Effects of Particle Shape on the Shear Behaviour and Breakage of Ballast: DEM Approach

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Effects of particle shape on the shear behaviour and breakage of ballast: DEM approach

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10 ABSTRACT:

This paper presents results obtained from Discrete Element Method (DEM) to study the effects of 11 particle shape on the shear behaviour and breakage of ballast aggregates. In this study, a series of 12 13 direct shear testing is performed on granular assemblies having various shape sphericities and 14 roundness. A clump-based degradation (breakage) model is incorporated into the DEM simulation to capture the breakage of aggregates during shearing. The results show that the decrease of particle 15 sphericity and roundness (angularity) results in an improvement in the shear performance of granular 16 17 assemblies but subsequent exacerbation in particle breakage, which in turn reduces the shear strength 18 and volumetric dilation. The breakage of particles localizes within an inclined band, with the width 19 and the inclination angle of the band increasing in assemblies comprising particles of low sphericity and roundness. A micromechanical analysis is conducted to examine the anisotropy of internal 20 structures and particle motions in granular assemblies. It is observed that both the shape of particles 21 22 and their breakage significantly influence these factors. Through the microscopic analysis, a fundamental governing mechanism of particle shape effects on the shear strength and the breakage 23 24 of granular materials is investigated at macroscopic scale.

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26 Keywords: Particle breakage; Sphericity and roundness; Shear behaviour; Anisotropy of internal

27 structure; Discrete element method

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28 **1. Introduction**

The importance of particle shape in influencing the shear behaviour of granular materials has been 29 30 extensively studied by many existing studies. For example, in geotechnical engineering, the shape of particles can affect the shear strength, permeability, abrasion resistance of sands, rockfills and railway 31 ballast materials (Bono and McDowell 2016; Chen et al. 2019; Rui et al. 2020; Taiba et al. 2018; Yang 32 and Luo 2015). In the pharmaceutical, food, and chemical industries, particle shape is considered to be 33 a key factor to influence the flowability, mixing, and processing of powders (Ketterhagen et al. 2009). 34 The shape of particles can also affect the packing density and diffusion behaviour of granular materials 35 36 used in energy storage applications such as lithiumion batteries and supercapacitors (Zhang et al. 2022). Moreover, the shape of particles has also reported to affect the filtration efficiency an flow resistance 37 of granular media used in water treatment and wastewater treatment processes (Hamidian et al. 2021). 38 In geotechnical engineering field, the shear behaviour of geomaterials often governs the strength 39 and deformation characteristics of the assemblies. (Cho et al. 2006) and (Altuhafi et al. 2016) compiled 40 several databases containing natural sands of different shapes to comprehensively study particle shape 41 42 effects on the shear behaviour of sand materials. A series of shape-dependent parameter correlations have been provided in their studies to justify particle shape effects on grain packing and mechanical 43 parameters including the extreme void ratios e_{max} and e_{min} , the shear wave velocity V_s , the 44 compression and decompression indices C_c and C_s , and three parameters of critical state line Γ , λ , and 45 ϕ_{cs} . A series of direct shear box testing was performed by (Li 2013) on sands mixed with clays and 46 crushed granite gravels, by which the effect of particle shape on the shear strength of composite soils 47 was explored. Besides the packing and strength characteristics of granular materials, the shape of 48 particles also affects their interface shear behaviour with other geosynthetics (Liu et al. 2021a; Miao et 49

50 al. 2017; Namjoo et al. 2022) or structures (Liu et al. 2022).

Numerical simulation methods such as the Discrete Element Method (DEM) has been widely 51 applied to study the mechanical behaviour of granular materials at microscopic scales, where the 52 53 angularity and breakage of particles can be simulated. There have been numerous studies conducted to investigate the effects of particle shape on the shear behaviour of granular materials (Coetzee 2016; 54 Danesh et al. 2020; Gong et al. 2019; Liu et al. 2019; Wu et al. 2021). They reported that the increase 55 in particle angularity leads to an improved shearing performance of granular materials because of the 56 enhanced inter-particle interlocking. The shape of particles also plays a crucial role in influencing the 57 microscopic responses of granular materials during shearing (Nuebel and Rothenburg 1996). (Zhao et 58 59 al. 2017) performed a series of shearing tests on granular pakcings comprising super-ellipsoids with 60 various shapes, and investigated the shape effects on the internal structure characteristics of granular materials. (Xu et al. 2021) investigated the influence of particle shape on the fabric anisotropy of 61 62 granular materials at their critical states, and found that the critical fabric anisotropy of assemblies decreases with the increase of particle aspect ratio. A study conducted by (Yang et al. 2016) showed 63 that particle shape directly influences the strain localization patterns, fabric distributions, and 64 65 probability distribution of the normalized contact forces within granular assemblies.

Particle degradation (breakage) is another salient feature of granular materials and plays a significant role in influencing the mechanical behaviour of granular assemblies (Chen et al. 2022; Coop et al. 2004; Indraratna et al. 2009; Mcdowell 2002). However, the influence of particle shape effect on particle degradation has not been considered in the above-mentioned studies. (Sun and Zheng 2017) analyzed the breakage-induced shape evolution of ballast aggregates subjected to triaxial compression by using fractal theory. (Jo et al. 2011) found that the shape of particles affects the formation of shear band within crushable assemblies. (Jing et al. 2020) simulated ballast aggregates with different 73 flakiness and elongation indices in DEM, and found that flaky and elongated aggregates produce more particle breakage among all the tested ballast materials. (Nie et al. 2020) simulated the shear behaviour 74 75 of granular materials with different shapes caused by natural erosion process, and found that an 76 increased erosion degree of particles results in the decrease in the shear strength and volumetric deformation. There are some studies showing that the shape of particles influences not only their 77 breakage strength but also their breakage patterns (Afshar et al. 2017; Zhang et al. 2020). A recent 78 79 study carried out by (Seyvedan et al. 2023) using the coupled DEM and extended Finite Element Method (XFEM) showed that the angularity and the eccentricity of particles significantly affect the 80 particle breakage and mechanical behaviour of rock-fills subjected to direct shearing. 81

82 Despite the significant progress achieved thus far, the influence of particle shape on the shear behaviour of granular materials, particularly their breakage responses and the microscopic 83 84 characteristics of aggregates, remains unclear. To address this gap, this study employs a series of direct 85 shearing tests on aggregates with varying shapes and sizes using the DEM. The investigation encompasses an examination of strength, deformation, and breakage band characteristics for granular 86 materials with different sphericities and roundnesses. Additionally, the microscopic properties of 87 88 aggregates, including internal structure anisotropy and particle motion are analysed, through which the mutual influence mechanism of particle shape effects on the macroscopic mechanical behaviour of 89 90 granular materials is investigated from a particulate perspective.

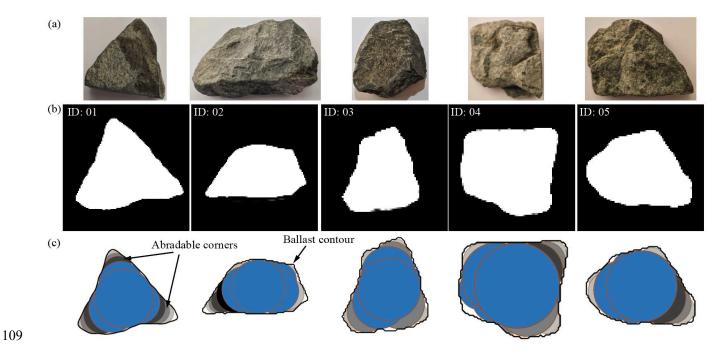
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92 **2.** Discrete element modeling

93 2.1 Modelling irregularly-shaped particles in DEM

94 To capture a high irregularity and angularity of quarried ballast having different shapes and sizes,

95 an X-Ray computed tomography (CT) scanning machine with a resolution of 0.3 mm \times 0.3 mm \times 0.6 mm per voxel was adopted. After scanning, an image-based processing strategy as detailed by (Chen 96 et al. 2019) was applied to reconstruct the irregular morphology of ballast particles. Fig. 1(a and b) 97 98 shows the images of five typical ballast particles and their representative slices taken across the bodies. The obtained greyscale images were then binarized by converting the particle solid into white and the 99 100 background into black, and an algorithm based on the 8-adjacency area method (Ege and Karaca 2016) 101 was developed to automatically extract the particle solid contours, as shown in Fig. 1(c). To represent the irregular shapes of ballast particles in DEM, a group of spheres of varying sizes were clumped 102 together within the contour using the 'Bubble Pack' algorithm (Taghavi 2011). Two parameters, the 103 104 minimum radius ratio $\rho = 0.1$, which represents the size ratio of the smallest to largest pebble in the 105 clump, and the maximum intersection angle $\varphi = 135^\circ$, which describes the distance between two 106 intersecting pebbles, were used to govern the precision of the generated particles. The images of five 107 typical particle clumps are shown in Fig. 1(c), and a total of 40 ballast particles of various shapes were 108 prepared for this study.



110 Fig. 1. (a) Images of five typical ballast particles; (b) CT scanning slices; and (c) created clumps used

- 6 -

113 2.2 Particle shape quantification

114 Particle shape can be fully quantified by three independent sub-quantities, with each describing the shape at different scales or orders. The large scale (first order) focuses on the overall form/ 115 morphology of the particle, and the commonly adopted quantities for large scale include sphericity 116 (Wadell 1933), elongation (Zingg 1935), etc. An intermediate-scale (second order) quantity, such as 117 roundness or angularity (Powers 1953), describes the properties of sharp corners and edges on the 118 particle boundaries. The smallest scale (third order) focuses on the surface texture or the particle 119 120 roughness (Alshibli and Alsaleh 2004). Among the three-scale parameters, particle sphericity and roundness have been acknowledged as the most important quantities as they directly govern the macro 121 and microscopic mechanical behaviour of granular materials (Guo et al. 2022). Therefore, the 122 123 sphericity and roundness values of ballast particles will be considered in the current DEM analysis.

There are various sphericity parameters that have been proposed in the past, and they can be broadly classified into two categories based on principal dimensions (such as Feret's diameter, Aspect Ratio, or Circle Ratio) or overall geometry properties (such as surface area, perimeter or volume). To increase the credibility of description on particle sphericity, two sphericity parameters as suggested by (Liu et al. 2019), the circle ratio (S_c) and the area sphericity (S_a), has been adopted. The S_c and S_a of the 40 selected ballast particles were calculated as given by:

$$S_c = \frac{D_{ins}}{D_{cir}} \tag{1}$$

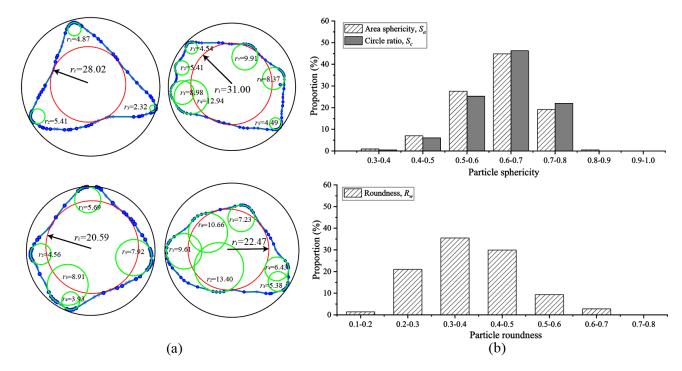
 $S_a = \frac{A_s}{A_{cir}}$ (2)

Where, D_{ins} and D_{cir} are the diameters of the largest inscribed circle and the smallest circumscribed circle, respectively; A_s and A_{cir} are the areas of a particle and its smallest circumscribed circle, 134 respectively, as shown in Fig. 2(a).

The roundness and angularity are used to describe the corners and sharp edges of a particle, with a large roundness value indicating a low level of angularity. By using the projections of particles on the 2-dimensional plane, (Wadell 1933) proposed a classic methodology to determine the roundness of a particle, as expressed by:

$$R_w = \frac{1}{N} \frac{\sum r_i}{R} \tag{3}$$

where, *N* is the number of particle corners; r_i is the radius of curvature of the corner; *R* is the radius of the maximum inscribed circle in the plane of measurement. In this study, a technique called 'locally weighted scatter plot smoothing' (LOESS) (Zheng and Hryciw 2015) was adopted for ballast roundness computation, and the corners of ballast particles are determined, as shown in Fig. 2(a).



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Fig. 2. (a) Diagrams of shape quantification for 4 typical particles; and (b) distribution histograms of
sphericity and roundness for 40 ballast particles

147 Fig. 2(b) shows the distribution histograms for the two sphericity parameters and the roundness of 148 the 40 ballast particles. It can be seen that more than 90% of the examined ballast particles have S_c and S_a values between 0.50 and 0.80, with sphericity values of 0.60~0.70 accounting for the greatest proportion. Particle roundness ranges from 0.15 to 0.50, with the majority of particles having R_w of 0.30. Based on the calculated sphericity and roundness values, 40 ballast particles are classified into four groups: (i) low-sphericity-low-roundness, $S_1 - R_1$ ($0.40 \le S_c, S_a < 0.63$ and $0.10 \le R_w <$ 0.30), (ii) low-sphericity-high-roundness, $S_1 - R_2$ ($0.40 \le S_c, S_a < 0.63$ and $R_w \ge 0.30$), (iii) highsphericity-low-roundness $S_2 - R_1$ ($0.63 \le S_c, S_a < 1.0$ and $0.10 \le R_w < 0.30$), and (iv) highsphericity-high-roundness, $S_2 - R_2$ ($0.63 \le S_c, S_a < 1.0$ and $R_w \ge 0.30$).

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157 2.3 Modelling ballast breakage in DEM

158 Upon repeated train loading, ballast undergoes progressive degradation and breakage. The dominant breakage patterns of granular materials has been reported as corner abrasion or surface 159 attrition (Sun et al. 2014). To model the breakage of rigid ballast clumps in DEM, (Liu et al. 2021b) 160 161 developed a 2D abrasion model and the model has been well validated by a series of DEM simulations 162 for Los Angeles Abrasion (LAA) testing on ballast aggregates. The proposed particle degradation model has been widely used in the existing discrete element modeling of ballast aggregates because of 163 164 its superiority in capturing the corner abrasion behaviour of irregular ballast particles in the long-term 165 and improved efficiency in computational resources (Chen et al. 2022, 2023).

According to (Liu et al. 2021b), the irregularly-shaped particles are abraded in either shearing or crushing mode based on the contact force acting on the sharp corner. The broken corner pebble will be automatically removed from the system and replaced by either one or two newly-introduced fragment balls located tangent to its parent clump if a maximum contact force criterion is satisfied. The sizes of the fragment balls are determined based on the non-overlapping volume between the broken pebble and its parent clump. A linear size expansion will be applied to the fragment balls after their

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172 introduction for the mass conservation of the entire system. The breaking sequence of pebbles in each ballast clump is represented by the color depth as shown in Fig. 1(c). In addition, to prevent ballast 173 clump from limitless breaking, pebbles that are able to be abraded is selected and predefined based on 174 175 their sizes relative to the largest pebbles in each ballast clump. Fig. 1(c) shows the potential breakable pebbles for the five typical ballast clumps, with the unbreakable parent clumps being colored as blue. 176 The developed abrasion model was incorporated into the current DEM analysis, and it was 177 178 automatically triggered during the simulation to capture the breakage of ballast aggregates during 179 loading. The validation of the particle degradation model can refer to Section 3.

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181 2.4 Direct shear test simulation

In this study, a series of direct shear test simulations were conducted on ballast aggregates of 182 various shapes. To allow for a clearer representation of the shear behaviour and provide valuable 183 184 insights into the granular material's response under shearing conditions, the current DEM analysis was conducted using 2D modeling instead of 3D. A total of four samples were prepared by choosing ballast 185 particles randomly from different particle groups. The samples were created by first placing overlapped 186 circular disks with a specific certain particle size distribution (PSD) inside a rectangular shearing box 187 188 having dimensions of 500 mm in height, 600 mm in width at the bottom, and 700 mm at the top, as illustrated in Fig. 3. The bottom shearing box was 100mm wider than the upper box to ensure a constant 189 190 shearing area. The PSD complied with the Chinese Railway Ballast Standard (TB/T 2140-2008), which 191 is comparable to other widely-used standards across the world, such as the Australian Standard AS 2758.7 ($d_{50} = 35$ mm). The disk clouds were initially cycled to reach their equilibrium state when the 192 unbalanced force ratio of the entire system was less than 10^{-5} , and the disks were then replaced by 193 194 clumps of irregularly shaped ballast that had volumes equal to the corresponding disks (measured in

unit thicknesses out of plane). Prior to any subsequent shearing, all the samples were preloaded under
a normal pressure of 100 kPa to increase the density of the ballast aggregates.

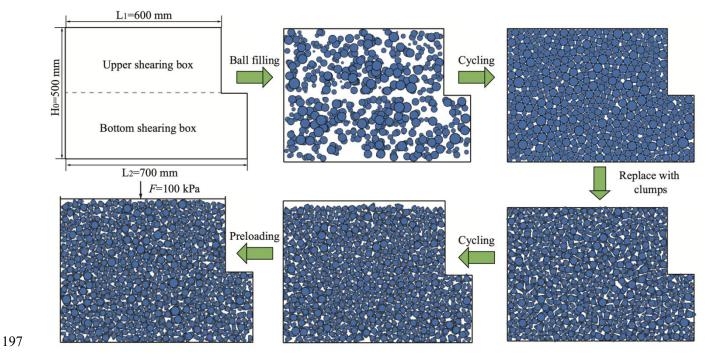




Fig. 3. Preparation of DEM model for direct shear test simulation

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3. Parameter calibration and model validation

In addition to particle size and shape, the contact model and micro-mechanical parameters can also affect the accuracy of DEM simulation. In this study, a linear contact law was applied to simulate the contacts among particles. Before applying the created irregular ballast particles and the proposed degradation model to the current DEM analysis, a series of preliminary simulations on the triaxial testing (Fig. 4(a)) and the Los Angeles Abrasion (LAA) testing (Fig. 4(b)) were performed to determine the appropriate parameters for ballast aggregates and to validate the effectiveness of the particle degradation model in capturing ballast breakage behaviour.

208 The predicted shear stress-strain responses were compared with those obtained using large-scale

209 triaxial testing by (Indraratna et al. 2013). A DEM model with an initial dimension of 300 mm (D) \times 600 mm (H) identical to the triaxial chamber size was prepared. The ballast particles were randomly 210 selected from the established particle library (Chen et al. 2019) for the generation of the aggregates, 211 212 with its particle size distribution (PSD) following the Australian Standard for ballast, AS 2758.7 (2015). The monotonic shearing was conducted on the ballast aggregate under various values of friction 213 coefficient (μ) and normal and shear stiffness of particle contacts (k_n and k_s), which are considered as 214 215 the predominant parameters governing the stress-strain behaviour of granular materials in discrete element modeling. Fig. 4(a) shows the shear stress-strain responses predicted by the DEM model 216 capturing particle breakage in contrast to the experimental data provided by (Indraratna et al. 2013). In 217 218 essence, the DEM model simulating particle degradation has made a satisfactory prediction of the shear 219 stress-strain response of the ballast aggregates for a given confining pressure albeit some fluctuations. The calibrated micro-mechanical parameters for ballast aggregates are summarized in Table. 1. A 220 221 global damping coefficient of 0.7 was adopted to represent energy dissipation, so that any non-physical oscillation of small-sized particles could be avoided during the DEM simulation. 222

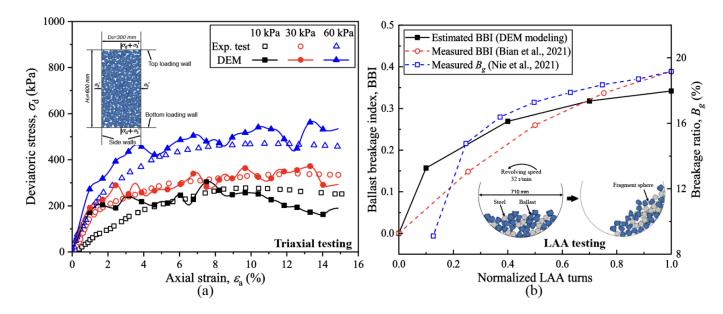




Fig. 4. (a) Shear stress-strain responses obtained by DEM modeling and laboratory tests by (Indraratna

et al. 2013) in triaxial testing; (b) the estimated BBI compared with the measured BBI by (Bian et al.

226 2021) and the B_g by (Nie et al. 2021) in LAA testing

Parameters	Values
Ballast density (kg/m ³)	2700
Contact stiffness of ballast, k_{nb} , k_{sb} (N/m)	5.0×10 ⁸
Contact stiffness of walls, k_{nw} , k_{sw} (N/m)	1.0×10^{9}
Friction coefficient of ballast, μ_b	0.8
Friction coefficient of wall, μ_w	0.5
Local damping	0.7

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Table 1: Micromechanical parameters used in the DEM analysis

The calibrated parameters were then used in the numerical simulations on the LAA testing. The 228 detailed information about the LAA modeling can refer to (Liu et al. 2021b). Fig. 4(b) shows the 229 estimated Ballast Breakage Index (BBI) with the increase of the normalized LAA turns (defined as the 230 current LAA turns relative to the total LAA turns). As comparison, the BBI by (Bian et al. 2021) and 231 the Marsal's breakage index B_q by (Nie et al. 2021) measured in their laboratory testing are also 232 presented in Fig. 4(b). It is seen that both the DEM modeling and the laboratory testing exhibited 233 234 comparable trends with an increase in the normalized LAA turns, where the breakage index values (BBI or B_g) increased at a diminishing rate, indicating a gradually declining ballast breakage. This is 235 because continuous abrasion causes ballast to become rounder, reducing the breakage possibility of 236 individual ballast particle (Guo et al. 2018; Qian et al. 2017). 237

Based on the aforementioned calibration and validation, the DEM model used in this study can be justified as being able to accurately represent the mechanical and breakage behaviour of ballast aggregates, and the numerical results generated by the current DEM analysis should have a high credibility for the discussion of particle shape effect.

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243 **4. Results and Discussions**

The direct shearing was then performed on ballast aggregates under four different normal stresses of $\sigma_n = 15, 35, 55, \text{ and } 75 \text{ kPa}$ until a horizontal displacement of $\Delta_s = 60 \text{ mm}$ was reached. The clumpbased particle degradation model was automatically triggered every 200 cycling steps to capture the breakage of ballast particles during shearing. In addition, DEM simulations were also performed without incorporating the degradation model to compare the effects of particle breakage on the macro and microscopic behaviour of ballast aggregates.

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251 4.1 Shear stress and volumetric deformation

The predicted shear stress and volumetric deformation for different ballast groups subjected to 252 various normal stresses are presented in Fig. 5 and Fig. 6. The results predicted by the corresponding 253 254 breakable DEM models are also included to investigate the influence of particle breakage on the shear stress and volumetric deformation. It is seen that the breakable samples exhibit lower shear stresses 255 256 than their equivalent unbreakable samples, and these differences become greater owing to the elevating particle breakage occurred at higher normal pressures. When ballast breakage is prevented, the 257 aggregate tends to dilate immediately during the shearing; by comparison, significant volumetric 258 compression was observed in all the breakable scenarios, especially in those under higher normal 259 260 pressures.

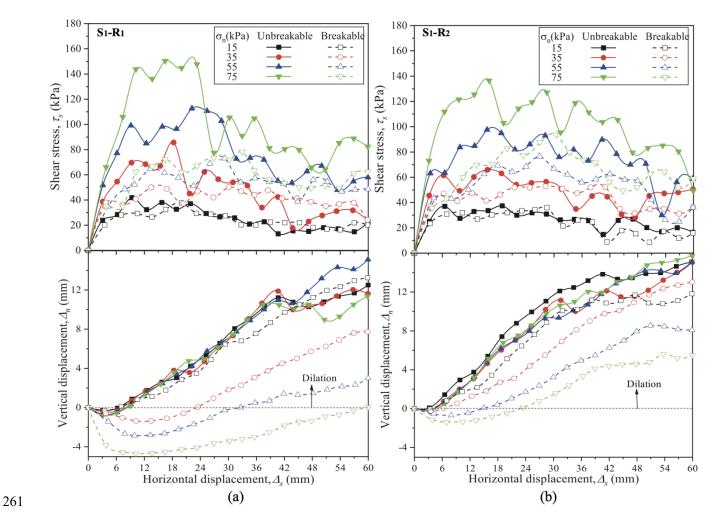


Fig. 5. The responses of shear stress and vertical displacement for (a) $S_1 - R_1$; and (b) $S_1 - R_2$

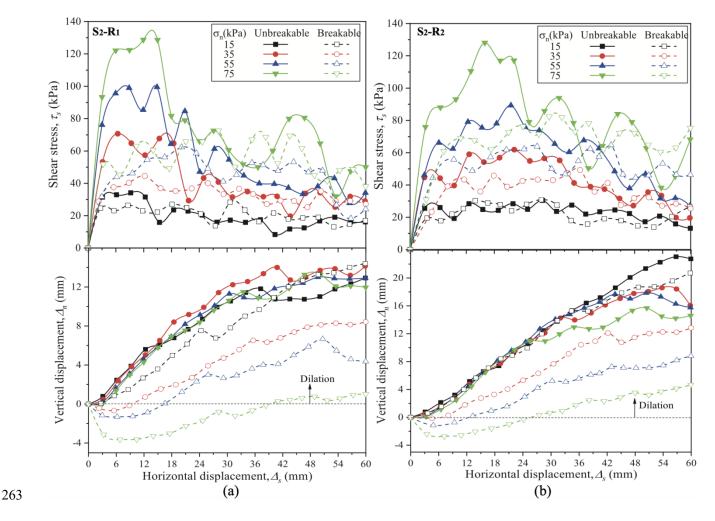


Fig. 6. The responses of shear stress and vertical displacement for (a) $S_1 - R_1$; and (b) $S_1 - R_2$

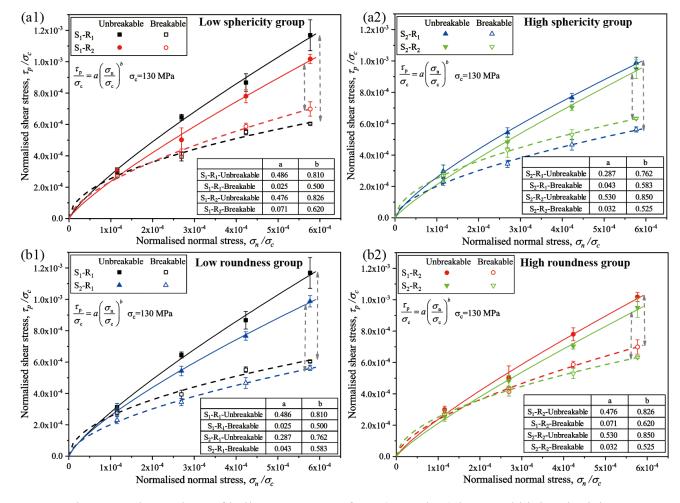
Fig. 7(a1 and a2) shows the strength envelops of ballast aggregates with different particle roundness from low- and high- sphericity groups. Previous studies have shown that the shear strength envelops of granular materials tend to be nonlinear as a result of interparticle interlocking and breakage. In this study, the nonlinear model proposed by (Indraratna et al. 1993) is adopted to examine the shear responses of ballast aggregates, as given:

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$$\frac{\tau_p}{\sigma_c} = a(\frac{\sigma_n}{\sigma_c})^b \tag{4}$$

where, the peak shear stress τ_p and the normal pressure σ_n were normalized with the uni-axial compressive strength $\sigma_c = 130$ MPa of parent rock for ballast material; *a* and *b* are two dimensionless parameters. As expected, the strength envelop of ballast aggregate is significantly affected by particle shapes and particle breakage. Considering the unbreakable scenarios, it is seen that the two low-

roundness aggregates (i.e., $S_1 - R_1$ and $S_2 - R_1$) obtained higher peak strengths than other groups 275 having similar sphericities but higher roundness (i.e., $S_1 - R_2$ and $S_2 - R_2$). This is because less 276 rounded particles have more angular corners of large curvatures, which can provide resistance during 277 shearing and lead to a higher shear strength. In contrast, the breakable samples exhibit lower shear 278 strength than their comparable unbreakable ones due to reduced shearing resistance associated with the 279 breakage of sharp corners. Furthermore, the strength reduction in low-roundness aggregates is greater, 280 which may be due to the increased corner breakage during shearing. 281





284

Fig. 7. The strength envelops of ballast aggregates from (a1 and a2) low- and high-sphericity group; 283 and (b1 and b2) low- and high-roundness group

Fig. 7(b1 and b2) shows the strength envelops of ballast with various sphericities from low- and 285 high- roundness groups. As expected, the increased irregularity of ballast particles with higher 286

sphericity $(S_1 - R_1, S_1 - R_2)$ results in higher shear strengths than those with low-sphericity $(S_2 - R_1, S_2 - R_2)$. Additionally, for two assemblies (either from the low-roundness or high-roundness groups) under a given applied normal stress, the breakage-induced strength decreases are almost identical regardless of their sphericities. This finding implies that the overall particle morphology plays a less significant role in affecting the shear strength development of the ballast aggregate compared to particle corner angularity, which therefore ought to be given greater consideration when selecting ballast materials for railroad construction to ensure better bearing capacity.

294

295 *4.2 Ballast breakage*

296 Fig. 8 shows the locations of the ballast fragments simulated in DEM (represented by blue dots) for $S_1 - R_2$ at the shearing displacement Δ_s of 15, 30, 45, 60 mm under $\sigma_n = 75$ kPa. It is shown that 297 the breakage is localised within an inclined zone (width, d_b) developing from the rear of the top 298 299 shearing box to the front of the bottom box, and this zone is observed to become narrower as shearing progresses (i.e., d_b =352 and 303 mm at Δ_s =15 and 60 mm, respectively). To quantitatively examine 300 301 the distribution of ballast fragments, an inclined breakage band within which more than 85% fragments localize is defined. The width d_b and the inclined angle β_b of the breakage band for $S_1 - R_2$ at 302 different shearing displacements are presented in Fig. 8. At $\Delta_s = 15$ mm, the d_b is 352 mm, which is 303 about 10.05 d_{50} , with the β_b of 16.6° towards the horizontal plane, however, the d_b decreases to 303 304 mm (8.66 d_{50}) accompanied by an increase in the β_b to 20.6° at $\Delta_s = 60$ mm, indicating a 305 306 concentrating particle breakage in assemblies during shearing.

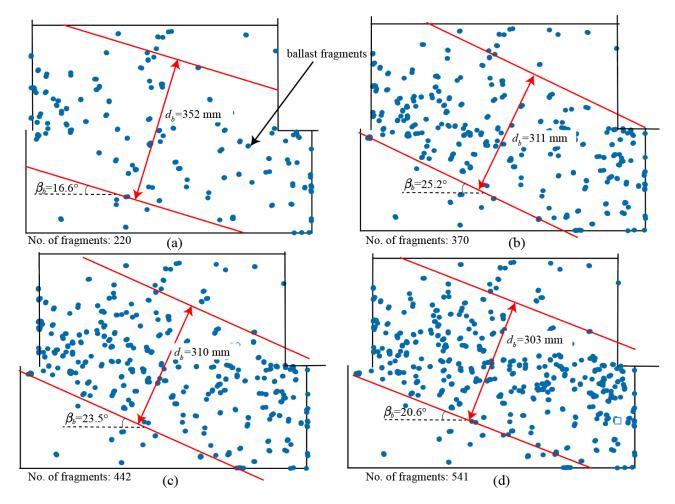


Fig. 8. The distribution of ballast fragments in $S_1 - R_2$ under $\sigma_n = 75$ kPa at Δ_s of (a) 15 mm; (b) 30 mm; (c) 45 mm; and (d) 60 mm

To investigate the influence of particle shape on the amount of breakage, the total volumes of 310 ballast fragments V_f in aggregates having various shapes as shearing develops under $\sigma_n = 75$ kPa are 311 presented in Fig. 9(a). It is seen that the predicted V_f of two low-roundness groups ($S_1 - R_1$ and $S_2 - R_1$ 312 R_1) are greater than that of two high-roundness ones $(S_1 - R_2 \text{ and } S_2 - R_2)$, indicating increased 313 particle breakage in less rounded aggregates owing to their increasing corner angularities. In contrast, 314 the breakage in samples with varied sphericity but similar roundness $(S_1 - R_1 \text{ with } S_2 - R_1, \text{ or } S_1 - R_1)$ 315 R_2 with $S_2 - R_2$) is close during the most shearing phase, except to the $S_2 - R_1$ which obtains a 316 relatively high value of V_f at the end of shearing owing to the continuous breakage of corners with 317 large curvatures. 318

319	Fig. 9(b and c) shows the evolution of d_b and β_b of ballast aggregates having various particle
320	shapes under $\sigma_n = 75$ kPa. At $\Delta_s = 6$ mm, the d_b of two low-roundness groups $(S_1 - R_1 \text{ and } S_2 - R_1)$
321	are 450 mm (12.86 d_{50}) and 390 mm (11.14 d_{50}), respectively, however, that of two high-roundness
322	groups $(S_1 - R_2 \text{ and } S_2 - R_2)$ are about 325 mm (9.29 d_{50}). With the increase of Δ_s , the d_b of $S_1 - R_1$
323	and $S_2 - R_1$ gradually decrease, and maintain at about 310~325 mm (8.86~9.29 d_{50}) after the Δ_s
324	reaches 36 mm. By comparison, the d_b of $S_1 - R_2$ and $S_2 - R_2$ show little variation over the entire
325	shearing process. As for the β_b , it is seen from Fig. 9(c) that the β_b of $S_1 - R_1$ and $S_2 - R_1$ are about
326	21.6° and 25.3° at $\Delta_s = 6$ mm, respectively; however, the β_b of $S_1 - R_2$ and $S_2 - R_2$ are relatively
327	greater, with values of 27.9° and 28.5°. As shearing develops, the β_b of $S_1 - R_2$ and $S_2 - R_2$ decrease
328	and maintain at about 18.0° at later stage of shearing. In contrast, the β_b of $S_1 - R_1$ and $S_2 - R_1$
329	experience minor decrease and reach ultimate values of about 23.0°.

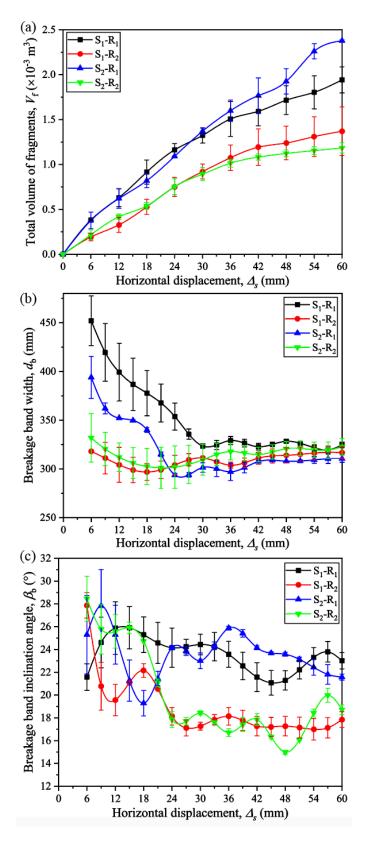


Fig. 9. The evolution of (a) total volume of fragments V_f ; (b) breakage band width d_b ; and (c) breakage

band inclination angle β_b of ballast aggregates with various shapes

333 The breakage band of low-roundness aggregates at the initial stage of shearing is wider than that

of high-roundness ones. This is because more particles are broken outside the breakage band (that is 334 the front of the top shearing box and the rear of the bottom shearing box), which results in a more 335 dispersed particle breakage. However, as less rounded particles are more prone to breaking than 336 337 rounded ones, the subsequent shearing induces an increasing particle breakage within the breakage band region from the rear of the top shearing box to the front of the bottom shearing box in the low-338 roundness aggregates, causing the breakage band to narrow. In contrast, the overall particle breakage 339 in high-roundness aggregates is comparably lower, and it is observed to be more concentrated near the 340 horizontal plane where large shear deformation occurs, resulting in a smaller inclination angle of the 341 breakage band during shearing. These results imply that particle corner angularity has a greater impact 342 343 on the breakage of ballast compared to the sphericity, producing more broken fragments distributing 344 across a larger region within the assemblies.

345

346 *4.3 Microscopic responses*

347 4.3.1 Characteristics of inter-particle interaction

The distributions of inter-particle contact forces in breakable and unbreakable $S_1 - R_1$ at different 348 shearing displacements ($\Delta_s = 0, 15, 60 \text{ mm}$) under $\sigma_n = 75 \text{ kPa}$ are shown in Fig. 10. Contacts are 349 represented as solid lines connecting the centroids of two contacting particles, with line thicknesses 350 proportional to contact force magnitudes. The inter-particle contacts within the assembly are 351 homogeneously distributed at the start of shearing ($\Delta_s = 0$ mm). As shearing progresses, the contacts 352 between particles intensify, accompanied by increases in the maximum and the averaged contact force 353 of assemblies, and an obvious band develops from the rear of the top shearing box to the front of the 354 355 bottom box, within which relatively enhanced inter-particle contacts are localized. In comparison to $\Delta_s = 15$ mm, the inter-particle contacts at the end of shearing ($\Delta s = 60$ mm) are weaker, with contact 356

forces decreasing, particularly for the unbreakable sample. This microscopic response explains the macroscopic strength softening behaviour after achieving the peak shear stress state, as shown in Fig. 5 and Fig. 6. The breakage of particles also plays a profound effect on the distribution of inter-particle contact, which is stronger and more intensified in the unbreakable sample. This observation implies that when subjected to direct shearing, partilce breakage decreases the intensity of inter-particle contact within the assembly, and therefore reduced shear strengths are expected in breakable samples.

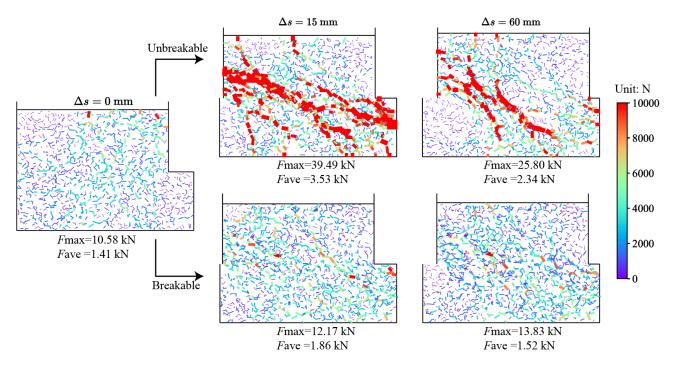


Fig. 10. The distributions of inter-particle contact in breakable and unbreakable $S_1 - R_1$ at typical shearing displacements (i.e., $\Delta_s = 0$, 15, 60 mm) under $\sigma_n = 75$ kPa

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Fig. 11 shows the distributions of inter-particle contact in unbreakable and breakable samples with different particle shapes at $\Delta_s = 15$ mm and $\sigma_n = 75$ kPa. When breakage is prohibited, it is observed that the distribution of inter-particle contact is significantly affected by particle shape, which is intensified as the sphericity and roundness of the particle inside the assembly decrease. In contrast, when breakage is permitted, the influence of particle shape is diluted, and the distributions of interparticle contact within the four breakable samples show marginal differences regardless of their

372 sphericity and roundness.

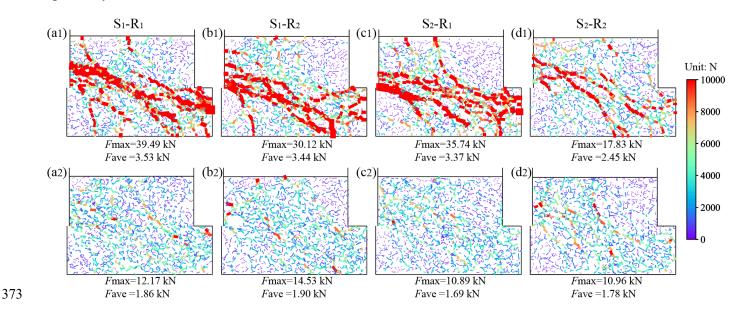


Fig. 11. The distributions of inter-particle contact in (a1-d1) unbreakable samples; and (a2-d2) breakable samples at $\Delta_s = 15$ mm under $\sigma_n = 75$ kPa

To investigate the distribution of inter-particle contact force within the assembly, the spatial space is evenly divided into 36 bins of a bin angle of 10°, and the contact force vectors $(f(\omega_i))$ that fall within the *i*-th bin are collected to calculate the distribution density $(P(\omega_i))$ of inter-particle contact force in the *i*-th bin, as given by:

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$$P(\omega_i) = \frac{\sum f(\omega_i)}{N_i F_{ave}}$$
(5)

where, N_i is the number of inter-particle contacts in the *i*-th bin, F_{ave} is the averaged contact force. The Fourier analysis is performed on the $P(\omega_i)$ based on Rothenburg and Bathurst [5] and Liu et al. [2] to quantify the anisotropy of inter-particle contact forces, as given by:

$$F(\theta_i) = 1 + a\cos 2(\theta_i - \theta_a) + b\cos 4(\theta_i - \theta_a)$$
(5)

where, $F(\theta_i)$ is the distribution density of inter-particle contact force at the orientation angle of θ_i ; *a*, *b*, and θ_a are fitting parameters, with the |a| + |b| and θ_a representing the degree of anisotropy and principal orientation of inter-particle contact force.

Fig. 12 shows the evolution of anisotropy level |a| + |b| and the principal anisotropy orientation - 24 -

 θ_a for breakable and unbreakable $S_1 - R_1$ under $\sigma_n = 75$ kPa. It is seen that the |a| + |b| and θ_a of the assemblies rapidly increases to its peak with the onset of shearing. As shearing progresses, the |a| + |b| progressively decreases to a residual value, whilst the θ_a remains constant until the end of loading. In comparison to unbreakable scenarios, it is seen that the |a| + |b| and θ_a of breakable scenarios are comparatively lower, indicating that particle breakage reduces the anisotropy of interparticle contact forces, which is detrimental to the development of shear resistance of the assembly.

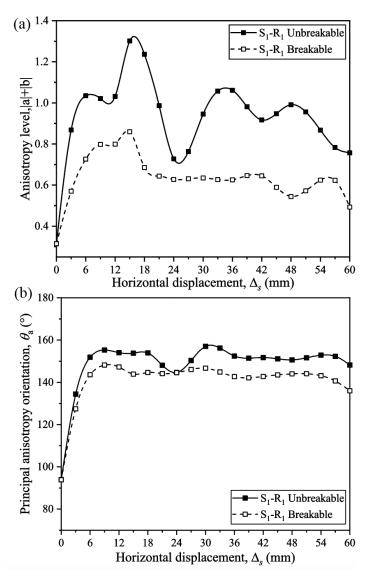
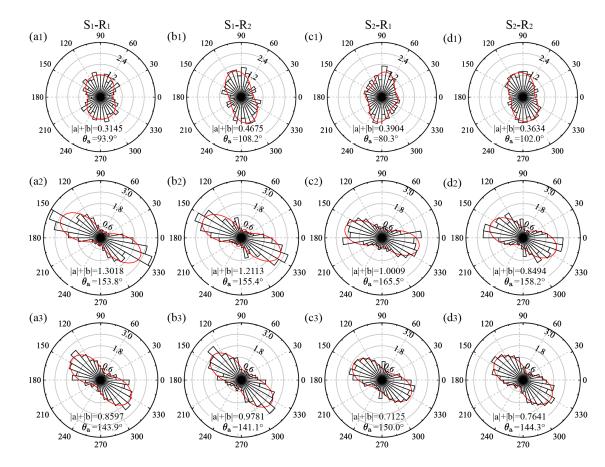


Fig. 12. The evolution of (a) anisotropy level |a| + |b|; and (b) principal anisotropy orientation θ_a for unbreakable and breakable $S_1 - R_1$ sample at $\sigma_n = 75$ kPa

Fig. 13 (a1-d1) show the rose diagrams of inter-particle contact forces for the four samples under

 $\sigma_n = 75$ kPa before shearing. It is seen that the inter-particle contact forces are vertically distributed in order to support the self-weight of ballast aggregate as well as the applied normal stress. The rose diagrams of inter-particle contact forces for the four samples at $\Delta_s = 15$ mm in unbreakable and breakable scenario are shown in Fig. 13 (a2-d2) and Fig. 13 (a3-d3), respectively. As shearing develops, the inter-particle contact force orientates towards horizontal plane, with an orientation close to that of the contact force distributions as observed in Fig. 11.

The |a| + |b| and θ_a of each scenario is also presented in Fig. 13. The |a| + |b| of the four 405 samples prior to shearing is relatively small, with a value of around $0.31 \sim 0.47$, indicating a low 406 anisotropy level of inter-particle contact forces. The shearing increases the contact force anisotropy as 407 408 the |a| + |b| increases to 0.85 ~ 1.30 and 0.71 ~ 0.97 for unbreakable and breakable scenario, 409 respectively. Meanwhile, the orientation of principal inter-particle contact force develops from θ_a of $80.3^{\circ} \sim 108.2^{\circ}$ to $153.8^{\circ} \sim 165.5^{\circ}$ and $141.1^{\circ} \sim 150.0^{\circ}$. When it comes to the effect of particle shape, 410 411 it is seen that the differences in θ_a of assemblies with various particle shapes are marginal. However, a smaller anisotropy level of interparticle contact force is expected within assemblies having higher 412 particle roundness or particle sphericity, which explains the shear strength reduction in assemblies with 413 414 more spherical and rounder particles as shown in Fig. 7.



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Fig. 13. The rose diagrams of inter-particle contact forces for ballast aggregates with various shapes 416 (a1-d1) before shearing; (a2-d2) unbreakable and (a3-d3) breakable samples at $\Delta_s = 15$ mm 417 According to the analysis of the contact chain distribution and the evolution of anisotropy of 418 contact forces presented above, both the shape and breakage of the particle have a considerable impact 419 on the characteristics of inter-particle interaction performance of ballast assemblies. With the increase 420 421 of particle sphericity and roundness as well as the permission of particle breakage, the intensity of contact chains and the anisotropy of contact forces of the assembly decrease, consequently resulting in 422 a reduced macroscopic shear strength. 423

425 *4.3.2 Characteristics of particle motion*

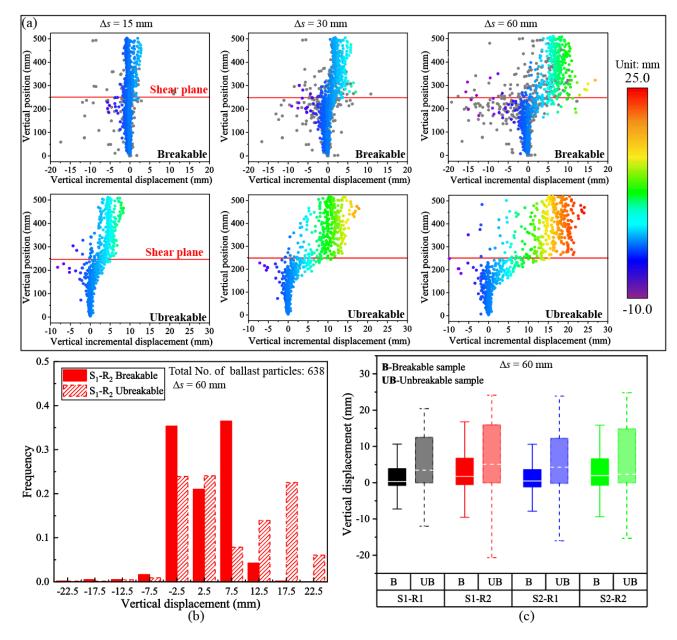
426 The characteristics of particle motion in terms of translational displacement and rotation for 427 aggregates with various shapes of are analysed to examine the fundamental mechanism underlying the

dilatation of ballast. Fig. 14(a) shows the profiles of particle vertical displacement at $\Delta_s =$ 428 15, 30, 60 mm for the breakable and unbreakable $S_1 - R_2$ under $\sigma_n = 75$ kPa. Each ballast particle is 429 represented as a dot in the profile, together with information about its position and incremental 430 431 displacement along the vertical direction (relative to $\Delta_s = 0$ mm). The displacement profiles of the generated ballast fragments after breakage are also included in the figure as represented by gray dots. 432 During the shearing progress, the vertical displacement of ballast aggregate in the bottom box is quite 433 minimal (< 2.5 mm). In comparison, those in the top box and close to the shearing plane exhibit 434 relatively greater vertical incremental displacement, which grows steadily as the shearing progresses. 435 These vertical displacements have been reported as the largest contributor to the volumetric dilation of 436 437 the ballast assembly.

Fig. 14(b) shows the histogram of the percentage of ballast particles with different vertical 438 displacements for the breakable and unbreakable $S_1 - R_2$ at $\Delta_s = 60$ mm under $\sigma_n = 75$ kPa. It is 439 shown that particle breakage significantly reduces the vertical incremental displacements of ballast 440 aggregates. In the breakable groups, more than 90% of ballast particles exhibit vertical displacements 441 ranging from approximately -2.5 mm to 7.5 mm. Conversely, the unbreakable samples show an 442 443 increased proportion of particles having greater vertical displacements, ranging from -2.5 mm to 22.5 mm. This phenomenon leads to a restrained volumetric dilation in the breakable samples, as observed 444 in Fig. 5 and Fig. 6. Moreover, a noteworthy observation is that a majority of the ballast fragments 445 undergo negative vertical displacements, especially those near the shear plane. This suggests that the 446 fragments tend to settle down after breaking from their parent ballast particles, further reducing the 447 overall volumetric dilation of the breakable assembly. 448

449 Fig. 14(c) shows a box plot comparing the vertical displacements of breakable and unbreakable aggregates with various shapes. The results reveal that aggregates with less spherical shapes $(S_1 - R_1)$ 450 - 28 -

and $S_1 - R_2$) or rounder shapes $(S_1 - R_2 \text{ and } S_2 - R_2)$ exhibit comparatively greater vertical incremental displacements than highly spherical aggregates $(S_2 - R_1 \text{ and } S_2 - R_2)$ or angular aggregates $(S_1 - R_1 \text{ and } S_2 - R_1)$. The median vertical displacements for $S_1 - R_1$, $S_1 - R_2$, $S_2 - R_1$, and $S_2 - R_2$ in breakable and unbreakable situations are around 0.38 mm, 1.74 mm, 0.50 mm, 1.96 mm, and 3.46 mm, 5.09 mm, 4.30 mm, 2.35 mm, respectively. This observation suggests that the utilization of ballast aggregates with higher sphericity and lower roundness can help mitigate the volumetric dilation of the assembly.



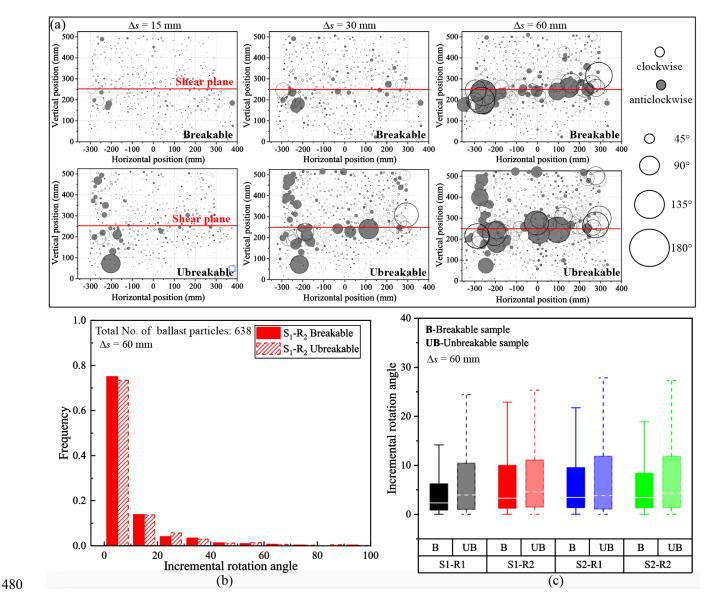
459 Fig. 14. (a) Profiles of particle vertical displacement during the shearing; (b) histogram of the

458

460 percentage of ballast particles with different vertical displacements for $S_1 - R_2$; (c) variations of the 461 vertical displacements for different particle groups under $\sigma_n = 75$ kPa

Fig. 15(a) shows the particle incremental rotation angle (relative to $\Delta_s = 0$ mm) for unbreakable 462 and breakable $S_1 - R_2$ at $\Delta_s = 15, 30, 60$ mm when under $\sigma_n = 75$ kPa. Each ballast particle is 463 represented by a circle whose size is proportional to the magnitude of its incremental rotation angle, 464 with transparent and black background colors denoting clockwise and anticlockwise rotation, 465 respectively. With the increase of Δ_s , the incremental rotation angles of the ballast particles steadily 466 rise, and a more profound particle rotation (> 90°) is observed within the shear plane area. The 467 incremental rotation of ballast particles is significantly reduced when breakage is allowed. When 468 469 subjected to shearing forces, particles in an assembly are prone to rolling over their surroundings, however, the climbing and the rotation distance are reduced and compensated because of the breaking 470 of sharp corners and edges that occurs at the local contacting area between two particles, resulting in a 471 472 smaller particle incremental rotation angle.

Fig. 15(b) shows the histogram depicting the percentage of ballast particles with different incremental rotation angles for the breakable and unbreakable $S_1 - R_2$ aggregates at $\Delta_s = 60$ mm under $\sigma_n = 75$ kPa. It is seen that more than 90% of the ballast particles have incremental rotation angles below 20°. Regarding the effect of particle shape, the box plot in Fig. 15(c) reveals that there is only a slight difference in particle rotation among aggregates with various shapes. The median incremental rotation angles for $S_1 - R_1$, $S_1 - R_2$, $S_2 - R_1$, and $S_2 - R_2$ in breakable and unbreakable groups are 2.34°, 3.27°, 3.42°, 3.46°, and 3.94°, 4.26°, 3.84°, 4.59°, respectively.



481 Fig. 15. (a) Profiles of particle incremental rotation; (b) histogram of the percentage of ballast particles 482 with different incremental rotation angles for $S_1 - R_2$; (c) variations of the incremental rotation angles 483 for different particle groups under $\sigma_n = 75$ kPa

It can be concluded that both particle shape and breakage influence the characteristics of particle motion during direct shearing, however, the breakage plays a more profound effect on the translational and rotational movement of ballast particles, which are significantly suppressed in all the breaking scenarios, consequently a smaller volumetric dilation is observed for breakable samples compared to their corresponding unbreakable ones.

489 **5.** Conclusions

This study has examined the shear behaviour of crushable granular materials with various shape sphericities and roundness by using the DEM simulations. The effect of irregular particle shapes on the shear response and the breakage behaviour of a granular assembly was investigated. Detailed microscopic characteristics in terms of anisotropy of internal structures and particle motion were then analysed. The main conclusions which could be drawn from this study are listed below:

495 1. An improved shear strength was observed in aggregates with lower sphericity and roundness as expected. However, the decrease in particle sphericity (<0.63) and roundness (<0.3) led 496 to an aggravation in particle breakage (hence compromised particle interlocking), which 497 hindered the development of shear strength while reducing the dilation of the granular 498 assembly. This indicates an inevitable trade-off between the shape irregularity and breakage 499 of the particles, and therefore, achieving an optimal balance between the role of shape 500 irregularity and the extent of particle degradation is crucial for enhancing the overall 501 mechanical performance of a granular assembly. 502

5032. When subjected to direct shearing, ballast aggregates experienced continuous grain504breakage, which mainly localized within an inclined band in the shear box. As shearing505developed, the breakage of particles was gradually concentrated along the shearing plane,506causing the width and the inclination angle of this breakage band to decrease to about507 $310~325 \text{ mm} (8.86~9.26d_{50})$ and $18^{\circ}~23.0^{\circ}$ towards the shearing plane, respectively.508These findings highlight the dynamic nature of particle breakage and its spatial distribution509during shearing.

- 32 -

510 3. The breakage of aggregates is further influenced by the particle shapes especially by the corner roundness. Owing to the extensive abrasion of particle corners with large curvatures, 511 the aggregates with lower roundness show an exacerbated particle breakage, indicated by a 512 513 wider breakage band $(11.14 \sim 12.86d_{50})$ and a greater inclination angle (23.0°) towards the end of shearing. These findings underscore the importance of considering the corner 514 angularity of particles, rather than just their overall morphologies, when selecting ballast 515 material for railroad construction to ensure optimal load-bearing performance. Moreover, 516 the authors believe this to be an important aspect of DEM modelling that cannot be 517 visualized by other means such as through experimental work. 518

4. At the peak state ($\Delta_s = 15 \text{ mm}$), the averaged inter-particle contact forces F_{ave} within 519 520 unbreakable assemblies were about 2.45~3.53 kN, with the corresponding anisotropy level |a| + |b| and the principal anisotropy orientation θ_a of inter-particle contacts being about 521 0.85~1.30 and 153.8°~165.5°, respectively. As a result of particle breakage, the F_{ave} 522 decreases to about 1.69~1.90 kN, accompanied by the values of |a| + |b| and θ_a 523 decreasing to 0.71~0.97 and 141.1°~150.0°, respectively. These results suggest beyond 524 doubt that the compromised shear strength of granular assemblies due to particle breakage 525 is primarily attributed to the weakening and less intensified inter-particle contact network 526 within the aggregates. 527

5. This study demonstrated that within a granular assembly, both the extent of breakage and shape irregularity influence the displacement of particles. For instance, when there is insignificant breakage, ballast particles experienced an averaged vertical displacement of about 2.35~5.09 mm and an averaged incremental rotation angle of 3.84°~4.59°. These values decreased to 0.38~1.96 mm and 2.34°~3.46°, respectively, for assemblies showing
notable breakage. These results highlight that the suppressed particle motion due to
breakage can be the primary cause for reduced volumetric dilation observed in the granular
assembly.

For future DEM studies, it is recommended to include more ballast breakage patterns, such as bulk splitting to ensure even a more realistic numerical model for ballast breakage behaviour under various shearing conditions. Furthermore, it is suggested to extend potential future work to more sophisticated 3D modeling, albeit substantially increased computational time and effort. This numerical advancement should offer a more realistic representation of particle shapes irregularities and sizes, and the corresponding particle interactions within the granular assembly, providing a more insightful study of ballast behaviour as a discrete medium.

543 **Declarations**

544 Data Availability

545 The data used to support the findings of this study are available from the corresponding author 546 upon request.

547 Conflicts of Interest

548 The authors all declare no conflict of interest.

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553 **References**

- Afshar, T., M. M. Disfani, A. Arulrajah, G. A. Narsilio, and S. Emam. 2017. "Impact of particle
 shape on breakage of recycled construction and demolition aggregates." *Powder Technology*,
 308: 1–12. https://doi.org/10.1016/j.powtec.2016.11.043.
- Alshibli, K. A., and M. I. Alsaleh. 2004. "Characterizing Surface Roughness and Shape of Sands
 Using Digital Microscopy." *J. Comput. Civ. Eng.*, 18 (1): 36–45.
 https://doi.org/10.1061/(ASCE)0887-3801(2004)18:1(36).
- Altuhafi, F. N., M. R. Coop, and V. N. Georgiannou. 2016. "Effect of Particle Shape on the
 Mechanical Behavior of Natural Sands." *Journal of Geotechnical and Geoenvironmental Engineering*, 142 (12): 04016071. American Society of Civil Engineers.
 https://doi.org/10.1061/(ASCE)GT.1943-5606.0001569.
- Bian, X., K. Shi, W. Li, X. Luo, E. Tutumluer, and Y. Chen. 2021. "Quantification of Railway
 Ballast Degradation by Abrasion Testing and Computer-Aided Morphology Analysis." J.
 Mater. Civ. Eng., 33 (1): 04020411. https://doi.org/10.1061/(ASCE)MT.1943-5533.0003519.
- Bono, J. P. D., and G. R. McDowell. 2016. "Investigating the effects of particle shape on normal
 compression and overconsolidation using DEM." *Granular Matter*, 18 (3): 55.
 https://doi.org/10.1007/s10035-016-0605-5.
- Chen, J., R. Gao, and Y. Liu. 2019. "Numerical Study of Particle Morphology Effect on the Angle of
 Repose for Coarse Assemblies Using DEM." *Advances in Materials Science and Engineering*, 2019: 1–15. https://doi.org/10.1155/2019/8095267.
- 573 Chen, J., J. S. Vinod, B. Indraratna, N. T. Ngo, R. Gao, and Y. Liu. 2022. "A discrete element study
 574 on the deformation and degradation of coal-fouled ballast." *Acta Geotech.*, 17 (9): 3977–
 575 3993. https://doi.org/10.1007/s11440-022-01453-4.
- 576 Chen, J., J. S. Vinod, B. Indraratna, T. Ngo, and Y. Liu. 2023. "DEM study on the dynamic responses
 577 of a ballasted track under moving loading." *Computers and Geotechnics*, 153: 105105.
 578 https://doi.org/10.1016/j.compgeo.2022.105105.
- 579 Cho, G. C., J. Dodds, and J. C. Santamarina. 2006. "Particle shape effects on packing density,
 580 stiffness, and strength: Natural and crushed sands." *J. Geotech. Geoenviron. Eng.*, 132 (5):
 581 591–602. https://doi.org/10.1061/(ASCE)1090-0241(2006)132:5(591).

Coetzee, C. J. 2016. "Calibration of the discrete element method and the effect of particle shape."
 Powder Technology, 297: 50–70. https://doi.org/10.1016/j.powtec.2016.04.003.

- Coop, M. R., K. K. Sorensen, T. B. Freitas, and G. Georgoutsos. 2004. "Particle breakage during
 shearing of a carbonate sand." *Géotechnique*, 54 (3): 157–163.
 https://doi.org/10.1680/geot.2004.54.3.157.
- Danesh, A., A. A. Mirghasemi, and M. Palassi. 2020. "Evaluation of particle shape on direct shear
 mechanical behavior of ballast assembly using discrete element method (DEM)."
- 589 *Transportation Geotechnics*, 23: 100357. https://doi.org/10.1016/j.trgeo.2020.100357.
- Ege, O., and I. Karaca. 2016. "Banach fixed point theorem for digital images." *J. Nonlinear Sci. Appl.*, 08 (03): 237–245. https://doi.org/10.22436/jnsa.008.03.08.
- 592 Gong, J., Z. Nie, Y. Zhu, Z. Liang, and X. Wang. 2019. "Exploring the effects of particle shape and

- content of fines on the shear behavior of sand-fines mixtures via the DEM." *Computers and Geotechnics*, 106: 161–176. https://doi.org/10.1016/j.compgeo.2018.10.021.
- Guo, Y., V. Markine, J. Song, and G. Jing. 2018. "Ballast degradation: Effect of particle size and
 shape using Los Angeles Abrasion test and image analysis." *Construction and Building Materials*, 169: 414–424. https://doi.org/10.1016/j.conbuildmat.2018.02.170.
- Guo, Y., J. Xie, Z. Fan, V. Markine, D. P. Connolly, and G. Jing. 2022. "Railway ballast material selection and evaluation: A review." *Construction and Building Materials*, 344: 128218.
 https://doi.org/10.1016/j.conbuildmat.2022.128218.
- Hamidian, A. H., E. J. Ozumchelouei, F. Feizi, C. Wu, Y. Zhang, and M. Yang. 2021. "A review on
 the characteristics of microplastics in wastewater treatment plants: A source for toxic
 chemicals." *Journal of Cleaner Production*, 295: 126480.
 https://doi.org/10.1016/j.jclepro.2021.126480.
- Indraratna, B., N. C. Tennakoon, S. S. Nimbalkar, and C. Rujikiatkamjorn. 2013. "Behaviour of clayfouled ballast under drained triaxial testing." *Géotechnique*, 63 (5): 410–419.
 https://doi.org/10.1680/geot.11.P.086.
- Indraratna, B., J. S. Vinod, and J. Lackenby. 2009. "Influence of particle breakage on the resilient
 modulus of railway ballast." *Geotechnique*, 59 (7): 643–646.
 https://doi.org/10.1680/geot.2008.T.005.
- Indraratna, B., L. S. S. Wijewardena, and A. S. Balasubramaniam. 1993. "Large-scale triaxial testing
 of grey wacke rockfill." *Géotechnique*, 43 (1): 37–51. ICE Publishing.
 https://doi.org/10.1680/geot.1993.43.1.37.
- Jing, G. Q., Y. M. Ji, W. L. Qiang, and R. Zhang. 2020. "Experimental and Numerical Study on
 Ballast Flakiness and Elongation Index by Direct Shear Test." *Int. J. Geomech.*, 20 (10):
 04020169. https://doi.org/10.1061/(ASCE)GM.1943-5622.0001791.
- Jo, S.-A., E.-K. Kim, G.-C. Cho, and S.-W. Lee. 2011. "Particle Shape and Crushing Effects on
 Direct Shear Behavior Using DEM." *Soils and Foundations*, 51 (4): 701–712.
 https://doi.org/10.3208/sandf.51.701.
- Ketterhagen, W. R., M. T. am Ende, and B. C. Hancock. 2009. "Process Modeling in the
 Pharmaceutical Industry using the Discrete Element Method." *Journal of Pharmaceutical Sciences*, 98 (2): 442–470. https://doi.org/10.1002/jps.21466.
- Li, Y. 2013. "Effects of particle shape and size distribution on the shear strength behavior of
 composite soils." *Bull Eng Geol Environ*, 72 (3): 371–381. https://doi.org/10.1007/s10064013-0482-7.
- Liu, F., M. Ying, G. Yuan, J. Wang, Z. Gao, and J. Ni. 2021a. "Particle shape effects on the cyclic
 shear behaviour of the soil–geogrid interface." *Geotextiles and Geomembranes*, 49 (4): 991–
 1003. https://doi.org/10.1016/j.geotexmem.2021.01.008.
- Liu, Q.-W., R.-P. Chen, H.-L. Wang, Z.-Y. Yin, and H.-N. Wu. 2022. "Effect of Particle Shape on
 Soil Arching in the Pile-Supported Embankment by 3D Discrete-Element Method
 Simulation." *International Journal of Geomechanics*, 22 (4): 04022027. American Society of
 Civil Engineers. https://doi.org/10.1061/(ASCE)GM.1943-5622.0002313.
- Liu, Y., R. Gao, and J. Chen. 2019. "Exploring the influence of sphericity on the mechanical
 behaviors of ballast particles subjected to direct shear." *Granular Matter*, 21 (4): 94.
 https://doi.org/10.1007/s10035-019-0943-1.
- Liu, Y., R. Gao, and J. Chen. 2021b. "A new DEM model to simulate the abrasion behavior of
 irregularly-shaped coarse granular aggregates." *Granular Matter*, 23 (3): 61.

638 https://doi.org/10.1007/s10035-021-01130-5. 639 Mcdowell, G. R. 2002. "On the Yielding and Plastic Compression of Sand." Soils and Foundations, 42 (1): 139–145. https://doi.org/10.3208/sandf.42.139. 640 Miao, C. X., J. J. Zheng, R. J. Zhang, and L. Cui. 2017. "DEM modeling of pullout behavior of 641 geogrid reinforced ballast: The effect of particle shape." Computers & Geotechnics, 81: 249-642 261. https://doi.org/10.1016/j.compgeo.2016.08.028. 643 Namjoo, A. M., M. Baniasadi, K. Jafari, S. Salam, M. Mohsen Toufigh, and V. Toufigh. 2022. 644 "Studying effects of interface surface roughness, mean particle size, and particle shape on the 645 shear behavior of sand-coated CFRP interface." Transportation Geotechnics, 37: 100841. 646 https://doi.org/10.1016/j.trgeo.2022.100841. 647 Nie, Z., M. Ashiru, X. Chen, and S. H. Mohamud. 2021. "Appraisal of Railway Ballast Degradation 648 649 Through Los Angeles Abrasion, Cyclic Loading Tests, and Image Technics." Advances in Geotechnical Engineering & Geoenvironmental Engineering, Sustainable Civil 650 651 Infrastructures, S. Shu, J. Wang, and M. Souliman, eds., 48-58. Cham: Springer International Publishing. 652 Nie, Z., C. Fang, J. Gong, and Z.-Y. Yin. 2020. "Exploring the effect of particle shape caused by 653 erosion on the shear behaviour of granular materials via the DEM." International Journal of 654 Solids and Structures, 202: 1–11. https://doi.org/10.1016/j.ijsolstr.2020.05.004. 655 Nuebel, K., and L. Rothenburg. 1996. "Particle Shape Effect in Stress-Force-Fabric Relationship for 656 657 Granular Media." Journal of the Mechanical Behavior of Materials, 7 (3): 219-233. De Gruyter. https://doi.org/10.1515/JMBM.1996.7.3.219. 658 Powers, M. C. 1953. "A New Roundness Scale for Sedimentary Particles." SEPM JSR, Vol. 23. 659 https://doi.org/10.1306/D4269567-2B26-11D7-8648000102C1865D. 660 Qian, Y., H. Boler, M. Moaveni, E. Tutumluer, Y. M. A. Hashash, and J. Ghaboussi. 2017. 661 "Degradation-Related Changes in Ballast Gradation and Aggregate Particle Morphology." J. 662 663 Geotech. Geoenviron. Eng., 143 (8): 04017032. https://doi.org/10.1061/(ASCE)GT.1943-5606.0001706. 664 Rui, S., Z. Guo, T. Si, and Y. Li. 2020. "Effect of particle shape on the liquefaction resistance of 665 calcareous sands." Soil Dynamics and Earthquake Engineering, 137: 106302. 666 https://doi.org/10.1016/j.soildyn.2020.106302. 667 Seyyedan, S. M., A. A. Mirghasemi, and S. Mohammadi. 2023. "DEM-XFEM Study of Particle 668 669 Shape Effect on Particle Breakage of Granular Materials." Geotech Geol Eng, 41 (5): 3115-3137. https://doi.org/10.1007/s10706-023-02448-y. 670 Sun, Q. D., B. Indraratna, and S. Nimbalkar. 2014. "Effect of cyclic loading frequency on the 671 permanent deformation and degradation of railway ballast." Géotechnique, 64 (9): 746-751. 672 https://doi.org/10.1680/geot.14.T.015. 673 Sun, Y., and C. Zheng. 2017. "Breakage and shape analysis of ballast aggregates with different size 674 distributions." Particuology, 35: 84-92. https://doi.org/10.1016/j.partic.2017.02.004. 675 676 Taghavi, R. 2011. "Automatic clump generation based on mid-surface." Continuum and Distinct Element Numerical Modeling in Geomechanics, 791–7. Melbourne, Australia. 677 Taiba, A. C., Y. Mahmoudi, M. Belkhatir, and T. Schanz. 2018. "Experimental Investigation into the 678 679 Influence of Roundness and Sphericity on the Undrained Shear Response of Silty Sand Soils." Geotechnical Testing Journal, 41. https://doi.org/10.1520/GTJ20170118. 680 Wadell, H. 1933. "Sphericity and Roundness of Rock Particles." Journal of Geology, 41 (3): 310-681 331. 682

- Wu, K., W. Sun, S. Liu, and G. Cai. 2021. "Influence of particle shape on the shear behavior of
 superellipsoids by discrete element method in 3D." *Advanced Powder Technology*, 32 (11):
 4017–4029. https://doi.org/10.1016/j.apt.2021.09.001.
- Ku, M. Q., N. Guo, and Z. X. Yang. 2021. "Particle shape effects on the shear behaviors of granular assemblies: irregularity and elongation." *Granular Matter*, 23 (2): 25.
 https://doi.org/10.1007/s10035-021-01096-4.
- Yang, J., and X. D. Luo. 2015. "Exploring the relationship between critical state and particle shape
 for granular materials." *Journal of the Mechanics and Physics of Solids*, 84: 196–213.
 https://doi.org/10.1016/j.jmps.2015.08.001.
- Yang, Y., J. F. Wang, and Y. M. Cheng. 2016. "Quantified evaluation of particle shape effects from
 micro-to-macro scales for non-convex grains." *Particuology*, 25: 23–35.
 https://doi.org/10.1016/j.partic.2015.01.008.
- Zhang, J., J. Qiao, K. Sun, and Z. Wang. 2022. "Balancing particle properties for practical lithium ion batteries." *Particuology*, 61: 18–29. https://doi.org/10.1016/j.partic.2021.05.006.
- Zhang, T., C. Zhang, J. Zou, B. Wang, F. Song, and W. Yang. 2020. "DEM exploration of the effect
 of particle shape on particle breakage in granular assemblies." *Computers and Geotechnics*,
 122: 103542. https://doi.org/10.1016/j.compgeo.2020.103542.
- Zhao, S., N. Zhang, X. Zhou, and L. Zhang. 2017. "Particle shape effects on fabric of granular random packing." *Powder Technology*, 310: 175–186.
 https://doi.org/10.1016/j.powtec.2016.12.094.
- Zheng, J., and R. D. Hryciw. 2015. "Traditional soil particle sphericity, roundness and surface
 roughness by computational geometry." *Géotechnique*, 65 (6): 494–506.
 https://doi.org/10.1680/geot.14.P.192.
- 706 Zingg, T. 1935. "Beitrag zur Schotteranalyse." ETH Zurich.

708

List of Figures and Tables

- Table 1: Micromechanical parameters used in the DEM analysis
- Fig. 1. (a) Images of five typical ballast particles; (b) CT scanning slices; and (c) created clumps used
- 712 in DEM simulations
- Fig. 2. (a) Diagrams of shape quantification for 4 typical particles; and (b) distribution histograms of
- 714 sphericity and roundness for 40 ballast particles
- 715 Fig. 3. Preparation of DEM model for direct shear test simulation
- Fig. 4. (a) Shear stress-strain responses obtained by DEM modeling and laboratory tests by (Indraratna
- et al. 2013) in triaxial testing; (b) the estimated BBI compared with the measured BBI by (Bian et al.
- 718 2021) and the B_g by (Nie et al. 2021) in LAA testing
- Fig. 5. The responses of shear stress and vertical displacement for (a) $S_1 R_1$; and (b) $S_1 R_2$
- Fig. 6. The responses of shear stress and vertical displacement for (a) $S_1 R_1$; and (b) $S_1 R_2$
- Fig. 7. The strength envelops of ballast aggregates from (a1 and a2) low- and high-sphericity group;
- and (b1 and b2) low- and high-roundness group
- Fig. 8. The distribution of ballast fragments in $S_1 R_2$ under $\sigma_n = 75$ kPa at Δ_s of (a) 15 mm; (b) 30
- 724 mm; (c) 45 mm; and (d) 60 mm
- Fig. 9. The evolution of (a) total volume of fragments V_f ; (b) breakage band width d_b ; and (c) breakage
- band inclination angle β_b of ballast aggregates with various shapes
- Fig. 10. The distributions of inter-particle contact in breakable and unbreakable $S_1 R_1$ at typical
- shearing displacements (i.e., $\Delta_s = 0, 15, 60 \text{ mm}$) under $\sigma_n = 75 \text{ kPa}$
- Fig. 11. The distributions of inter-particle contact in (a1-d1) unbreakable samples; and (a2-d2)
- 730 breakable samples at $\Delta_s = 15$ mm under $\sigma_n = 75$ kPa
- Fig. 12. The evolution of (a) anisotropy level |a| + |b|; and (b) principal anisotropy orientation θ_a for

- unbreakable and breakable $S_1 R_1$ sample at $\sigma_n = 75$ kPa
- Fig. 13. The rose diagrams of inter-particle contact forces for ballast aggregates with various shapes
- (a1-d1) before shearing; (a2-d2) unbreakable and (a3-d3) breakable samples at $\Delta_s = 15$ mm
- Fig. 14. (a) Profiles of particle vertical displacement during the shearing; (b) histogram of the
- percentage of ballast particles with different vertical displacements for $S_1 R_2$; (c) variations of the
- 737 vertical displacements for different particle groups under $\sigma_n = 75$ kPa
- Fig. 15. (a) Profiles of particle incremental rotation; (b) histogram of the percentage of ballast particles
- 739 with different incremental rotation angles for $S_1 R_2$; (c) variations of the incremental rotation angles
- 740 for different particle groups under $\sigma_n = 75$ kPa