes
 2 in the parameter values can reveal sensitivities for each parameter [38]. The legs of the spider
 3 represent the extent and direction of the effects of changing parameter values. Obtained results, as
 4 shown in Fig.15, indicates the sensitivity analysis for the round trip efficiency (*RTE*). The gap ratio
 5 parameter has the highest effect on the resulting *RTE*; if the gap ratio varies by 10%, the *RTE*
 6 changes by 15.6%. Other main influencing factors are the buckets moving speed and efficiency of
 7 air compressor and gearbox, of which variation by 10.8% results in a change in *RTE* of about 10%.
 8 The impacts of the spacing ratio and air wasting from the buckets are lower than other parameters.
 9 This means that the gap ratio and the buckets moving speed are highly sensitive in the design and
 10 operation of the proposed system. Future work should focus on building a laboratory size air-
 11 displacement system for power generation and model validation using experimental data. Research should
 12 also focus on the design of a system that uses recyclable materials that reduce environmental pollution upon
 13 disposal. A thermodynamic analysis of the experimental system is required to give more information about
 14 the energy efficiency of the air-displacement system.

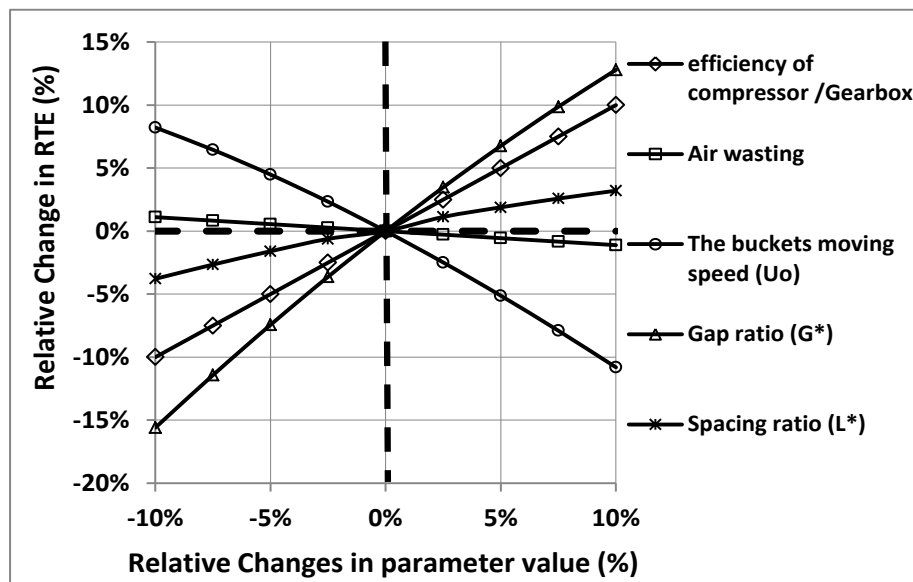
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Table 3 The base values of the sensitivity analysis parameters

| Sensitivity Analysis Parameters | Air compressor efficiency | Air wasting from the buckets | Gearbox efficiency | The buckets moving speed | The wall gap parameter (G^*) | The cylinder gap parameter (L^*) |
|---------------------------------|---------------------------|------------------------------|--------------------|--------------------------|----------------------------------|--------------------------------------|
| Base value | 80% | 10% | 90% | 0.65 m/s | 0.25 | 1.25 |

17



18

19

Fig.15 Sensitivity analysis for the round trip efficiency of CAES/BPG system

20

4. Conclusions

1 This study has introduced a method for coupling the compressed air energy storage (CAES) with
2 buoyancy force energy storage (BPG) for the wind/solar energy storage. Key design parameters of
3 the buoyancy power generation; i.e. L^* , G^* , and U_o were investigated to optimize the system
4 performance. The following points have been concluded from the physical and hydraulic
5 assessments of the CAES/BPG system:

- 6 • ANSYS-Fluent was applied to simulate the performance of the BPG system and k- ω SST
7 turbulence model was selected for calculating the required flow parameters.
- 8 • Based on the ANSYS-Fluent results, the buckets drag force increased with decreasing G^* and
9 increasing L^* .
- 10 • The obtained results showed that the maximum value of net buoyancy power density and the
11 maximum energy density production occurred at $L^*=1.25$, $G^*=0.25$ and $U_o= 0.65$ m/s.
- 12 • The results showed also the optimum of the buckets moving speed has an increasing trend
13 by increased G^* while the optimum speed is slightly decreased with increasing L^* .
- 14 • The *RTE* of the proposed BPG system was between 47% and 60% for different G^* values,
15 indicating its potential as an alternative method to other energy storage technologies, such as
16 Hydro, Flywheels, Batteries, Electro-Thermal (ETES) and Compressed Air (CAES).
- 17 • The sensitivity analysis results showed that the gap ratio parameter has the highest effect on
18 the resulting *RTE* and then the buckets moving speed is the most effective parameter. Inversely,
19 the spacing ratio and air wasting from the buckets have the lowest effects on the resulting *RTE*.

20 The proposed air-displacement system is a promising method to replace chemical-based processes.
21 This system reduces environmental pollution during the operational time and can entirely be
22 recycled at the end of its life. Future work should focus on building a laboratory size air-
23 displacement system for power generation, and model validation using experimental data.

24 25 **5. Acknowledgments**

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27 acknowledge the University of Technology Sydney and Shahrekord University for their support.
28 It can be noted that the authors are pleased to share their data set with readers who wish to replicate
29 the results of this study.

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