

# Canadian Geotechnical Journal

### Shear Resistance Evolution of Geogrid-Aggregate Interfaces under Direct Shear: Insights from 3D DEM Simulations

Journal:	Canadian Geotechnical Journal			
Manuscript ID	cgj-2023-0531.R1			
Manuscript Type:	Article			
Date Submitted by the Author:	06-Jan-2024			
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Is the manuscript for consideration in a Special Issue or Collection?:	Not applicable (regular submission)			
Keyword:	geogrid, shear band, shear resistance, transverse rib, passive resistance			



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Abstract: This paper presents a mesoscopic evaluation of the shear resistance evolution of 18 19 geogrid-aggregate interfaces subjected to direct shear loading. A three-dimensional discrete 20 element method (DEM) model was developed based on experimental data. The tensile response 21 of geogrid were simulated through a series of calibration tests. Aggregate with complex particle 22 shapes were simulated to accurately capture the interlocking effect among aggregates based on 23 the real particle surface. The individual shear resistance components were quantified based on 24 particle displacement field and contact distribution characteristics. The influences of aperture-25 aggregate size ratio and geogrid stiffness on the shear resistance components are discussed. 26 The results indicate that the peak value of shear resistance component follows a descending order from frictional resistance of aggregate, to passive resistance of transverse rib, and to 27 28 geogrid-aggregate interface frictional resistance. During the shear process, the frictional 29 resistance of aggregate becomes active first, followed by the geogrid-aggregate interface 30 frictional resistance, and then the development of passive resistance of transverse ribs starts 31 with a certain lag. Optimizing the geogrid-aggregate size ratio and utilizing geogrids with 32 higher rib stiffness could enhance the passive resistance of transverse ribs but would not 33 significantly affect the geogrid-aggregate interface frictional resistance and frictional 34 resistance of aggregate.

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Keywords: geogrid, direct shear test, shear band, shear resistance, transverse rib, passive
resistance.

39 **Résumé** : Cet article présente une évaluation mésoscopique de l'évolution de la résistance au 40 cisaillement des interfaces géogrille-granulats soumises à une charge de cisaillement direct. Un modèle de méthode des éléments discrets (MED) tridimensionnel entièrement calibré a été 41 42 développé en se basant sur des données expérimentales. La réponse à la traction et le 43 comportement en déformation de la géogrille ont été simulés par le biais d'une série de tests de 44 calibration. Les granulats aux formes de particules complexes ont été simulés afin de capturer 45 avec précision l'effet d'interblocage entre les granulats basé sur la surface réelle des particules. 46 Les composantes individuelles de résistance au cisaillement ont été quantifiées en se basant sur 47 le champ de déplacement des particules et les caractéristiques de distribution des contacts. Les 48 influences du rapport de taille entre l'ouverture et les granulats ainsi que de la rigidité de la 49 géogrille sur les composantes de résistance au cisaillement sont discutées. Les résultats 50 indiquent que la valeur maximale de la composante de résistance au cisaillement suit un ordre 51 décroissant de la résistance au frottement des agrégats à la résistance passive des nervures 52 transversales, puis à la résistance au frottement de l'interface géogrille-agrégat. Au cours du 53 cisaillement, la résistance au frottement des agrégats s'active en premier, suivie de la résistance 54 au frottement de l'interface géogrille-agrégat, puis le développement de la résistance passive 55 des nervures transversales commence avec un certain retard. L'optimisation du rapport taille 56 des ouvertures/taille des agrégats et l'utilisation de géogrilles à nervures plus rigides pourraient 57 améliorer la résistance passive des nervures transversales, mais n'affecteraient pas de manière 58 significative la résistance au frottement de l'interface géogrille-agrégat et la résistance au 59 frottement des agrégats.

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Mots-clés : Géogrille, Essai de cisaillement direct, Bande de cisaillement, Résistance au
cisaillement, Nervure transversal, Résistance passive.

### 64 **1. Introduction**

Geogrids are widely used in various soil reinforcement projects in the field of geotechnical 65 66 engineering, providing feasible solutions to land utilization and structural stability issues (Jia 67 et al., 2021; Ke et al., 2021; Liu et al., 2007; Yang et al., 2012; Zhang et al., 2022). In the design of geogrid-reinforced soil structures, the shear behavior of geogrid-soil interfaces is a 68 crucial consideration, as it significantly influences the performance and stability of 69 geosynthetic reinforced soil (GRS) structures (Jewell et al., 1985). Hence, the interaction 70 71 mechanism between the geogrid and soil is of great significance in understanding the behavior 72 of GRS structures.

The characterization of geogrid-soil interfaces is vital in enhancing the understanding of 73 74 geogrid-soil interaction. Various testing approaches have been developed for this purpose, 75 including pull-out tests, direct shear tests, in-soil tensile tests, and ramp tests (Palmeira, 2009). Among them, pull-out tests and direct shear tests have been widely adopted to study the 76 conditions and broad applicability(Abdelrahman et al., 2008; Alfaro et al., 1995; Ezzein and 77 78 Bathurst, 2014; Liu et al., 2009b; Lopes and Ladeira, 1996). The interaction between the 79 geogrid and soil in pull-out tests is associated with interface frictional resistance and rib-80 bearing resistance (i.e., passive resistance of transverse ribs) of the geogrid. Previous studies 81 have been conducted for quantitative evaluations of the rib-bearing resistance of geogrids, 82 revealing that transverse ribs contribute approximately 75% to 90% of the total pull-out resistance (Cardile et al., 2017; Moraci and Gioffrè, 2006; Palmeira and Milligan, 1989). This 83 emphasizes the vital role of geogrid's transverse ribs in the shear resistance of the geogrid-soil 84

85 interface.

86 Nevertheless, few studies have focused on the quantitative evolution of individual shear resistance components at the geogrid-aggregate interface under direct shear conditions. Liu et 87 88 al. (2009a) conducted a series of direct shear tests on geogrid-soil interfaces, studying the 89 interaction at the geogrid-soil interface during direct shear, which comprises soil-soil frictional 90 resistance, geogrid surface-soil frictional resistance, and passive resistance of geogrid 91 transverse ribs. Presently, the evaluation of passive resistance of transverse ribs is primarily 92 based on a comparison of the peak shear strength between the reinforced and unreinforced 93 specimens, along with the ratio of the geogrid opening area to the area of the reinforced plane 94 (Jia et al., 2023; Liu et al., 2009a). However, the evolution of individual components 95 contributing to the total shear resistance during the shear process remains unclear, and there is 96 a need for investigating the evolution of passive resistance of transverse ribs during the 97 shearing process. Consequently, the interaction mechanism of geogrid and aggregates in the 98 direct shear mode has not been fully revealed, necessitating a mesoscopic perspective to 99 comprehend the interface interaction and clarify the underlying reinforcement mechanism. 100 Most experimental studies have focused on the macroscopic mechanism of geogrid-soil 101 interaction (Ferreira et al., 2015; Liu et al., 2016; Sweta and Hussaini, 2018; Wang et al., 2019). 102 However, the factors influencing the interaction between the geogrid ribs and soil particles can 103 be divided into two categories (Zhou et al., 2012). One is related to the micro behavior of the

104 soil and the geogrid, including grain size, particle shape of soil, and local deformation of the

105 geogrid. The other relates to macro boundary conditions, specimen size, and stress state. While

106 experimental studies have provided significant insights, most conventional testing methods 107 have limitations in revealing microscale interactions at the geogrid-aggregate interface, such 108 as interlocking and contact force evolution between individual aggregates. Although non-109 intrusive measurements, such as high-resolution digital cameras (Abdi and Mirzaeifar, 2017; 110 Zhou et al., 2012) and transparent soil laser-assisted imaging (Peng and Zornberg, 2019), have 111 been adopted in laboratory to study the micro-mechanisms interaction between the geogrid and aggregates, the results are limited to capturing deformation patterns. Quantifying and tracking 112 113 the geogrid-aggregates interlocking behavior and the evolution of individual shear resistance 114 components during the shear process remains challenging. Therefore, it is necessary to utilize 115 the Discrete Element Method (DEM) to simulate and track the interaction between the geogrid 116 and soil particles from a micromechanical perspective.

117 DEM has been widely used to investigate the meso-scale behavior, such as interlocking 118 and sliding between soil particles, in studies on soil-structure interface behavior (Chen et al., 119 2018; Grabowski et al., 2021; Jia et al., 2023; McDowell et al., 2006; Miao et al., 2020; Ngo 120 et al., 2014; Wang et al., 2022; Wang and Yin, 2022). Previous research has indicated two 121 crucial factors that should not be overlooked in the interaction of geogrid-soil interfaces: the 122 particle shape of aggregates (Ferellec and McDowell, 2010; Gao and Meguid, 2018; Miao et 123 al., 2017; Stahl et al., 2014; Tutumluer et al., 2012; Zhou et al., 2018), which directly affects 124 the relative movement and rotation of particles, and the flexural stiffness of geogrid (Feng and Wang, 2023; Ferellec and McDowell, 2012; Jia et al., 2023), which directly influences the 125 deformation mode of geogrid. Therefore, accurately reproducing the particle shape of soils and 126

127 the local deformation response of geogrids is crucial in numerical simulations.

128 In this study, direct shear tests are conducted on the geogrid-aggregate interfaces and the 129 corresponding DEM models are developed to quantitatively evaluate the evolution of 130 individual shear resistance components subjected to direct shear loading. The influences of 131 aggregate shape and geogrid flexural stiffness are considered. The passive resistance of 132 transverse ribs is quantified based on the distribution of shear bands and the evolution of contact forces. The results of this study provide a better understanding of the interaction 133 134 mechanism between the geogrid and aggregates from a meso-mechanical perspective, which is 135 of significance for the design of GRS structures.

136

### 137 **2. DEM Model and Parameter Calibration**

The DEM model of geogrid-aggregate interface shear was developed using PFC3D. DEM modeling procedures of geogrid and aggregate are introduced, and the corresponding calibration of parameters is established based on the experimental results.

### 141 **2.1 Geogrid**

The present study employed a typical polypropylene biaxial geogrid as a reinforcement. This geogrid has an average joint thickness of 5.0 mm and rib thickness of 3.5 mm. The centerto-center distance between two adjacent joints is 40 mm, and the width of the geogrid ribs varies from 8 mm to 4 mm between these joints. The geometric characteristics of geogrid were simulated in the DEM model using bonded sphere strings, with particle sizes ranging from 1.5 mm to 3 mm. The contact between the spheres was governed by the linear parallel bond contact 148 model, which allows for the transmission of bending and tensile forces. This contact model has 149 also been extensively utilized to simulate the tensile behavior of geogrids accurately (Chen et 150 al., 2012; Feng and Wang, 2023; Ferellec and McDowell, 2012; Ngo et al., 2014; Stahl et al., 151 2014). For per timestep, the increment of normal and tangential forces  $\Delta F_{n,s}$ , bending moments 152  $\Delta M_b$ , and twisting moments  $\Delta M_t$  within the parallel bond can be mathematically described as 153 follows:

154 
$$\Delta \bar{F}_{n,s} = \bar{A} \Delta U_{n,s} \bar{k}_{n,s}$$
(1)

155 
$$\overline{\Delta M}_b = I \Delta \Theta_b \overline{k}_n \tag{2}$$

156 
$$\overline{\Delta M}_t = J \Delta \Theta_t \overline{k}_s \tag{3}$$

157 Where,  $\Delta U_{n,s}$ ,  $\Delta \theta_b$ , and  $\Delta \theta_t$  are the increment of relative normal and shear displacement, the 158 increment of relative bend rotation, and the increment of relative twist rotation, respectively; 159  $\bar{k}_{n,s}$  is the normal and shear stiffness of parallel bond;  $\bar{A}$ , I and J are the parallel bond cross-160 section area, the moment of inertia of the parallel bond cross section and the polar moment of 161 inertia of the parallel bond cross-section, respectively, which are calculated as:

162 
$$\overline{A} = \overline{nR^2}$$
 (4)

$$I = \frac{1}{4} \Pi R^4 \tag{5}$$

$$J = \frac{1}{2} \Pi R^4 \tag{6}$$

165 where  $\overline{R} = \min(R_1, R_2)$  is the radius of the smaller of the two pieces in contact with each other. 166 The effective modulus  $\overline{E}^*$  and stiffness ratio  $\overline{K}^*$  of parallel bond, as input parameters related 167 to Young's modulus (tension) and Poisson's ratio, can be calculated by the following formula: 168  $\overline{E}^* = \overline{k_n}L$  (7)

169 
$$\boldsymbol{\kappa}^* = \frac{k_n^-}{\bar{k}_s} \tag{8}$$

170 where  $L = R_1 + R_2$  is the contact length, which can be represented as the sum of the radius of 171 two pieces in contact with each other.

172 The calibration of contact parameters for tensile properties primarily relies on the experimental results of single rib tensile tests. As shown in Fig. 1, tensile tests were conducted 173 along both the machine direction (MD) and the cross-machine direction (CMD) of the geogrid. 174 175 In general, the tensile test results from the experiments and simulations are in good agreement 176 for both the MD and CMD. During the direct shear test of geogrid-aggregate interfaces, the 177 local strain of geogrid with typical stiffness did not exceed 5% (Jia et al., 2023). Within this 178 range of strain, the stress-strain relationship of the geogrid used in this study is nearly linear. 179 For the subsequent simulations, high values were assigned to the normal and shear strength of 180 the parallel bond to prevent failure (i.e., rupture), as this study primarily focuses on the 181 interlocking behavior between the geogrid and aggregates under typical normal stresses. 182 Overall, the numerical simulation results are in good agreement with the experimental results. 183 To replicate the deformation mode of geogrid in the numerical simulations accurately, it 184 is crucial to consider the aperture stability and bending resistance of geogrid. The two-aperture 185 extension tests were conducted, as shown in Fig. 2, to calibrate the deformation behavior of 186 geogrid model. The observed deformations of geogrid include upward buckling of the middle 187 transverse rib, tension, and outward rotation of the longitudinal ribs on both sides. To quantify 188 these deformations, the flexible buckling height  $(h_f)$  of the middle section of the transverse rib 189 and the distance, d, between the two joints connecting the transverse rib were measured. With

a tensile force  $F_t = 0.25$  kN, the test yielded  $h_f/d = 2.16$ . In Fig. 2 (b), the distribution of contact tension within the numerical model produces the value of  $h_f/d = 2.07$ , which demonstrates an excellent agreement with the experimental results. Consequently, the model parameters employed in this study can effectively capture the tensile response and deformation behavior of geogrid. Table 1 provides an overview of the calibrated geogrid model parameters.

### 195 **2.2 Aggregate**

196 The tests in this study utilized limestone as the aggregate, which possesses angular 197 characteristics. The comparison of particle size distribution of the gravel from the experiments 198 and DEM simulations is presented in Fig. 3(a). Previous experimental and simulation studies 199 have demonstrated that particle shape significantly influences the interlocking among particles 200 (Liu et al., 2021; Wang et al., 2021; Ying et al., 2021; Zhou et al., 2018). In the DEM 201 simulations, an aggregate modeling method based on the real particle surface was employed to 202 accurately capture the interlocking effect among aggregates. The aggregate model employs 203 overlapping spheres to replicate the shape of actual irregular particles using 'clump' logic 204 (Ferellec and McDowell, 2010; Ferellec and McDowell, 2012). The surface of a real particle 205 is first captured as a cloud of points in 3D space using scanning techniques. Spheres are then 206 grown from random points on this surface, expanding normally to the maximum extent possible 207 inside the particle volume without penetrating the surface boundary. Each sphere expands as 208 much as possible to fill the interior volume. The more spheres used, the better the resolution of 209 the particle shape. This allows complex realistic particle shapes to be generated for DEM 210 simulations by filling the scanned volume with optimized overlapping spheres, which helps to

211 mimic the actual particle shape. It should be noted that the aggregate model in this study cannot 212 simulate particle breakage. The normal and shear stresses involved in this study are much 213 smaller than the breakage strength of limestone (typically greater than 5 MPa) (Feng et al., 214 2022; Wang et al., 2023). Therefore, the influence of particle breakage is ignored in this study. 215 To ensure accurate particle dynamics and prevent incorrect inertia caused by uneven mass 216 distribution due to sphere overlap, this study utilizes a calculation method that assumes a 217 homogeneous polyhedron. The centroid and inertia tensor of the polyhedron are computed 218 accordingly (Mirtich, 1996). The linear contact model in DEM was adopted for the contact 219 between particles. This model is widely used in simulating cohesionless materials and has been proven to be highly reliable in capturing their behavior (McDowell et al., 2006; Ngo et al., 220 2014; Stahl et al., 2014; Wang et al., 2022; Wang et al., 2014; Zhou et al., 2018). The linear 221 222 contact model is dominated by a linear-elastic spring contact law. The incremental normal and 223 shear contact force,  $\Delta F_{ns}$ , and friction strength update can be calculated as:

$$\Delta F_{n,s} = \Delta U_{n,s} k_{n,s} \tag{9}$$

225

$$F_s = \mu F_n \tag{10}$$

where  $\Delta U_{n,s}$  is the incremental normal and shear displacement;  $k_{n,s}$  is the normal and shear stiffness;  $\mu$  is the interparticle friction coefficient. The effective modulus  $E^*$  and stiffness ratio  $K^*$  of linear contact can be calculated:

$$E^* = \frac{k_n L}{\Pi R_{\min}^2}$$
(11)

$$\kappa^* = \frac{k_n}{k_s} \tag{12}$$

where L and  $R_{\min}$  are the contact length and the smaller radius of the two pieces in contact, respectively.

Furthermore, to ensure computational efficiency, the influence of particle shape is assessed based on the peak shear strength observed in the direct shear test (detailed information on the direct shear test process is provided later). The approximation effect of particle shape is quantitatively evaluated using a volume error,  $E_V$ , which can be expressed as follows (Katagiri, 2019):

$$E_V = \frac{\left|V_S - V_C\right|}{V_S} \tag{13}$$

where  $V_S$  represents the volume of the closed three-dimensional polyhedron representing the particle surface, and  $V_C$  represents the volume of the clump particle.

Fig. 3(b) compares the simulation results and the direct shear test results for four different types of particles, each characterized by a different volume error ( $E_{Vi}$ ). To balance the computational efficiency and accuracy, the volume error selected for the aggregate particles in this study is  $E_{V3} = 0.087$ .

Fig. 4 shows the direct shear test results for aggregates obtained from the experiments and the DEM simulations. The comparison between these results demonstrates a reasonable agreement, indicating that the DEM model can capture the evolution of shear strength of the aggregate. This agreement further validates the accuracy and reliability of the DEM model. The calibrated parameters of the aggregates adopted in the current DEM analysis are summarized in Table 2.

### 251 **2.3 Geogrid-aggregate interface direct shear tests**

252 The direct shear test apparatus is presented in Fig. 5. It consists of upper and lower shear 253 boxes constructed from steel plates, providing rigid boundary conditions. The upper and lower 254 shear boxes both have a height of H = 200 mm and a width of W = 300 mm. The length of the 255 upper shear box along the shear direction is L=300 mm, while the length of the lower shear 256 box is  $L_l = 360$  mm. The larger area of the lower shear box can ensure a constant contact area during the shearing process. A vertical actuator was connected to the top of the upper shear 257 258 box to apply constant normal stress. A horizontal actuator was utilized to apply shear stress on 259 the lower shear box at a constant rate. The geogrid specimen was fixed to the front edge of the 260 lower shear box using clamping blocks and bolts. The longitudinal rib of the geogrid aligned 261 with the shear direction, while the transverse rib was perpendicular to the shear direction. 262 According to ASTM D 5321, the geogrid extended with a sufficient distance along the relative 263 movement direction of the upper shear box to enable clamping to the lower shear box. During specimen preparation, the weight of soil in both the upper and lower shear boxes was carefully 264 265 controlled to ensure a consistent compacted soil density of  $\rho_c = 1600.5 \text{ kg/m}^3$ . A constant shear rate of  $v_s = 1$  mm/min was applied to the lower shear box until the shear displacement reached 266 267 30 mm. Tests were conducted under four different normal stresses of  $\sigma_n = 50$  kPa, 100 kPa, 150 kPa, and 200 kPa. 268

Fig. 6 shows the DEM model of the direct shear test. The upper and lower shear boxes were constructed with rigid friction-free walls, providing appropriate boundary conditions. The initial dimensions of the simulated shear boxes aligned with those of the laboratory tests, while

272 the initial height  $(H_{ini})$  was set to 400 mm to ensure an adequate number of particles generated 273 within the shear box and compacted to achieve the target density. Through iterative adjustments, 274 it was determined that setting the initial porosity to 0.55 yielded an aggregate particle height 275 (H) after final compaction that closely matched the experimental conditions. The geogrid 276 model, as shown in Fig. 6(a), was implemented to maintain the alignment of longitudinal ribs 277 along the shear direction. The geogrid particles were clamped and securely affixed to the lower shear box. Subsequently, a constant target normal stress was applied to the top of the shear box. 278 279 Finally, a constant shear rate was applied to the lower shear box. 280 The linear contact model was employed to simulate the interaction between the geogrid 281 and aggregate particles. Fig. 7 shows the comparison between the results of experiments and 282 DEM simulations. Before reaching the peak shear stress, the DEM simulations display a higher 283 stiffness compared to the experimental data. This discrepancy could be attributed to the 284 difference in the specimen preparation technique. Previous studies have highlighted that 285 uniformly compacted DEM specimens often exhibit non-physical load-deformation response 286 at low strain levels, which could explain the stiffer response before attaining the peak stress in 287 the DEM simulations (Feng et al., 2018; Thornton, 2000). Moreover, the disparity in post-peak 288 strength between the DEM simulations and experiments under the normal stress  $\sigma_n = 200$  kPa 289 could be due to the localized instability. The local instability of the specimen can be attributed 290 to the relative slip and rotation of coarse particles during the shearing process, which can result in the failure and reconstruction of inter-particle interlocking. In general, the DEM simulation 291 results agree with the experimental results. It indicates that the DEM model developed in this 292

study can effectively capture the nonlinear development of shear stress with increasing shear displacement and accurately represent the shear behavior of geogrid-aggregate interfaces. The calibrated parameters of geogrid-aggregate interface in the DEM simulations are summarized in Table 3.

297

**3. Results and Discussions** 

#### 299 **3.1 Interface shear resistance**

300 A dimensionless parameter, known as the shear strength coefficient, a, is employed to 301 quantify the reinforcement effect of geogrid-aggregate interfaces (Liu et al., 2009a; Tatlisoz et 302 al., 1998). The value a is determined as follows:

$$a = \frac{T_{s-g}}{T_s}$$
(14)

where  $\tau_{s-g}$  and  $\tau_s$  represent the peak shear strengths of the geogrid-aggregate interface and the unreinforced aggregates, respectively. Fig. 8(a) shows the comparison of the shear strength coefficient (*a*) obtained from the experiments and DEM simulations. The experimental and simulated values of *a* are greater than 1.0 and generally close to each other. This indicates that the geogrid can effectively enhance the shear strength of aggregates and further validate the effectiveness of the DEM model.

Fig. 8(b) presents the corresponding shear displacements at the peak shear strength obtained from the direct shear tests. The shaded area illustrates the difference between the corresponding shear displacements of reinforced and unreinforced specimens. Both the experimental and simulated results consistently demonstrate that the shear displacements at the 314 geogrid-aggregate interfaces are significantly larger than those of the unreinforced specimens 315 when the shear stress reaches the peak value. Previous studies have attempted to develop 316 quantitative evaluation methods for individual shear resistance components (Jia et al., 2023; 317 Liu et al., 2009a; Liu et al., 2009b). One such approximate method, proposed by Liu et al. 318 (2009a), involves allocating the total peak shear resistance based on the ratio of the surface 319 area of the geogrid to the total shear plane, and the ratio of the opening area of the geogrid to 320 the total shear plane. This assumes that the peak values of each resistance component occur 321 simultaneously. However, the data presented in Fig. 8(b) indicates that the peak values of each 322 component of the geogrid-aggregate interface shear resistance may not be synchronized. For 323 instance, the differences in shear displacement mobilized at peak shear stress between the 324 reinforced and unreinforced specimens under 50 kPa normal stress obtained from experiment 325 and DEM simulation were approximately 6.5 mm and 6.3 mm, respectively. This indicates that 326 the different shear resistance components may have different mechanisms for the mobilization 327 of shear strength. Hence, it becomes crucial to accurately quantify the evolution process of 328 each shear resistance component, especially the passive resistance provided by the transverse 329 ribs, to investigate the reinforcement mechanism of geogrid-aggregate interfaces.

**330 3.2** *Individual shear resistance components* 

As shown in Fig. 9, the total shear resistance of the geogrid-aggregate interface can be divided into three components: (i) internal frictional resistance,  $FR_s$ , which originates from the internal friction provided by the contact among the particles within the aperture. (ii) geogridaggregate interface frictional resistance,  $FR_{gs}$ , which arises from the frictional resistance

#### Canadian Geotechnical Journal

between the geogrid surface and particles. (iii) passive resistance,  $PR_g$ , which is attributed to the resistance exerted on the inner side of the transverse ribs resulting from the transverse ribaggregate interaction.

338 The interaction between the geogrid and aggregates at the geogrid-aggregate interface can 339 be better understood from a meso-perspective by examining the contact force distribution. As 340 an example, for the simulation with normal stress  $\sigma_n = 50$  kPa, Fig. 10 presents the contact force distribution around a representative geogrid aperture, simulated at different shear 341 342 displacements. The ribs of geogrid serve as tension members, experiencing internal tensile 343 contact forces (geogrid-geogrid contacts). Conversely, the aggregate-geogrid contacts and 344 aggregate-aggregate contacts are characterized by pressure-bearing contacts. These contacts 345 collectively form a force transmission network known as the contact force chains. As the shear 346 displacement increases, the contact directions adjust accordingly to adapt to the new stress conditions. The passive resistance provided by geogrid ribs can be explained from a meso-347 348 perspective as follows: a portion of the aggregates is trapped within the aperture and exerts 349 forces on the inner side of the ribs through contacts. The transverse ribs of geogrid actively 350 resist the relative movement of aggregates along the shear direction, thereby influencing the 351 displacement and contact state of particles. The interaction between the geogrid and aggregates 352 involves a complex mechanism, including the relative motion of particles, the evolution of 353 contact directions, and contact forces. The contribution of each shear resistance component to the total shear strength and its evolution by considering the relative movement and contact 354 355 evolution of particles will be elaborated in the following sections.

#### 356 **3.3 Geogrid deformations**

357 Fig. 11 presents the comparison of geogrid deformations between the experiment and 358 DEM simulation under the normal stress of  $\sigma_n = 50$  kPa. Both the experiment and DEM 359 simulation reveal similar deformation patterns: the longitudinal ribs along the shear direction 360 have minimal bending deformations, while the transverse ribs (perpendicular to the shear 361 direction) exhibit obvious flexible bending deformations, which emphasizes the crucial role of passive bearing resistance of transverse ribs in direct shear tests. The consistency between the 362 experimental and simulated deformations further validates the effectiveness of DEM model. It 363 364 is important to note that the geogrid deformations observed in the experiment from Fig. 11(a) 365 may be slightly smaller than the actual geogrid deformations after shear. This discrepancy arises because the shear force and the upper shear box were removed before taking the photo 366 367 for observation, leading to partial recovery of the elastic deformations of geogrid. Fig. 11(b) 368 also shows slices of aggregate particles at the interface after direct shear. A prominent 369 observation is that the aggregate particles subjected to shear at the geogrid-aggregate interface 370 consistently tend to move along the shear direction. The restraining effect of geogrid on the 371 aggregate particles primarily manifests in the particles being obstructed in front of the 372 transverse ribs.

#### 373 **3.4 Shear band**

In the direct shear tests of geogrid-aggregate interfaces, the shear plane is located along the upper surface of the geogrid. Consequently, the deformation primarily occurs within a narrow region known as the shear band near the geogrid surface. Identifying the shear band of 377 the geogrid-aggregate interface and quantifying its thickness based on particle kinematics can 378 aid in determining the interaction region. Fig. 12(a) presents the horizontal displacements of 379 the aggregates under normal stress of  $\sigma_n = 50$  kPa (negative values denoting displacements 380 along the shear direction). Jing et al. (2018) proposed a method to quantitatively assess the 381 thickness of the local shear band by utilizing the inflection point of the  $\delta_x$ -d curve, where  $\delta_x$ 382 and d are the displacement of aggregates in the x-axis direction and the depth of aggregate particles, respectively. To determine the thickness of the shear bands, the average displacement 383 384 component of particles in the shear direction (x-axis) is first calculated by averaging the 385 displacement field. Subsequently, a smooth curve f(d) is obtained through spline interpolation, 386 representing the relationship between the displacement in the x-axis direction ( $\delta_x$ ) and the thickness of the local zone. The first derivative f'(d) and the second derivative f''(d) are then 387 388 computed using the finite difference method. Finally, the curvature  $\kappa$  can be calculated as 389 follows:

390 
$$K = \frac{|f'(d)|}{(1+f'(d)^2)^{3/2}}$$
(15)

As suggested by Jing et al. (2018), the curvature  $\kappa = 0.02$  can be employed as the criterion to define the boundary of the local shear band. In direct shear tests, the two boundaries of the shear band are above and below the geogrid layer located in the upper and lower shear boxes, respectively. The thickness of the upper and lower shear bands can be defined as the distance from the corresponding boundary (upper or lower) of the shear band to the upper surface of the geogrid. Fig. 12(a) shows that the thickness of the upper shear band is significantly thicker than that of the lower shear band. For instance, at a normal stress of  $\sigma_n = 50$  kPa, the thickness of 398 the upper shear band is 42.6 mm, while the thickness of the lower shear band is 15.1 mm. This 399 indicates that the relative motion of particles within the upper shear band is more pronounced. This can be attributed to two main factors: Firstly, the servo normal stress is achieved through 400 401 displacement control by the actuator placed at the top of the upper shear box. As a result, if 402 there is a tendency for shear expansion at the interface, this servo mechanism enables the 403 particles to move upward rather than downward; Secondly, the shear interface is located on the upper surface of the geogrid rather than the lower surface, which influences the intensity of 404 particle motion within the shear band. Similar observations were also reported by Feng and 405 406 Wang (2023).

407 Fig. 12(b) displays the variations in shear band thickness under different normal stresses. In general, as the normal stress increases, the boundaries of both the upper and lower shear 408 409 bands move downward, while the total thickness of the shear band (the sum of the thicknesses 410 of the upper and lower shear bands) remains near constant at approximately  $3.4D_{50}$  ( $D_{50}$  is the 411 average particle size). This observation indicates that higher normal stress prevents the upward 412 expansion of the shear zone but promotes its downward progression. Several studies have also 413 demonstrated that under higher normal stresses, aggregate particles tend to be tightly 414 compressed and interlocked, resulting in less macroscopic volume dilatancy (Ferreira et al., 415 2015; Wang et al., 2021).

416 **3.5 Contact force distribution** 

417 The distribution of contact forces between particles can provide insights into the load 418 transfer mechanism at the geogrid-aggregate interface. In this study, the shear direction is 419 defined as the negative direction along the *x*-axis, indicating that the shear resistance acts in 420 the *x*-axis direction, while the vertical normal stress is defined as the negative direction along 421 the *z*-axis. Thus, the contact forces can be projected onto the *x*-*o*-*z* plane to quantify the 422 distribution. Rothenburg and Bathurst (1989) proved that the distribution of the contact normal 423  $C(\theta)$  and the normal contact force  $f(\theta)$  between particles can be approximated using second-424 order Fourier series:

425 
$$C(\boldsymbol{\theta}) = \frac{1}{2\pi} \begin{bmatrix} 1+a \cos 2(\boldsymbol{\theta}-\boldsymbol{\theta}) \end{bmatrix}$$
(16)

426 
$$f(\boldsymbol{\theta}) = f_0[1 + a_n \cos 2(\boldsymbol{\theta} - \boldsymbol{\theta}_n)]$$
(17)

where  $a_c$  and  $a_n$  are the anisotropy coefficients of the contact normal and normal contact forces, 427 respectively;  $\theta_c$  and  $\theta_n$  are the principal directions of contact normal and normal contact force 428 distribution, respectively;  $f_0$  is the average normal contact force. Fig. 13(a) presents the contact 429 430 force distribution in the geogrid-aggregate interface shear specimen at the peak shear stress under  $\sigma_n = 50$  kPa. The thickness of lines represents the magnitude of force chains. Some 431 432 localized voids in the force chains near the transverse rib of geogrid indicate that the relative 433 motion of particles caused by shear is influenced by the transverse rib. The sparseness of force 434 chains at the end of the upper shear box (away from the clamped end of geogrid) indicates a local reduction in normal stress, which is consistent with the results reported by Teixeira et al. 435 436 (2007). Furthermore, the direction of contact force in the upper shear band exhibits the most pronounced deflection. To further analyze the contact forces in this region, the normal and 437 438 tangential contact forces between aggregates are counted and analyzed using Fourier series approximation (FSA) fitting. Fig. 13(b) and 13(c) show the FSA fitting results for the contact 439

440 normal and normal contact forces, respectively. The principal direction of the contact normal describes the relative position information of particles, while the principal direction of the 441 442 normal contact force distribution describes the primary load information borne by the current 443 force chain of microstructure. The principal direction of the contact normal is  $\theta_c = 35^\circ$ , and the principal direction of the normal contact force distribution is  $\theta_n = 48^\circ$ . Additionally, the angle 444 445 between the normal contact direction and the shear direction is represented as  $a_c = \pi/2 - \theta_c$ , which can be used to determine whether the contact contributes to the passive resistance of 446 transverse ribs. 447 448 Fig. 14 shows the variations of  $\theta_c$  and  $\theta_n$  for specimens captured at the peak shear stress under different normal stresses. The trend of  $\theta_c$  and  $\theta_n$  changing with normal stress is consistent. 449 The principal directions of contact normal fluctuate between 35° and 37°. The principal 450

directions of the normal contact force are always greater than those of the contact normal,
ranging between 48° and 53°.

453

454

# 4. Determination of Individual Shear Resistance Components

Based on the previous analysis, the contact between the geogrid and aggregates, contributing to the passive resistance of transverse ribs, must satisfy two conditions: One is that the contact point should be between the transverse rib and aggregate particle; the other is that the contact position should be located at the inner edge of the transverse rib, and the angle between the projection of the contact normal direction (from the geogrid to the aggregate particles) in the *x-o-z* plane and the shear direction should be less than  $a_c$ , as shown in Fig. 15. 461 Once these contacts are identified, the passive resistance of transverse ribs,  $PR_g$ , during 462 shearing can be calculated as:

463

$$PR_{g} = -\sum_{a_{IR} \le a_{c}} f_{x}^{(gt-s)}$$
(18)

464 where  $f_{gt-s}$  is the x-direction component of the contact force for transverse rib-aggregate 465 contact. By subtracting the passive resistance of transverse ribs from the total geogrid 466 resistance, the geogrid-aggregate interface frictional resistance (*FR*<sub>gs</sub>) on the geogrid-aggregate 467 interface can be determined:

468

$$FR_{gs} = \sum f_{xi} - PR_g \tag{19}$$

469 where  $f_x$  represents the component of the contact force in the x-direction between the clamped 470 part of the geogrid and the rest of the geogrid, as shown in Fig. 15(b). Then, the internal 471 frictional resistance of aggregates  $(FR_s)$  is determined by subtracting the total geogrid 472 resistance from the total shear resistance. Moreover, quantifying the various shear resistance components at the geogrid-aggregate interface make it possible to gain insights into the 473 evolutions of individual components. This provides a comprehensive understanding of the 474 475 interaction between the geogrid and aggregates, shedding light on the reinforcement 476 mechanism.

Fig. 16 presents the evolution of shear resistance components as shear displacement progresses under different normal stresses. The peak value of each shear resistance component follows a descending order from frictional resistance of aggregate ( $FR_s$ ), to passive resistance of transverse ribs ( $PR_{gs}$ ), and to geogrid-aggregate interface frictional resistance ( $FR_{gs}$ ). During the shear process, with increasing shear displacement, the first occurrence of peak shear resistance corresponds to the geogrid-aggregate interface frictional resistance, followed by the

483 frictional resistance of aggregate, and the passive resistance of transverse ribs.

484 Take the specimen under  $\sigma_n = 50$  kPa as an example to elucidate the evolution process of 485 each shear resistance component, as shown in Fig. 16(a). Initially, the frictional resistance 486 between aggregates becomes active, succeeded by the geogrid-aggregate interface frictional 487 resistance. However, the development of passive resistance of transverse ribs exhibits a certain lag, particularly during the early stages of shear. Similar trends are observed under different 488 489 normal stresses. Additionally, each shear resistance component significantly increases with the 490 increase of normal stress. For instance, under normal stresses of  $\sigma_n = 50$  kPa, 100 kPa, 150 kPa, and 200 kPa, the peak values of the passive resistance of transverse ribs are 1.72 kN, 2.01 491 492 kN, 2.63 kN, and 3.31 kN, respectively. Notably, the frictional resistance of aggregate 493 component demonstrates the most substantial increase as the normal stress increases, as the 494 soil strength significantly depends on the normal stress for granular soils.

495 Fig. 17 shows the evolution of the contribution (i.e., the proportion concerning the total 496 shear resistance) of each shear resistance component, represented by  $C_{PRG}$ ,  $C_{FRG}$ , and  $C_{FRS}$ , 497 which denote the contribution of passive resistance of transverse ribs, geogrid-aggregate interface frictional resistance, and frictional resistance of aggregates, respectively. Based on 498 499 the peak total shear stress, the shear displacement is divided into two stages: pre-peak and post-500 peak. Prior to reaching the peak total shear stress, the contribution of passive resistance of transverse ribs continues to increase, while the contribution of frictional resistance of aggregate 501 fluctuates and decreases. The contribution of geogrid-aggregate interface frictional resistance 502

503 initially increases and subsequently decreases. Interestingly, during the initial shear stage, the 504 contribution of transverse rib passive resistance is lower than that of the geogrid-aggregate 505 interface frictional resistance. However, with further increasing shear displacement, the 506 contribution of transverse rib passive resistance gradually increases and surpasses the 507 contribution of the geogrid-aggregate interface frictional resistance, indicating the attainment 508 of a relatively strong interlocking state in the geogrid-aggregate system. When the total shear 509 resistance reaches its peak under each normal stress, the contribution of the passive resistance of transverse ribs ranges from 16.7% to 22.8%. Notably, the maximum contribution of the 510 511 passive resistance of transverse ribs consistently occurs after the peak total shear stress. In this 512 study, the maximum contribution of the passive resistance of transverse ribs reached 43.5%, as 513 shown in Fig. 17(a). In the post-peak stage of the total shear stress, the contribution of 514 transverse rib passive resistance continues to increase until it reaches the peak and then 515 fluctuates. This indicates that the passive resistance of transverse ribs can be maintained under 516 relatively large shear displacements. Overall, during the entire shear process, the contribution 517 of frictional resistance of aggregate exceeds the other two shear resistance components. This is 518 attributed to the large opening area of the geogrid aperture, which leads to more aggregate-519 aggregate contacts and interactions contributing to shear resistance compared to aggregate-520 geogrid contacts.

# 521 **5. Influence of Aperture-aggregate Size Ratio**

522 The relationship between aperture size and aggregate size has been identified as a 523 significant factor influencing the shear strength of geogrid-aggregate interfaces (Brown et al., 524 2007; Liu et al., 2022; Miao et al., 2020; Wang et al., 2016). This relationship is commonly 525 evaluated using the aperture-aggregate ratio,  $A_s/D_{50}$ , defined as the ratio of the geogrid aperture 526 size  $(A_s)$  to the average particle size of aggregate  $(D_{50})$ . In the geogrid-reinforced aggregate 527 structures, typical geogrid aperture sizes range between 15 mm and 65 mm (Indraratna et al., 528 2013; Liu et al., 2009a). To investigate the influence of aperture-aggregate ratio on the passive 529 resistance of transverse ribs, geogrid models with aperture sizes of 28 mm, 40 mm, and 56 mm 530 (corresponding to aperture-aggregate ratios of  $A_s/D_{50} = 1.67, 2.38$ , and 3.33, respectively) were 531 utilized for geogrid-aggregate interface direct shear tests. All these simulations were conducted under a normal stress  $\sigma_n = 50$  kPa while keeping the micro-contact parameters consistent with 532 the previously calibrated values. 533

534 As shown in Fig. 18(a), the specimen with  $A_s/D_{50} = 2.38$  exhibits the highest total shear 535 strength. This is because this aperture-aggregate ratio promotes interlocking between the coarse 536 aggregate-geogrid apertures. Fig. 18(b)-(d) presents the evolution curves of each shear resistance component with shear displacement for specimens with different  $A_s/D_{50}$ . The data 537 538 indicate that the passive resistance of transverse ribs in the specimen with  $A_s/D_{50} = 2.38$  is 539 significantly greater than those of the other specimens. In contrast, the geogrid-aggregate 540 interface frictional resistance and the frictional resistance of aggregate are similar for all specimens. The results demonstrate the significance of the passive resistance of transverse ribs 541 542 in enhancing the overall shear strength.

### 544 6. Influence of Geogrid Rib Stiffness

The secant stiffness at 2% strain of the geogrid,  $J_{2\%}$ , can be determined through geogrid 545 tensile tests and is considered as a crucial factor influencing the shear strength of geogrid-546 547 aggregate interfaces. The tensile stiffness values of several typical geogrids used in field 548 projects ranging from 330 kN/m to 1185 kN/m (Jia et al., 2021; Jiang et al., 2016; Yang et al., 549 2012). To investigate the influence of geogrid stiffness on the passive resistance of transverse 550 ribs, several additional geogrid numerical models were developed. The secant stiffness was set as  $J_{2\%} = 330$  kN/m, 660 kN/m, and 990 kN/m, respectively. It is noteworthy that, compared to 551 the specimen with  $J_{2\%} = 330$  kN/m, the normal stiffness of parallel bond,  $\bar{k_n}$ , in the other models 552 was uniformly scaled, ensuring that the stiffness ratio between the transverse and longitudinal 553 ribs remained constant. 554

555 Fig. 19 presents a comparison of simulation results from direct shear tests for geogrids 556 having three different secant stiffnesses. The results reveal that the peak shear stress increases 557 with the increase of geogrid stiffness, as expected. When examining the evolution of shear 558 resistance components, it is observed that increasing geogrid stiffness has minimal effect on 559 frictional resistance of aggregate  $(FR_s)$  and geogrid-aggregate interface frictional resistance  $(FR_g)$  but significantly influences the passive resistance of transverse ribs  $(PR_g)$ . Additionally, 560 561 at relatively small shear displacements (< 2.5 mm), the passive resistance of transverse ribs remains relatively low but rapidly increases as the shear displacement increases (Fig. 19(b)). 562 This behavior can be attributed to the interaction mechanism between the transverse ribs of 563 geogrid and aggregate, which leads to flexible deformation of transverse ribs (Fig. 11). 564

However, such deformation requires a certain shear displacement to occur, and higher geogrid stiffness reduces the required displacement. Overall, an increase in geogrid stiffness promotes the passive resistance of transverse ribs. Consequently, maximizing the passive resistance of transverse ribs can be achieved by employing geogrids with higher rib stiffness.

569

### 570 **7. Conclusions**

In this study, three-dimensional DEM models were developed to simulate the direct shear 571 572 tests investigating fundamental interaction mechanism of geogrid-aggregate interfaces. The 573 DEM model was calibrated based on the experimental results. By analyzing the displacement 574 field of particles, the local shear band at the geogrid-aggregate interface was identified, and the 575 contact normal direction of particles within the shear band was determined. Different types of 576 contacts were quantified to assess the evolution of each shear resistance component during the 577 direct shear test of geogrid-aggregate interface. Furthermore, the influences of apertureaggregate ratio  $(A_s/D_{50})$  and geogrid stiffness  $(J_{2\%})$  on the passive resistance of transverse ribs 578 579 were investigated. The following conclusions can be drawn:

(1) Under direct shear of geogrid-aggregate interfaces, higher normal stresses prevent the upward extension of shear band while promoting its downward development. As the normal stress increases, the boundaries of the upper and lower shear bands shift downwards, while the total thickness of shear band remains relatively constant. This indicates that particles tend to be closely compressed and interlocked under high normal stress conditions.

585 (2) During the initial shearing stage, the frictional resistance between aggregates becomes

active, followed by the geogrid-aggregate interface frictional resistance. The development of passive resistance of transverse ribs exhibits a certain lag, particularly in the early stages of shearing. With increasing normal stress, each shear resistance component experiences significant growth, with the frictional resistance component of aggregates exhibiting the most pronounced increase.

(3) When the total shear resistance reaches its peak value under different normal stresses, the contribution of the passive resistance of transverse ribs ranges between 16.7% and 22.8%. The maximum contribution of the passive resistance of transverse ribs consistently occurs after the peak of total shear stress, reaching a maximum of 43.5%. Furthermore, the passive resistance of transverse ribs mobilizes shear strength at greater shear displacement levels than the other two shear resistance components.

(4) The relationship between the geogrid aperture size and aggregate size  $(A_s/D_{50})$  has a limited impact on the geogrid-aggregate interface frictional resistance and the frictional resistance of aggregates. In contrast, the aperture-aggregate ratio plays a crucial role in enhancing the total shear strength by improving the passive resistance of transverse ribs. In this study, the maximum value of transverse rib passive resistance was increased by 110% and 41% at  $A_s/D_{50} = 2.38$  compared to  $A_s/D_{50} = 1.67$  and  $A_s/D_{50} = 3.33$ , respectively.

603 (5) Increasing the stiffness of geogrid has a minor influence on the frictional resistance of 604 aggregate and geogrid-aggregate interface frictional resistance, but significantly affects the 605 passive resistance of transverse ribs. Higher geogrid stiffness enables the mobilization of 606 passive resistance from the transverse ribs under smaller relative displacements between the

607	geogrid and aggregates, thereby promoting the development of passive resistance of transverse
608	ribs. Consequently, utilizing geogrids with higher rib stiffness maximizes the passive resistance
609	of transverse ribs.
610	
611	Acknowledgments
612	This research is supported by the National Natural Science Foundation of China (Grant
613	No. 52278360 and 52078392) and the National Key R&D Program of China (Grant No.
614	2022YFC3080400). The authors gratefully acknowledge the financial supports.
615	
616	Competing Interests Statement
617	The authors declare that they have no known competing financial interests or personal
618	relationships that could have appeared to influence the work reported in this paper.
619	
620	Data Availability Statement
621	Some or all data, models, or codes that support the findings of this study are available from
622	the corresponding author upon reasonable request.
623	
624	References
625	ASTM-D 5321. Standard test method for determining the coefficient of soil and geosynthetic
626	or geosynthetic and geosynthetic friction by the direct shear method. West Conshohocken,
627	PA, USA: ASTM International.

628	Abdelrahman, A.H., Ashmawy, A.K., Abdelmoniem, M., 2008. An Apparatus for Direct Shear,
629	Pullout, and Uniaxial Testing of Geogrids. Geotechnical Testing Journal 31, 470-479.
630	Abdi, M.R., Mirzaeifar, H., 2017. Experimental and PIV evaluation of grain size and
631	distribution on soil-geogrid interactions in pullout test. Soils and Foundations 57, 1045-
632	1058.
633	Alfaro, M.C., Miura, N., Bergado, D.T., 1995. Soil-geogrid reinforcement interaction by
634	pullout and direct shear tests. Geotechnical Testing Journal 18, 157-167.
635	Brown, S.F., Kwan, J., Thom, N.H., 2007. Identifying the key parameters that influence
636	geogrid reinforcement of railway ballast. Geotextiles and Geomembranes 25, 326-335.
637	Cardile, G., Gioffre, D., Moraci, N., Calvarano, L.S., 2017. Modelling interference between
638	the geogrid bearing members under pullout loading conditions. Geotextiles and
639	Geomembranes 45, 169-177.
640	Chen, C., McDowell, G., Rui, R., 2018. Discrete element modelling of geogrids with square
641	and triangular apertures. Geomechanics and Engineering 16, 495-501.
642	Chen, C., McDowell, G.R., Thom, N.H., 2012. Discrete element modelling of cyclic loads of
643	geogrid-reinforced ballast under confined and unconfined conditions. Geotextiles and
644	Geomembranes 35, 76-86.
645	Ezzein, F.M., Bathurst, R.J., 2014. A new approach to evaluate soil-geosynthetic interaction
646	using a novel pullout test apparatus and transparent granular soil. Geotextiles and
647	Geomembranes 42, 246-255.
648	Feng, G., Zhao, J., Wang, H., Li, Z., Fang, Z., Fan, W., Yang, P., Yang, X., 2022. Study of the

- 649 internal re-breaking characteristics of broken limestone during compression. Powder Technology 396, 449-455.
- 651 Feng, S.-J., Liu, X., Chen, H.-X., Zhao, T., 2018. Micro-mechanical analysis of geomembrane-
- 652 sand interactions using DEM. Computers and Geotechnics 94, 58-71.
- Feng, S.J., Wang, Y.Q., 2023. DEM simulation of geogrid-aggregate interface shear behavior: 653
- 654 Optimization of the aperture ratio considering the initial interlocking states. Computers and Geotechnics 154. 655
- 656 Ferellec, J.-F., McDowell, G.R., 2010. A method to model realistic particle shape and inertia
- 657 in DEM. Granular Matter 12, 459-467.

- Ferellec, J.F., McDowell, G.R., 2012. Modelling of ballast-geogrid interaction using the 658 659 discrete-element method. Geosynthetics International 19, 470-479.
- 660 Ferreira, F.B., Vieira, C.S., Lopes, M.L., 2015. Direct shear behaviour of residual soil-
- 661 geosynthetic interfaces - influence of soil moisture content, soil density and geosynthetic
- 662 type. Geosynthetics International 22, 257-272.
- Gao, G., Meguid, M.A., 2018. Effect of particle shape on the response of geogrid-reinforced 663
- systems: Insights from 3D discrete element analysis. Geotextiles and Geomembranes 46, 664 665 685-698.
- 666 Grabowski, A., Nitka, M., Tejchman, J., 2021. Comparative 3D DEM simulations of sand-
- 667 structure interfaces with similarly shaped clumps versus spheres with contact moments.
- Acta Geotechnica 16, 3533-3554. 668
- Indraratna, B., Hussaini, S.K.K., Vinod, J.S., 2013. The lateral displacement response of 669

670	geogrid-reinforced ballast under cyclic loading. Geotextiles and Geomembranes 39, 20-
671	29.
672	Jewell, R.A., Milligan, G.W.E., Sarsby, R.W., Dubois, D., 1985. Interaction between Soil and
673	Geogrids. Proc., Conference on Polymer Grid Reinforcement, London, pp.18-29.
674	Jia, M., Zhu, W., Xu, C., 2021. Performance of a 33m high geogrid reinforced soil embankment
675	without concrete panel. Geotextiles and Geomembranes 49, 122-129.
676	Jia, Y., Zhang, J., Chen, X., Miao, C., Zheng, Y., 2023. DEM study on shear behavior of
677	geogrid-soil interfaces subjected to shear in different directions. Computers and
678	Geotechnics 156.
679	Jiang, Y., Han, J., Parsons, R.L., Brennan, J.J., 2016. Field Instrumentation and Evaluation of
680	Modular-Block MSE Walls with Secondary Geogrid Layers. Journal of Geotechnical and
681	Geoenvironmental Engineering 142.
681 682	Geoenvironmental Engineering 142. Jing, XY., Zhou, WH., Zhu, HX., Yin, ZY., Li, Y., 2018. Analysis of soil-structural
681 682 683	<ul><li>Geoenvironmental Engineering 142.</li><li>Jing, XY., Zhou, WH., Zhu, HX., Yin, ZY., Li, Y., 2018. Analysis of soil-structural interface behavior using three-dimensional DEM simulations. International Journal for</li></ul>
681 682 683 684	Geoenvironmental Engineering 142. Jing, XY., Zhou, WH., Zhu, HX., Yin, ZY., Li, Y., 2018. Analysis of soil-structural interface behavior using three-dimensional DEM simulations. International Journal for Numerical and Analytical Methods in Geomechanics 42, 339-357.
<ul> <li>681</li> <li>682</li> <li>683</li> <li>684</li> <li>685</li> </ul>	Geoenvironmental Engineering 142. Jing, XY., Zhou, WH., Zhu, HX., Yin, ZY., Li, Y., 2018. Analysis of soil-structural interface behavior using three-dimensional DEM simulations. International Journal for Numerical and Analytical Methods in Geomechanics 42, 339-357. Katagiri, J., 2019. A novel way to determine number of spheres in clump-type particle-shape
<ul> <li>681</li> <li>682</li> <li>683</li> <li>684</li> <li>685</li> <li>686</li> </ul>	<ul> <li>Geoenvironmental Engineering 142.</li> <li>Jing, XY., Zhou, WH., Zhu, HX., Yin, ZY., Li, Y., 2018. Analysis of soil-structural interface behavior using three-dimensional DEM simulations. International Journal for Numerical and Analytical Methods in Geomechanics 42, 339-357.</li> <li>Katagiri, J., 2019. A novel way to determine number of spheres in clump-type particle-shape approximation in discrete-element modelling. Geotechnique 69, 620-626.</li> </ul>
<ul> <li>681</li> <li>682</li> <li>683</li> <li>684</li> <li>685</li> <li>686</li> <li>687</li> </ul>	<ul> <li>Geoenvironmental Engineering 142.</li> <li>Jing, XY., Zhou, WH., Zhu, HX., Yin, ZY., Li, Y., 2018. Analysis of soil-structural interface behavior using three-dimensional DEM simulations. International Journal for Numerical and Analytical Methods in Geomechanics 42, 339-357.</li> <li>Katagiri, J., 2019. A novel way to determine number of spheres in clump-type particle-shape approximation in discrete-element modelling. Geotechnique 69, 620-626.</li> <li>Ke, H., Ma, P.C., Lan, J.W., Chen, Y.M., He, H.J., 2021. Field behaviors of a geogrid</li> </ul>
<ul> <li>681</li> <li>682</li> <li>683</li> <li>684</li> <li>685</li> <li>686</li> <li>687</li> <li>688</li> </ul>	<ul> <li>Geoenvironmental Engineering 142.</li> <li>Jing, XY., Zhou, WH., Zhu, HX., Yin, ZY., Li, Y., 2018. Analysis of soil-structural interface behavior using three-dimensional DEM simulations. International Journal for Numerical and Analytical Methods in Geomechanics 42, 339-357.</li> <li>Katagiri, J., 2019. A novel way to determine number of spheres in clump-type particle-shape approximation in discrete-element modelling. Geotechnique 69, 620-626.</li> <li>Ke, H., Ma, P.C., Lan, J.W., Chen, Y.M., He, H.J., 2021. Field behaviors of a geogrid reinforced MSW slope in a high-food-waste-content MSW landfill: A case study.</li> </ul>
<ul> <li>681</li> <li>682</li> <li>683</li> <li>684</li> <li>685</li> <li>686</li> <li>687</li> <li>688</li> <li>689</li> </ul>	<ul> <li>Geoenvironmental Engineering 142.</li> <li>Jing, XY., Zhou, WH., Zhu, HX., Yin, ZY., Li, Y., 2018. Analysis of soil-structural interface behavior using three-dimensional DEM simulations. International Journal for Numerical and Analytical Methods in Geomechanics 42, 339-357.</li> <li>Katagiri, J., 2019. A novel way to determine number of spheres in clump-type particle-shape approximation in discrete-element modelling. Geotechnique 69, 620-626.</li> <li>Ke, H., Ma, P.C., Lan, J.W., Chen, Y.M., He, H.J., 2021. Field behaviors of a geogrid reinforced MSW slope in a high-food-waste-content MSW landfill: A case study. Geotextiles and Geomembranes 49, 430-441.</li> </ul>
<ul> <li>681</li> <li>682</li> <li>683</li> <li>684</li> <li>685</li> <li>686</li> <li>687</li> <li>688</li> <li>689</li> <li>690</li> </ul>	<ul> <li>Geoenvironmental Engineering 142.</li> <li>Jing, XY., Zhou, WH., Zhu, HX., Yin, ZY., Li, Y., 2018. Analysis of soil-structural interface behavior using three-dimensional DEM simulations. International Journal for Numerical and Analytical Methods in Geomechanics 42, 339-357.</li> <li>Katagiri, J., 2019. A novel way to determine number of spheres in clump-type particle-shape approximation in discrete-element modelling. Geotechnique 69, 620-626.</li> <li>Ke, H., Ma, P.C., Lan, J.W., Chen, Y.M., He, H.J., 2021. Field behaviors of a geogrid reinforced MSW slope in a high-food-waste-content MSW landfill: A case study. Geotextiles and Geomembranes 49, 430-441.</li> <li>Liu, CN., Ho, YH., Huang, JW., 2009a. Large scale direct shear tests of soil/PET-yarn</li> </ul>

691 geogrid interfaces. Geotextiles and Geomembranes 27, 19-30.

- Liu, C.N., Zornberg, J.G., Chen, T.C., Ho, Y.H., Lin, B.H., 2009b. Behavior of Geogrid-Sand
- 693 Interface in Direct Shear Mode. Journal of Geotechnical and Geoenvironmental694 Engineering 135, 1863-1871.
- Liu, F.Y., Wang, P., Geng, X., Wang, J., Lin, X., 2016. Cyclic and post-cyclic behaviour from
- 696 sand-geogrid interface large-scale direct shear tests. Geosynthetics International 23, 129-697 139.
- Liu, F.Y., Ying, M.J., Yuan, G.H., Wang, J., Gao, Z.Y., Ni, J.F., 2021. Particle shape effects
- on the cyclic shear behaviour of the soil-geogrid interface. Geotextiles and
  Geomembranes 49, 991-1003.
- Liu, F.Y., Zheng, Q.T., Wang, J., Fu, H.T., Gao, Z.Y., Ni, J.F., 2022. Effect of particle shape
- 702 on shear behaviour of aggregate-geogrid interface under different aperture ratios.
- 703 International Journal of Pavement Engineering 23, 2099-2109.
- Liu, H.L., Ng, C.W.W., Fei, K., 2007. Performance of a geogrid-reinforced and pile-supported
- highway embankment over soft clay: Case study. Journal of Geotechnical and
  Geoenvironmental Engineering 133, 1483-1493.
- 707 Lopes, M.L., Ladeira, M., 1996. Influence of the confinement, soil density and displacement
- rate on soil-geogrid interaction. Geotextiles and Geomembranes 14, 543-554.
- 709 McDowell, G.R., Harireche, O., Konietzky, H., Brown, S.F., Thom, N.H., 2006. Discrete
- 710 element modelling of geogrid-reinforced aggregates. Proceedings of the Institution of
- 711 Civil Engineers-Geotechnical Engineering 159, 35-48.

712	Miao, C., Zheng, J., Zhang, R., Cui, L., 2017. DEM modeling of pullout behavior of geogrid
713	reinforced ballast: The effect of particle shape. Computers and Geotechnics 81, 249-261.
714	Miao, C.X., Jia, Y.F., Zhang, J., Zhao, J.B., 2020. DEM simulation of the pullout behavior of
715	geogrid-stabilized ballast with the optimization of the coordination between aperture size
716	and particle diameter. Construction and Building Materials 255.
717	Mirtich, B., 1996. Fast and Accurate Computation of Polyhedral Mass Properties. Journal of
718	Graphics Tools 1, 31-50.
719	Moraci, N., Gioffrè, D., 2006. A simple method to evaluate the pullout resistance of extruded
720	geogrids embedded in a compacted granular soil. Geotextiles and Geomembranes 24, 116-
721	128.
722	Ngo, N.T., Indraratna, B., Rujikiatkamjorn, C., 2014. DEM simulation of the behaviour of
723	geogrid stabilised ballast fouled with coal. Computers and Geotechnics 55, 224-231.
724	Palmeira, E.M., 2009. Soil-geosynthetic interaction: Modelling and analysis. Geotextiles and
725	Geomembranes 27, 368-390.
726	Palmeira, E.M., Milligan, G.W.E., 1989. Scale and other factors affecting the results of pull-
727	out tests of grids buried in sand. Geotechnique 39, 511-524.
728	Peng, X., Zornberg, J.G., 2019. Evaluation of soil-geogrid interaction using transparent soil
729	with laser illumination. Geosynthetics International 26, 206-221.
730	Rothenburg, L., Bathurst, R.J., 1989. Analytical study of induced anisotropy in idealized
731	granular materials. Geotechnique 39, 601-614.
732	Stahl, M., Konietzky, H., te Kamp, L., Jas, H., 2014. Discrete element simulation of geogrid-

- stabilised soil. Acta Geotechnica 9, 1073-1084.
- 734 Sweta, K., Hussaini, S.K.K., 2018. Effect of shearing rate on the behavior of geogrid-reinforced
- railroad ballast under direct shear conditions. Geotextiles and Geomembranes 46, 251-256.
- 737 Tatlisoz, N., Edil, T.B., Benson, C.H., 1998. Interaction between Reinforcing Geosynthetics
- and Soil-Tire Chip Mixtures. Journal of Geotechnical and Geoenvironmental Engineering
  124, 1109-1119.
- 740 Teixeira, S.H.C., Bueno, B.S., Zornberg, J.G., 2007. Pullout resistance of individual
- 741 longitudinal and transverse geogrid ribs. Journal of Geotechnical and Geoenvironmental
  742 Engineering 133, 37-50.
- Thornton, C., 2000. Numerical simulations of deviatoric shear deformation of granular media.
  Geotechnique 50, 43-53.
- 745 Tutumluer, E., Huang, H., Bian, X.C., 2012. Geogrid-Aggregate Interlock Mechanism
- 746 Investigated through Aggregate Imaging-Based Discrete Element Modeling Approach.
- 747 International Journal of Geomechanics 12, 391-398.
- 748 Wang, H.-L., Zhou, W.-H., Yin, Z.-Y., Jie, X.-X., 2019. Effect of Grain Size Distribution of
- Sandy Soil on Shearing Behaviors at Soil-Structure Interface. Journal of Materials in Civil
   Engineering 31.
- 751 Wang, J., Chi, S., Zhou, X., Shao, X., 2023. Experimental and numerical investigation of the
- size effect of rockfill particles on crushing strength. Granular Matter 25.
- 753 Wang, J., Liu, F.Y., Wang, P., Cai, Y.Q., 2016. Particle size effects on coarse soil-geogrid

754	interface	response	in	cyclic	and	post-cyclic	direct	shear	tests.	Geotextiles	and
755	Geomem	branes 44,	854	-861.							

- 756 Wang, J., Ying, M., Liu, F., Yuan, G., Fu, H., 2021. Experimental investigation on the stress-
- 757 dilatancy response of aggregate-geogrid interface using parameterized shapes.
- 758 Construction and Building Materials 289.
- 759 Wang, P., Yin, Z.-Y., Zhou, W.-H., Chen, W.-b., 2022. Micro-mechanical analysis of soil-
- structure interface behavior under constant normal stiffness condition with DEM. Acta
- 761 Geotechnica 17, 2711-2733.
- Wang, P., Yin, Z.Y., 2022. Effect of particle breakage on the behavior of soil-structure
  interface under constant normal stiffness condition with DEM. Computers and
  Geotechnics 147.
- Wang, Z.J., Jacobs, F., Ziegler, M., 2014. Visualization of load transfer behaviour between
- 766 geogrid and sand using PFC2D. Geotextiles and Geomembranes 42, 83-90.
- 767 Yang, G., Liu, H., Lv, P., Zhang, B., 2012. Geogrid-reinforced lime-treated cohesive soil
- retaining wall: Case study and implications. Geotextiles and Geomembranes 35, 112-118.
- 769 Ying, M.J., Liu, F.Y., Wang, J., Wang, C.L., Li, M.F., 2021. Coupling effects of particle shape
- and cyclic shear history on shear properties of coarse-grained soil-geogrid interface.
- 771 Transportation Geotechnics 27.
- Zhang, J., Guo, W., Ji, M., Zhao, J., Xu, C., Zheng, Y., 2022. Field monitoring of vertical stress
- distribution in GRS-IBS with full-height rigid facings. Geosynthetics International 0, 1-
- 774 12.

- 775 Zhou, J., Chen, J.F., Xue, J.F., Wang, J.Q., 2012. Micro-mechanism of the interaction between
- sand and geogrid transverse ribs. Geosynthetics International 19, 426-437.
- 777 Zhou, Y., Wang, H., Zhou, B., Li, J., 2018. DEM-aided direct shear testing of granular sands
- incorporating realistic particle shape. Granular Matter 20.

Parameter	Value
Density, $\rho_g$ (kg/m <sup>3</sup> )	972
Local damping coefficient, $d_p$	0.7
Friction coefficient, $\mu_{g}$	0.43
Effective modulus, $E^*$ (MPa)	$6 \times 10^{2}$
Normal-to-shear stiffness ratio, $\kappa^*$	1
Longitudinal rib bond effective modulus, $\vec{E^*}$ (MPa)	$8 \times 10^{2}$
Transverse rib bond effective modulus, $\tilde{E}^*$ (MPa)	$6 \times 10^{2}$
Bond normal-to-shear stiffness ratio, $\vec{K}^*$	100
Bond radius multiplier, $\overline{r}_m$	1
Bond gap, $\overline{g}$ (m)	$7.5  imes 10^{-4}$

 Table 1. Geogrid model parameters.

**Table 2.** Aggregate particle model parameters.

Parameter	Value
Density, $\boldsymbol{\rho}_a$ (kg/m <sup>3</sup> )	2650
Local damping coefficient, $d_p$	0.7
Friction coefficient, $\mu_a$	0.55
Effective modulus. $E^*$ (MPa)	$2 \times 10^{3}$
Normal-to-shear stiffness ratio, $K^*$	1

 Table 3. Geogrid-aggregate contact parameters.

Parameter	Value
Friction coefficient, $\mu_s$	0.43
Effective modulus, $E^*$ (MPa)	$1.3 \times 10^{3}$
Normal-to-shear stiffness ratio, $\kappa^*$	1



Fig. 1. Comparison of tensile test results between experiments and DEM simulations.



Fig. 2. Comparison of two-aperture extension test results between experiment and DEM

simulation: (a) experiment; (b) DEM simulation.



Fig. 3. Comparison between experiments and DEM simulations: (a) particle size distribution;

(b) shear strength.



Fig. 4. Comparison of direct shear test results between experiments and DEM simulations.



Fig. 5. Apparatus for geogrid-aggregate interface direct shear test.



Fig. 6. DEM model of direct shear test: (a) geogrid model; (b) geogrid-aggregate interface

shear model.



Fig. 7. Comparison of interface direct shear test results between experiments and DEM

simulations.



Fig. 8. Comparison of experiments and DEM simulations: (a) interface shear strength coefficient; (b) shear displacement at peak shear strength.



Fig. 9. Shear resistance components in direct shear test.



**Fig. 10.** Contact force distribution mobilized in an aperture of geogrid: (a) at shear displacement of 9 mm; (b) at shear displacement of 18 mm; (c) at shear displacement of 27

mm.



Fig. 11. Comparison of geogrid deformations after shear between experiment and DEM simulation under  $\sigma_n = 50$  kPa: (a) experiment; (b) DEM simulation.



**Fig. 12.** Shear band distribution: (a) aggregate particle displacement distribution; (b) shear

band thickness.



**Fig. 13.** Contact force chains: (a) contact distribution at peak shear strength; (b) contact normal direction fitting; (c) normal contact force direction fitting.



Fig. 14. Principal direction of contact normal and normal contact force.



**Fig. 15.** Identification of contact forces contributing to shear resistance: (a) contacts contributing to transverse rib passive resistance; (b) contacts contributing to total geogrid

resistance.



Fig. 16. Shear resistance component evolution under different normal stresses: (a)  $\sigma_n = 50$ 

kPa; (b)  $\sigma_n = 100$  kPa; (c)  $\sigma_n = 150$  kPa; (d)  $\sigma_n = 200$  kPa.



Fig. 17. Shear resistance contribution under different normal stresses: (a)  $\sigma_n = 50$  kPa; (b)  $\sigma_n$ 

### = 100 kPa; (c) $\sigma_n$ = 150 kPa; (d) $\sigma_n$ = 200 kPa.



**Fig. 18.** Influence of aperture-aggregate ratio: (a) total shear stress; (b) transverse rib passive resistance; (c) geogrid-aggregate interface frictional resistance; (d) frictional resistance of

aggregate.



(c) (d)

**Fig. 19.** Influence of geogrid rib stiffness: (a) total shear stress; (b) transverse rib passive resistance; (c) geogrid-aggregate interface frictional resistance; (d) frictional resistance of

aggregate.