



## OPEN Mutation adaptive cuckoo search hybridized naked mole rat algorithm for industrial engineering problems

Rohit Salgotra<sup>1,2✉</sup>, Supreet Singh<sup>3</sup>, Pooja Verma<sup>4</sup>, Laith Abualigah<sup>6</sup> & Amir H Gandomi<sup>2,5,7✉</sup>

Cuckoo Search (CS) is a popular algorithm used to solve numerous challenging problems. In the present work, a novel variant of CS is presented to eliminate its shortcomings. The proposed algorithm is hybridized with the naked mole rat algorithm (NMRA) to enhance the exploitative behavior of CS, and is called Mutated Adaptive Cuckoo Search Algorithm (MaCN). This new algorithm has self-adaptive properties and its key feature is to divide the solutions into multiple sections, which are often called sub-swarms. In addition, a bare-bones search mechanism is also added to enhance exploration. The use of adaptive inertia weights helps optimize the switching probability, an important CS parameter that helps to achieve a balanced operation. The proposed MaCN algorithm is tested on CEC 2005 and CEC 2014 benchmark problems. Comparative studies showed that MaCN delivers promising results in solving CEC competition benchmark problems compared to JADE, success history-based adaptive DE (SHADE), LSHADE-SPACMA and self-adaptive DE (SaDE), among others. In addition to numerical benchmarks, MaCN is used to solve the industrial engineering frame structure and a comparison with hybridization of particle swarm with passive congregation (PSOPC), shuffled frog leaping algorithm hybrid with invasive weed optimization (SFLAIWO), particle swarm ant colony optimization (PSACO), early strategy with DE (ES-DE), and others show its superiority. In addition, the Wilcoxon ranksum and the Freidmann test statistically prove the significance of the proposed MaCN algorithm. MaCN was found to score first rank for the benchmarks. The application of the MaCN algorithm to solve the design problems of the suggests that the best new results are obtained for all test cases.

**Keywords** Cuckoo search, Naked mole-rat algorithm, Frame design problems, CEC benchmark functions, Mutated cuckoo search

There are countless real-world uses of optimization in every area. Many technical and industrial sectors are now struggling to develop a suitable optimizer or algorithm to handle real-world challenges. The primary justification for employing such techniques is that most applications may be characterized as possible domain problems related to the criteria to be achieved. This can be predicted since these methods are used in practically every field of research, including finance, architecture, mathematics, image analysis, weather prediction, industrial engineering, administration, manufacturing, planning, routing issues, pattern recognition, etc. These optimization issues are extremely complicated, making it difficult for academics to solve them quickly. Nature-inspired algorithms (NIAs) have been used in many sectors of research studies in recent years, and now are used in practically every discipline.

NIAs are found to be reliable algorithms for complex optimization problems. Major algorithms include stochastic paint optimizer<sup>1</sup>, sine cosine algorithm (SCA)<sup>2</sup>, flower pollination algorithm (FPA)<sup>3</sup>, differential evolution (DE)<sup>4</sup>, grey wolf optimizer (GWO)<sup>5</sup>, reptile search algorithm (RSA)<sup>6</sup>, harris hawks optimization (HHO)<sup>7</sup>, antlion optimization algorithm (ALO)<sup>8</sup>, naked mole-rat algorithm (NMRA)<sup>9</sup>, gradient-based optimizer<sup>10</sup>,

<sup>1</sup>Faculty of Physics and Applied Computer Science / Centre of Excellence in Artificial Intelligence, AGH University of Krakow, Kraków, Poland. <sup>2</sup>Faculty of Engineering & Information Technology, University of Technology Sydney, Sydney, Australia. <sup>3</sup>School of Computer Science, UPES, Dehradun, Uttarakhand, India. <sup>4</sup>Department of Computer Science & IT, Kathua Campus, University of Jammu, J & K, India. <sup>5</sup>University Research and Innovation Center (EKIK), Óbuda University, Bécsi út 96/B, 1034 Budapest, Hungary. <sup>6</sup>Al al-Bayt University, Computer Science Department, Mafraq, Jordan. <sup>7</sup>Department of Computer Science, Khazar University, Mahsati 41, Baku, Azerbaijan. ✉email: r.03dec@gmail.com; rohitsu@agh.edu.pl; gandomi@uts.edu.au

arithmetic optimization algorithm (AOA)<sup>11</sup>, aquila optimizer (AO)<sup>12</sup>, artificial bee colony (ABC) algorithm with local and global information interaction<sup>13</sup>, hybrid SCA<sup>14</sup>, an improved artificial rabbits optimization (ARO) algorithm with chaotic local search and opposition-based learning<sup>15</sup>, seahorse optimization algorithm based on chaotic maps<sup>16</sup>, feature selection using optimization methods<sup>17</sup>, enhanced artificial hummingbird algorithm (AHA)<sup>18</sup>, AHA improved by natural survivor method<sup>19</sup>, dynamic fitness-distance balance-based ARO<sup>20</sup> and adaptive gaining-sharing knowledge algorithm<sup>21</sup>. Although these algorithms have proven extraordinary effectiveness and performance, various assessments show that their performance and competitiveness depend on the tuning parameters used<sup>22,23</sup>. Scaling factor, mutation/crossover rate, switch probability, local/global search, conventional randomization, and population size (*popsiz*), are examples of such factors<sup>24</sup>. Early research shows that tuning the parameters of these algorithms requires a trial-and-error search. This procedure takes time and is inefficient. Premature convergence, stagnation of local optima, delayed convergence, and other issues plague these algorithms<sup>22</sup>. Due to these flaws, algorithms are prone to poor solution generation, which results in reduced variety and, as a result, an inability to identify the intended solution<sup>24</sup>. In general, NIAs have been discovered to have flaws and additional effort is needed to develop new algorithms for future scholars.

Cuckoo search (CS) is an effective algorithm introduced in 2009, and has been used in various research domains<sup>25</sup>. Moreover, the basic paper has achieved more than 8,800 citations to date<sup>25</sup>. The algorithm is simple in structure and is considered one of the most promising algorithms among domain researchers because of its linear nature. CS is divided into two parts: exploration (*expl*) via global search and exploitation (*expt*) via local search and a probability of switching ( $s_p$ ) to control *expl* and *expt* operation<sup>26</sup>. The parameter  $s_p$  helps the algorithm maintain a proper balance between both *expl* and *expt*. From the literature above and in section 3, it can be seen that most of the work in the literature deals with parametric modifications, and little has been done to improve the *expl* and *expt* simultaneously. There are modifications in the local or global search or a specific switch probability. Apart from that, very little work is available in the literature that improves the algorithm's overall performance.

Some recent CS adaptations to improve its overall performance aimed at adapting probability, global search, and local search<sup>26</sup>. Another modification was proposed in<sup>27</sup> that uses adaptive *population* reduction and adaptive switch probability. These modifications make the algorithm adaptive but require new initial and final parameters for adaptations. These parameters make CS complex and highly challenging in execution. Thus, new adaptations are required to the basic algorithms to make them self-adaptive. Apart from that, the hybridization of CS with other algorithms is still a novel concept and has not been explored to its full potential.

Here, a new adaptation of CS is proposed using self-adaptive properties and hybridization concerning naked mole-rat algorithm (NMRA)<sup>9</sup>. The proposed algorithm is named mutation adaptive cuckoo search, inspired by NMRA (MaCN). The proposed MaCN algorithm employs the concepts of iterative division and population division as inspired from<sup>26</sup>. Here, the population division means that the population is split into multiple parts, and each set of these populations are evaluated using different mathematical equations. Iterative division on the other hand deals with multiple set of iterations for finding new solutions. Another modification is adding a bare-bones mechanism for enhanced *expl*, hybridization concerning NMRA for improved *expt*, and inertia weights *iw* associated with switch probability for balancing both *expl* and *expt* operations<sup>28</sup>. The reason for using a bare-bones mechanism is because of its better capabilities to reinforce complementary search for achieving cooperative search<sup>29</sup>. NMRA, on the other hand, is found to provide better *expt* capabilities by enhancing the search space concerning the best solution<sup>9</sup>. Apart from these modifications, adaptive reduction in *popsiz* is also followed to minimize the computational burden of the proposed technique<sup>30</sup>.

To check the capability of proposed MaCN algorithm, CEC 2005 dataset<sup>31</sup> and CEC 2014<sup>32</sup> datasets are used. These test functions are highly challenging benchmarks and have been exploited by researchers from various different domains of research. In order to have a fair comparison, more than fifteen recently introduced algorithms namely cuckoo version 1.0 (CV 1.0)<sup>26</sup>, NMRA<sup>9</sup>, memory guided sine cosine algorithm (MGSCA)<sup>33</sup>, beta DE (BDE)<sup>34</sup>, equilibrium optimizer<sup>35</sup>, covariance adaptation based evolution strategy (CMA-ES)<sup>36</sup>, hybridization of SCA with crow search algorithm (SCCS)<sup>37</sup>, adaptive external archive based DE (JADE)<sup>38</sup>, success-history based DE (SHADE)<sup>39</sup>, extended GWO (GWO-E)<sup>40</sup>, self adaptive DE (SaDE)<sup>41</sup>, whale optimization algorithm with opposition based learning (OEWOA)<sup>42</sup>, hybridization of SHADE with CMA-ES (LSHADE-SPACMA)<sup>43</sup>, and fractional-order calculus-based FPA (FA-FPO)<sup>44</sup> are used.

On the other hand, the algorithms under comparison for CEC 2014 benchmark problems are MGSCA<sup>33</sup>, BDE<sup>34</sup>, population-based incremental learning (PBIL)<sup>45</sup>, chaotic CS (CCS)<sup>46</sup>, improved symbiotic organisms search (ISOS)<sup>47</sup>, random walk GWO (RW-GWO)<sup>48</sup>, blended biogeography-based optimization (B-BBO)<sup>49</sup>, laplacian BBO (LX-BBO)<sup>50</sup>, variable neighbourhood BA (VNBA)<sup>51</sup>, and improved elephant herding optimization (IMEHO)<sup>52</sup> have been used. Apart from that, three industrial engineering problems have also been used to test the performance of MaCN algorithm. Statistical tests (Wilcoxon rank-sum test<sup>53</sup> and Friedman's test<sup>54</sup>) are done for proving the statistical significance of MaCN. From results in section 5, it can be seen that the proposed MaCN is efficient and is a strong candidate for optimization research. The major highlights of our work are as:

- A hybrid variant of CS using nMRA is proposed to enhance the exploitative properties of CS, named as MaCN.
- New concepts of iterative/generation division is added, by classifying search agents into multiple segments and different mathematical equations for each are used.
- To make the algorithm self-adaptive six mutation operators are applied. It is also taken into account that the added modifications help the algorithm in better exploration and exploitation.
- The size of the population is reduced over the course of iterations, to reduce the computational burden of the proposed algorithm.

- A comparison on CEC 2005, and CEC 2014 is done with respect to JADE, SaDE, SHADE, CMA-ES, LSHADE-SPACMA, LX-BBO, HGAPSO, STMP-SSOA and others, to prove the competitiveness of the proposed algorithm.
- Three industrial engineering frame design problems are also taken into account to prove the significance of the proposed algorithm.

Overall, the paper is divided into seven sections. Here the basic concepts of optimization research, the motivation behind present work, and brief details about the present work are presented in section 1. Section 2 gives details about CS, whereas Section 3 has the recent literature on the modifications and application of CS to real applications. Details about the proposal are presented in section 4 and corresponding results are discussed in section 5. The summary of results and insightful implications are discussed in section 6. Finally, the conclusion and future scope are drawn in the final section 7. The outline of the present work is given in Figure 1.

## Basics of cuckoo search algorithm

The cuckoo search algorithm (CS) is a swarm intelligence-based NIA<sup>25</sup> based on the breeding behaviour of cuckoo species found in nature. The basic idea of CS is discussed as:

### Cuckoos breeding behaviour

Cuckoos are prevalent birds due to the beautiful voice and strategy of reproduction they are used. The cuckoo species like *ani* and *guirafollow* brood parasitic behaviour by placing their eggs in other species nests. Although cuckoo species enhance the probability of hatching of their eggs by removing the eggs of another species<sup>55</sup>. If the other species or host birds found that eggs placed in the nest are not their own, then host birds either throw the eggs away or dump the whole nest. Some species of cuckoo are experts in mimicry of pattern and colour of some host eggs. By this, the abandoned rate of the cuckoo eggs is reduced, and the reproduction rate increases. Further, parasitic cuckoos usually select a nest in which the host species just lay down eggs. This is because the cuckoo eggs hatch comparatively faster than the host eggs and after hatching, it throws out host eggs. So, the cuckoo chick gets more food from the host<sup>55</sup>. Sometimes, the cuckoo chick sometimes mimics the host chick's voice to enhance the chance of getting more food.

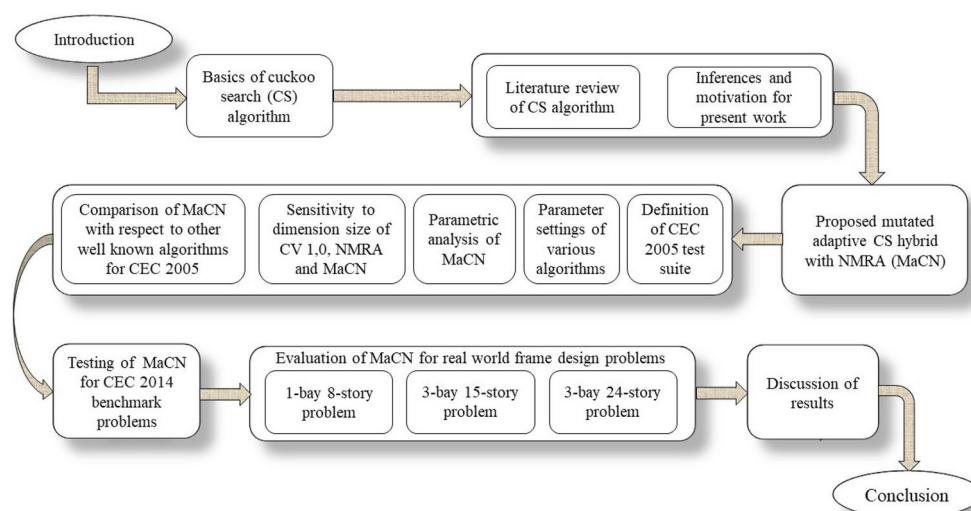
### Lévy flights

In nature, most of the birds follow random walks to find food. In the same way, cuckoos also follow random walks where the following location depends on the transition probability and current location. The different studies are given in<sup>56,57</sup> shows that the behaviour of main birds illustrates the Lévy flight characteristics. The use of Lévy flights enhances the capability of searching in comparison with a simple random walk. It is also a random walk where length of steps follows a heavily-tailed distribution function<sup>25</sup>. Due to this behaviour, it has been used for optimization, and early-stage results prove its capability for optimal search<sup>58</sup>.

### Cuckoo Search

Three ideal basic rules are utilized to define the CS algorithm<sup>25</sup>, such as:

- One cuckoo only lays one egg, which they find at random in a nest.
- The best eggs are chosen and passed down to future generations.



**Fig. 1.** Outline of the article.

- The value of host nests is constant, and the host probability  $p \in [0, 1]$  to recognize cuckoo eggs. The host bird either discard the cuckoo egg, or quit the entire nest and build a new nest. It's also believed that some  $n$  nests are replaced with new nests, for diversity.

Cuckoo search can be implemented using the three rules stated above, with each cuckoo representing a possible solution. Using the Lévy flight, a new nest or solution  $x_i^{t+1}$  for the  $i^{th}$  cuckoo is generated.

$$x_i^{t+1} = x_i^t + \alpha \otimes Levy(\beta) \quad (1)$$

where,  $x_i^t$  is a current solution to find the next solution  $x_i^{t+1}$ ,  $\alpha > 0$  is the step size corresponds to the scale of problem under consideration and  $\otimes$  defines element wise multiplication. The main objective to find a new solution (cuckoo) and possibly a better solution to replace not good solution. Here, Lévy flight based random walk is preferred because it explores effectively. The Lévy flight step size is much longer and derived from the Lévy distribution having an infinite mean and variance.

$$Levy \sim \mu = t^{-\beta}, (1 < \beta \leq 3) \quad (2)$$

where  $\beta$  is the probability of an event occurring. Some new solutions acquired by Lévy flights are close to the best solution ever developed, and they improve the speed of local search. However, far-field optimization should be used to define a portion of new solutions, and the position of these solutions should be away from the present best to prevent the system from becoming stuck in local minima. The steps of cuckoo search are based on a random walk inspired by power-law distribution, resulting in a heavy-tailed step size. Randomization on a larger scale allows for such a large step size. The literature review is detailed in the next section.

## Literature review

In this section, a detailed literature on CS and inference drawn from the literature has been discussed. The detailed literature is broadly categorized into two parts: a literature based on modifications of CS and a literature based on applications of CS.

### Literature based on modifications

Cuckoo search is a very promising algorithm for different fields of optimization. In<sup>59</sup> a binary CS with sigmoid function was proposed to solve binary optimization problems. In addition, discrete versions of CS (DCS) have been proposed by<sup>60,61</sup> to tackle the traveling salesman problem (TSP). The DCS algorithm proposed by<sup>61</sup> uses population rebuilding to improve its efficiency compared to discrete PSO<sup>62</sup>. The modified CS algorithm (MCS) in<sup>63</sup> was used to solve the unconstrained optimization problems. As the author tested the performance of MCS by applying only on eight benchmark functions, it can be analyzed that functions providing good results are considered, and the rest are neglected. The other version of MCS was implemented<sup>64</sup> with rough sets to handle high dimension data for feature selection. This version is meant to reduce learning parameters so that consumption time decreases and convergence speed increases.

In addition, Abdul et al.<sup>65</sup> proposed another version of MCS to suppress the side lobes in the linear antenna array. The other variant of MCS was implemented in<sup>66</sup> to solve analytical aspects of multiobjective distribution systems with different compensators. Here, the basic CS algorithm was modified using a crossover operator to maintain a balance between *expl* and *expt*. This leads to an improvement in the convergence rate and quality of the solution. The one-rank CS algorithm<sup>67</sup> was proposed for the optimization of the algorithmic trading system. In this, a new solution was generated by combining the phases *expl* and *expt* and the best utilization of Lévy flight such as step size  $\alpha = 0.01$ . The performance of basic CS was enhanced by a new variant of MCS<sup>68</sup> to optimize the wired-EDM process. CS was modified<sup>69</sup> to converge faster, although it is not guaranteed that the rate of convergence is fast because it is based on random walks. The other variants of CS consist of improved CS (ICS) by modify step length for solving coloring problem of planar graph<sup>70</sup>, new CS with improved *expl* and *expt* properties for numerical optimization<sup>76</sup>, Chaotic CS to reconstruct chaotic dynamics<sup>71</sup>, enhanced CS for contrast management of grey scale images<sup>72</sup>, Complex valued CS to optimize design problems<sup>73</sup>, novel CS-based on Gauss distribution (GCS)<sup>74</sup>, quantum CS for clustering data problems<sup>75</sup>, new CS integrated with fuzzy system<sup>76</sup>, hybrid multi-objective CS based on dynamical local search<sup>77</sup>, improved CS integrated with chaotic flower pollination algorithm to maximize coverage area of wireless sensor network<sup>78</sup>, hybrid CS with GWO for medical image fusion<sup>79</sup>, hybridization of CS with BA for optimization of numerical benchmark functions<sup>80</sup>, hybrid CS with krill herd optimization algorithm for engineering problems<sup>81</sup>, fractional-order CS to identify parameters of financial system<sup>44</sup>, hybrid CS with Levenberg-Marquardt back propagation algorithm<sup>82</sup> and it can be seen that local optima stagnation problem will be avoided. Hybrid CS with genetic algorithm (CS-GA) was proposed to solve redundancy allocation and reliability problems<sup>83</sup>, drilling path optimization problem for PCB holes<sup>84</sup> and hole making sequence optimization problem<sup>85</sup>. CS was also hybridized with differential evolution (CS-DE) for planning optimization problem of uninhabited combat air vehicle (UCAV)<sup>86</sup>, solving constrained engineering problems<sup>87</sup> and three-dimensional path planning problem of UCAV<sup>88</sup>. Hybrid CS with ant colony optimization (CS-ACO) to solve routing problem of mobile ad hoc network<sup>89</sup>, and job scheduling problem<sup>90</sup>. The population-based Harmony search algorithm is hybridized with CS (CS-HS) for the optimal water distribution system design<sup>91</sup>, and continuous optimization problems<sup>92</sup>. The CS was also hybridized with other local search-based algorithms such as CS with tabu search algorithm to solve quadratic assignment problems<sup>93</sup>, CS with quantum computing for knapsack problems<sup>94</sup>, CS with Nelder-Mead method for performance optimization of multi-cell solar system<sup>95</sup>, CS with newton method to solve linear least square problem<sup>96</sup> and CS with GWO to extract parameters of photo voltaic models<sup>97</sup>.



## Applications of CS algorithm

Apart from the modifications, CS is found to be capable for solving real optimization problems. These problems include diagnosis of diabetes<sup>98</sup>, clustering of web documents<sup>99</sup>, image recognition<sup>100</sup>, low contrast satellite images quality improvement<sup>101</sup>, structure design problems<sup>102</sup>, embedded system design problem<sup>103</sup>, designing of wind power system<sup>103</sup>, optimization of surface roughness in laser cutting<sup>104</sup>, power loss reduction of distribution system<sup>105</sup>, design of computer-aided power system<sup>106</sup>, economic load dispatch problem<sup>107</sup>, twitter sentiment analysis<sup>108</sup>, movie recommender system<sup>109</sup>, higher order filter design<sup>110</sup> and multi-machine power system stabilizer design problem<sup>111</sup>. The other applications of CS are forecasting of electrical load for power supply system<sup>112</sup>, optimization of visible light communication coverage in smart homes<sup>113</sup>, multi-objective hydro-thermal scheduling<sup>114</sup>, thinning of circular antenna arrays<sup>115</sup>, optimize efficiency of home energy management system<sup>116</sup>, detection of vibration fault for hydro-electric generating unit<sup>117</sup>, multi-objective community detection for dynamic networks<sup>118</sup>, solving non-linear equations of systems<sup>119</sup>, optimized configuration of electric distribution network<sup>120</sup>, waste management in smart cities<sup>121</sup>, navigation of mobile robots in uncertain environment<sup>122</sup>, gathering of load-balanced data<sup>123</sup>, prediction of defect in software data sets<sup>124</sup>, web service composition<sup>125</sup>, designing of hydraulic damper<sup>126</sup> and optimization of water distribution system<sup>127</sup>.

## Motivation for present work

Though, a lot of articles have been published on basic CS<sup>128</sup>. However, most of the work on the application part presented only minute details about the algorithms, and very limited research work has been done on parametric enhancements<sup>129</sup>. Thus posing a serious challenge on the proper *expl* and *expt* properties of CS algorithm. Apart from that, most of the hybridization's and improved version of CS deals with the change in one or two parameters and not necessarily the whole algorithm<sup>26</sup>. The major drawback of these algorithms is that, most of the proposed improvements are based on the basic CS and not on the enhanced versions. Thus there is a need to propose new hybrid versions of CS algorithm. Also recent studies on iterative division and population adaptation has brought significant advancements in the performance of CS algorithm<sup>40</sup>. All of the above said issues have motivated the authors to propose a new improvement in CS and its overall performance. In the next section, why's and how's of the proposed MaCN are discussed in details.

## The proposed MaCN algorithm

CS is one of many researchers' most promising optimization algorithms. Numerous works have been done to enhance its performance and solve real complex optimization problems. This algorithm is more suitable when dealing with higher dimension problems of optimization with additional improvements. As per no free lunch theorem<sup>130</sup>, no algorithm is considered a generic problem solver, so it motivates the researchers to hybridize and introduce modifications in CS. These modifications enhance the performance of an algorithm and make it capable of solving computationally complex problems. The classical CS suffers from the problems of stagnation and poor switching between *expl* and *expt* phases<sup>129</sup>. In a general CS, four parameters are of significant concern and need to be enhanced for better algorithm performance. Among these four parameters, scaling factor, switch probability (*pa*),  $\epsilon$  parameter of local random walk is the third parameter, and *popsiz*e of search agents is the final parameter. As discussed in section 3.3, all these four parameters have not been exploited to their full potential, and there is still scope for modification.

In the present study, the above discussed four parameters are adaptive instead of static nature, and based on this new algorithm has been proposed. The main aim of this newly proposed algorithm to mitigate the problems of poor *expt* and *expl*, slow convergence speed, and improper balancing between local search & global search. This algorithm is considered an extended version of CV 1.0 and named mutation adaptive CS hybrid with NMRA (MaCN). This algorithm is also based on the iterative/generation division concept<sup>26</sup>. In the division of generations concept, the population of search agents is classified into multiple segments and different mathematical notations define each segment. Here, the proposed algorithm follows the dual iterative division and broadly splits into global search phase (*gsp*) and local search phase (*lsp*). The different phases of the proposed algorithm and various modifications are discussed in consecutive subsections.

## Initialization

The first phase of MaCN is to deal with initialization of  $N$  cuckoos (population) in the random manner for dimension  $d$  of a problem. This phase is mathematically modelled as:

$$x_{i,k} = x_{min,k} + r(0,1) \times (x_{min,k} - x_{max,k}) \quad (3)$$

where,  $i$  corresponds to range  $[1, 2, \dots, n]$ ,  $k$  defines for  $[1, 2, \dots, d]$ ,  $x_{i,k}$  represents  $i^{th}$  solution for the  $k^{th}$  dimension;  $r(0,1)$  is a random number between  $[0,1]$ ;  $x_{min,k}$  and  $x_{max,k}$  denotes lower and upper boundary conditions. This phase is kept same during the execution of complete algorithm and incorporate major changes from the first generation.

## Global search phase

In the *gsp* of the proposed algorithm, for first half of the generations, original equation of basic CS are used. The equation used to represent the *gsp* of basic CS is defined as:

$$x_i^{t+1} = x_i^t + \alpha \otimes Levy(\beta)(x_{best} - x_i^t) \quad (4)$$

where  $x_i^{t+1}$  is the new solution for current iteration,  $x_i^t$  defines the solution generated in previous iteration,  $\otimes$  symbol denotes the entry wise multiplication,  $x_{best}$  is current best and step size  $\alpha > 0$  is defined by dimension  $d$  of the problem. The randomization used here is based on Lévy distribution and generated by equation (2).

Further, a new modification based on the bare-bones variant has been added in equation (4) of classical CS. The main aim of using this mechanism to generate new, highly diverse solutions and helps in improving the performance of algorithms during *expl* operation. The modified mathematical equation of the *gsp* then becomes,

$$Gx_{i,d} = W_r \times x_{new}^{t+1} + (1 - W_r) \times Cx_{i,d} \quad (5)$$

$$\text{for } Cx_{i,d} = n\left(\frac{x_{p,d}^t + q_{k,d}^t}{2}, |s_{p,d}^t - x_{q,d}^t|\right)$$

where  $Gx_{i,d}$  denotes the modified solution in *gsp* for  $d$  dimension of the problem,  $W_r$  is coefficient of weight defined in stochastic manner with range  $[0,1]$ ,  $x_{p,d}^t$  &  $x_{q,d}^t$  are two randomly selected solutions from entire population for problem dimension  $d$  and all the remaining notations used here have same relevance as provided in basic CS. The bare-bones mechanism is commonly referred to as cooperative search mechanism and used in PSO<sup>29</sup>. This mechanism uses the collaborative benefits of different search operators and hence controls the problems that occur due to one search operator. The bare-bones parameter can generate large step size during the initial iterations so that the algorithm performs better for *expl* operation. Thus, this mechanism is introduced to provide large step sizes and enhance the *expl* process of MaCN.

For the second set of iterations, more heed is paid to the *expt* operation of the algorithm and formulate new equations to make it capable for finding optimal solution. Here, the new equations have been derived from original *gspequation* of CS in combination with GWO algorithm<sup>5</sup>. These equations are used to generate new solution and mathematically defined as:

$$g_1 = x_i - M_1(N_1.x_{new} - x_i^t); \quad g_2 = x_i - M_2(N_2.x_{new} - x_i^t); \quad g_3 = x_i - M_3(N_3.x_{new} - x_i^t) \quad (6)$$

$$x_{new}^{t+1} = \frac{g_1 + g_2 + g_3}{3} \quad (7)$$

Here the new solution is denoted by  $x_{new}$  for current iteration value and  $M_1$ ,  $M_2$ ,  $M_3$  and  $N_1$ ,  $N_2$ ,  $N_3$  are derived from  $M$  and  $N$  respectively. The definition of  $M$  and  $N$  are given by:

$$M = 2m.r_1 - m; \quad N = 2.r_2 \quad (8)$$

where  $m$  decreases linearly from 2 to 0 by changes its value in accordance with iterations,  $r_1$  &  $r_2$  randomly distributed in range  $[0,1]$ . This new equation is utilized due to better *expt* properties of GWO so that the algorithm is able to exploit potential solutions in *gsp*.

### Local search phase

The *lsp* of original CS mainly deals with local random walk of search agents and governed by equation (9)

$$x_i^{t+1} = x_i^t + \alpha \otimes (\epsilon) \otimes (x_p^t - x_q^t) \quad (9)$$

where  $x_p^t$  and  $x_q^t$  are random solutions from the whole population for  $t^{th}$  iteration and the rest of the notations are the same as the *gsp*. The  $\epsilon$  parameter is randomly distributed between 0 and 1.

In the present work, only  $\epsilon$  parameter of equation (9) has been replaced by scaling factor (S)<sup>131</sup> for first half of the iterations and new parametric equation is defined as:

$$S_i^{t+1} = \begin{cases} \frac{1}{2} \times (\sin(2\pi \times f_{req} \times t + \pi) \times \frac{t_{max} - t}{t_{max}} + 1); & \text{if } r > 0.5 \\ \frac{1}{2} \times (\sin(2\pi \times f_{req} \times t) \times \frac{t_{max} - t}{t_{max}} + 1); & \text{if } r < 0.5 \end{cases} \quad (10)$$

where,  $f_{req}$  is the frequency of sine signal,  $t$  and  $t_{max}$  is the current and maximum iterations.

For the second iterative half, the MaCN algorithm is governed by a new equation. This new equation is used from breeder phase of NMRA<sup>9</sup>. From the original paper of NMRA, it has been found that NMRA exhibits good *expt* properties, and due to these properties, the breeder phase equation of NMRA is added in this phase for the second iterative half. The mathematical description of this equation is given as:

$$x_i^{t+1} = (1 - \lambda)x_i^t + \lambda(x_{best} - x_i^t) \quad (11)$$

$\lambda$  is responsible for controlling the frequency of mating with queen and based on simulated annealing (*sa*) *iw*. A detailed description of *sa iw* is given in the parameter adaptation subsection. All the other notations used in equation (11) have the same meaning as used in the *gsp*.

### Population adaptation

The *popsiz*e is a crucial parameter for optimization. When solving optimization problems, *popsiz*e multiplied by maximum iterations, gives the total function evaluations. It is important to remember that the bigger the *popsiz*e, the larger is the total number of function evaluations, and that a smaller *popsiz*e, while having fewer function evaluations, may result in local optima stagnation. A diminishing population strategy based on<sup>30</sup> is used. This method aids in initial *expl* with a full *popsiz*e, and a limited population method leads to better solutions in

the final stages. It also aids in the provision of better convergence properties and the discovery of new global optimum solutions without sacrificing the previous global best. The general equation for population adaptation is given by:

$$N_{t+1} = \begin{cases} (1 - \Delta f_t^{best})N_t, & \text{if } \Delta f_t^{best} \leq \Delta f_{max}^{best} \\ (1 - \Delta f_{max}^{best})N_t, & \text{if } \Delta f_t^{best} > \Delta f_{max}^{best} \\ \min_N, & \text{if } N_{t+1} < \min_N \end{cases} \tag{12}$$

where  $N_{t+1}$  is the *popsiz*e at generation  $t$ ,  $\Delta f_t^{best}$  is given by  $(\frac{f_{t-1}^{best} - f_{t-2}^{best}}{|f_{t-2}^{best}|})$  is the change in the best fitness,  $\Delta f_{max}^{best}$  is the threshold. Also, a minimum *popsiz*e has been established to mitigate the negative consequences of smaller population levels. The overall shape is an exponential curve at first, followed by a steady state, and finally an exponential drop. It's worth noting that there's no need to define a user-based pattern.

Parametric adaptations

Overall, in present work there are two major parameters; i) Switch probability (*pa*) of CS algorithm, ii) NMRA's mating factor ( $\lambda$ ). These parameters are made adaptive with the help of five *iw*. These *iw* help in balancing *expl* and *expt* phases of algorithm<sup>132</sup>. Here, five types of *iw* namely simulated annealing (*sa*) *iw*, exponential decreasing (*exp*) *iw*, linear decreasing (*linear*) *iw*, chaotic *iw* and logarithmic decreasing (*log*) *iw* are used for parametric analysis of MaCN algorithm. The mathematical description of these *iw* are presented in Table 1

Greedy selection

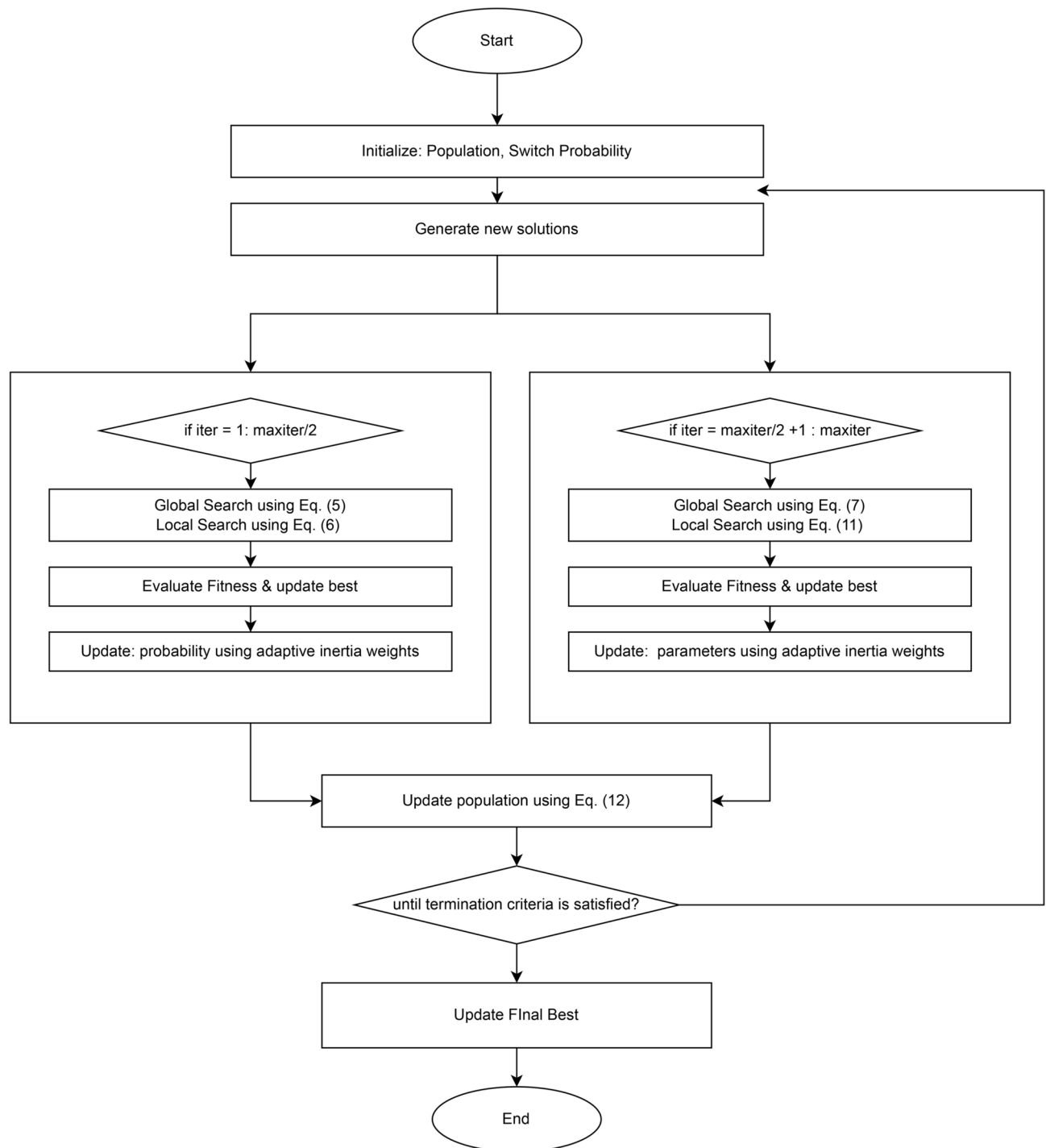
The final phase of optimization algorithm is selection of newly generated solution. For proposed algorithm MaCN, selection procedure is greedy in nature and newly generated solution is compared with solution of previous generation. So, if the new solution is more fit than the previous solution, then the new solution is replaced by the previous solution. The mathematical equation to present greedy selection procedure is given as:

$$S_{new}^{t+1} = \begin{cases} S_{new} & \text{if } f(S_{new}) < f(S_i^t) \\ S_i^t & \text{otherwise} \end{cases} \tag{13}$$

where  $S_{new}^{t+1}$  is the solution generated in current  $t + 1$  iteration,  $S_i^t$  defines the solution generated in previous iteration and  $f(S_i^t)$  represents the fitness value for  $S_i^t$  solution. The pseudocode of the proposed MaCN is presented in Algorithm 1, and the flow chart is given in Figure 2.

S.No	Inertia Weight	Mathematical Description	Initial values	Significance
1	sa <sup>133</sup>	$\gamma_k = \gamma_{min} + (\gamma_{max} - \gamma_{min}) \times r^{(k-1)}$	$\gamma_{max}, \gamma_{min}, k = rand[0, 1]$ $r = 0.95$	Improve convergence rate
2	exp <sup>134</sup>	$\gamma(iter) = \gamma_{min} + (\gamma_{max} - \gamma_{min})exp\left[-\frac{iter}{(\frac{t_{max}}{10})}\right]$	$\gamma_{max}, \gamma_{min} = rand[0, 1]$ $iter =$ current iteration $t_{max} =$ maximum iterations	Algorithm convergence faster during initial stages
3	linear <sup>135</sup>	$\gamma_k = \gamma_{max} - \left(\frac{\gamma_{max} - \gamma_{min}}{t_{max}}\right) \times k$	$\gamma_{max}, \gamma_{min}, k = rand[0, 1]$ $t_{max} =$ maximum iterations	Algorithm work efficiently in <i>expt</i> phase
4	chaotic <sup>136</sup>	$\gamma_k = (\gamma_1 - \gamma_2) \times \frac{t_{max} - iter}{t_{max}} + \gamma_2 \times k$	$\gamma_1 = 0.9; \gamma_2 = 0.4$ $k = 4 \times k \times (1 - k)$	Explore search space efficiently
5	log <sup>137</sup>	$\gamma(iter) = \gamma_{max} + (\gamma_{min} - \gamma_{max}) \times log_{10}\left(k + \frac{10 \times iter}{t_{max}}\right)$	$\gamma_{max}, \gamma_{min}, k = rand[0, 1]$ $iter =$ current iteration $t_{max} =$ maximum iterations	Avoid local optima stagnation problem

Table 1. Description of various inertia weights.



**Fig. 2.** Flow Chart of the proposed MaCN algorithm.

---

```

1: Begin
2: Define: size of population ( $N$ ); switching probability ( $pa$ );
3: if  $i = 1$ : maximum iterations then
4:   global search using Eqn. (5)
5:   local search using Eqn. (9)
6:   evaluate fitness using Eqn. (13)
7:   update  $N$  using Eqn. (12)
8:   update  $pa$  using different  $iw$ 
9: else
10:  global search using Eqn. (7)
11:  local search using Eqn. (11)
12:  evaluate fitness using Eqn. (13)
13:  update  $N$  using Eqn. (12)
14:  update  $p$  using different  $iw$ 
15:  update  $\lambda$  using different  $iw$ 
16: close;
17: update final best
18: End

```

---

**Algorithm 1.** Pseudocode of proposed MaCN algorithm

---

### Computational complexity

The complexity of the developed MaCN is based on the complexity of traditional CS, NMRA, and bare-bones, and it is given as follows.

$$O(MaCN) = (N) \times O(CS) \times (O(NMRA) + O(bare - bones)) \quad (14)$$

where, the time complexity of the used CS optimizer is given in Equation (15), for NMRA is shown in Equation (16), and for bare-bones is given in Equation (17).

$$O(CS) = O(N \times (t \times Dim + 1)) \quad (15)$$

$$O(NMRA) = O(N \times Dim) \quad (16)$$

$$O(bare - bones) = O(N \times Dim) \quad (17)$$

Therefore, the complexity of the MaCN is given.

$$O(MaCN) = O(t \times N \times (Dim + N)) \quad (18)$$

where,  $t$  is the iteration counter,  $N$  as the maximum solutions, and  $Dim$  presents the problem dimension.

It is clear from the time complexity analysis that the proposed MaCN does not take more complexity compared to other basic methods. The primary process, like the solutions initialization and solutions evaluation, is almost the same as the basic method. However, the maximum time complexity of MaCN is acceptable and does not exceed other methods.

### Results and discussion

Here, to analyse the performance, two datasets (CEC 2005 and CEC 2014) from CEC competitions and steel frame design optimization problems are taken into consideration. The section is broadly classified into 7 subsections. The definition of CEC 2005 test suite is presented in the first subsection, and detail regarding various parameters of different NIAs is given in the second. The parametric analysis of the proposed MaCN is in the third subsection. In the fourth subsection, sensitivity to dimension size has been analyzed for 5 different values. After performing the parametric and dimensional analysis, the fifth and sixth subsections deal with the performance analysis of the proposed MaCN for the CEC 2005 test suite and for the highly complex CEC 2014 test suite. The seventh subsection deals with a comparative analysis of real frame design optimization problems.

All the results are simulated on HP 14 notebook, AMD Ryzen 5 processor, 8GB RAM, 64-bit Windows 10 and MATLAB 2016a.

#### Description of CEC 2005 test suite

This section gives the definition of CEC 2005 test suite<sup>31</sup> to test the performance of MaCN. This test suite mainly consist of two types of functions as presented in Table 2. Firstly, Unimodal functions (G1 to G7) having single global minimum, are used to check algorithm effectiveness to perform the *expt* phase. In order to check the convergence of the algorithm for *expl* operations, multi-modal benchmarks (G8 to G12) are used. The optimum fitness value of all test functions is listed in the last column of Table 2 and taken as  $f_{min} = 0$ .



Function	Dim	Range	Shift position	$f_{min}$
Uni-modal functions				
$G1(q) = \sum_{i=1}^n q_i^2$	30	$[-100, 100]$	$[-30, -30, \dots, -30]$	0
$G2(q) = \sum_{i=1}^n  q_i  + \prod_{i=1}^n  q_i $	30	$[-10, 10]$	$[-3, -3, \dots, -3]$	0
$G3(q) = \sum_{i=1}^n (\sum_{j=1}^i q_j)^2$	30	$[-100, 100]$	$[-3, -3, \dots, -3]$	0
$G4(q) = \max_i \{  q_i , 1 \leq i \leq n \}$	30	$[-100, 100]$	$[-3, -3, \dots, -3]$	0
$G5(q) = \sum_{i=1}^{n-1} 100(q_{i+1} - q_i^2)^2 + (q_1 - 1)^2$	30	$[-30, 30]$	$[-3, -3, \dots, -3]$	0
$G6(q) = \sum_{i=1}^n ([q_i + 0.5])^2$	30	$[-10, 10]$	$[-3, -3, \dots, -3]$	0
$G7(q) = \sum_{i=1}^n i q_i^4 + \text{random}[0, 1]$	30	$[-1.28, 1.28]$	$[-3, -3, \dots, -3]$	0
Multi-modal functions				
$G8(q) = \sum_{i=1}^n [q_i^2 - 10 \cos(2\pi q_i) + 10]$	30	$[-5.12, 5.12]$	$[-30, -30, \dots, -30]$	0
$G9(q) = -20 \exp(-0.2 \sqrt{\frac{1}{n} \sum_{i=1}^n q_i^2}) - \exp(\frac{1}{n} \sum_{i=1}^n \cos(2\pi q_i)) + 20 + e$	30	$[-100, 100]$	$[-30, -30, \dots, -30]$	0
$G10(q) = \frac{1}{4000} \sum_{i=1}^N q_i^2 - \prod_{i=1}^N \cos(\frac{q_i}{\sqrt{i}}) + 1$	30	$[-600, 600]$	$[-30, -30, \dots, -30]$	0
$G11(q) = \frac{\pi}{n} 10 \sin(\pi p_1) + \sum_{i=1}^n -1(p_i - 1)^2 [1 + 10 \sin^2(\pi p_{i+1})]$	30	$[-50, 50]$	$[-30, -30, \dots, -30]$	0
$(p_n - 1)^2 + \sum_{i=1}^u (q_i, 10, 100, 4) p_i = 1 = \frac{q_i+1}{4}$				
$G12(q) = 0.1(\sin^2(3\pi q_1) + \sum_{i=1}^n (q_i - 1)^2 (1 + \sin^2(3\pi q_i + 1)))$	30	$[-50, 50]$	$[-30, -30, \dots, -30]$	0
$+0.1((q_n - 1)^2 [1 + \sin^2(2\pi q_n)] + \sum_{i=1}^n u(q_i, 5, 100, 4))$				

**Table 2.** Description of CEC 2005 test functions.

Algorithm name	Parameters involved
CV 1.0 <sup>26</sup>	$\bar{\alpha}$ =Linearly decreasing [2,0]; Switch Probability ( $p_a$ )=0.5
OEWOA <sup>42</sup>	$\bar{\alpha}$ = Exponentially decreasing function; $b = 1$
SCCS <sup>37</sup>	$r_1, r_2, r_3 = [0, 1]$
PBIL <sup>52</sup>	Learning rate ( $LR$ )=0.1; Mutation probability ( $p_m$ )=0.02
ISOS <sup>47</sup>	$q \in [1, 100]\%$ , $r \in [0, 1]$
B-BBO <sup>50</sup>	$H = 1$ ; $I = 1$
GWO-E <sup>40</sup>	$\bar{\alpha}$ = Linearly decreasing from 2 to 0
FA-FPO <sup>138</sup>	$\alpha = [0.1, 1]$ , $S = \text{adaptive}$
IMEHO <sup>52</sup>	$w$ = Linearly decreasing in range [0.9,0.2]; $\alpha \in [0,1]$ ; Probability ( $p_c$ )=0.05
SaDE <sup>41</sup>	$F, CR$ = self adaptive
SHADE <sup>35</sup>	$P_{best} = 0.1$ , $ARCrate = 2$
LX-BBO <sup>50</sup>	$H = 1$ ; $I = 1$
LSHADE-SPACMA <sup>35</sup>	$c=0.8$ , $P_{best} = 0.11$ , $ARCrate = 1.4$ , $FCP=0.5$
JADE <sup>38</sup>	$F = 0.5$ ; $CR = 0.9$ ; $1/c = [5, 20]$ ; $p = [0.05, 0.20]$
EO <sup>35</sup>	$a_1 = 2$ , $a_2 = 1$ , $\text{sign}(r - 0.5)$
VNBA <sup>52</sup>	Loudness ( $A$ )=0.5; Pulse rate ( $r$ )=0.5
RW-GWO <sup>48</sup>	$\bar{\alpha}$ = Linearly decreased from 2 to 0
CCS <sup>52</sup>	Switch probability ( $p_a$ )=0.25
NMRA <sup>9</sup>	$bp = 0.5$ ; $\lambda = [0, 1]$ ;
BDE <sup>34</sup>	$F, CR$ = Beta distribution
MGSCA <sup>33</sup>	$r_1$ = adaptive; $r_2 = [0, 2\pi]$ ; $r_3$ = uniformly distributed [0,2]
MaCN	Switch probability ( $p_a$ )= Exponential decreasing; mating factor ( $\lambda$ )=sa; Population= <i>adaptive</i>

**Table 3.** Parameter selection of various algorithms under comparison.

## Parameter settings

To test the efficiency of proposed MaCN for two test suites (CEC 2005 and CEC 2014), its statistical results are analysed with other improved algorithms. In case of CEC 2005 test functions, algorithms used for comparison are CV 1.0<sup>26</sup>, NMRA<sup>9</sup>, MGSCA<sup>33</sup>, BDE<sup>34</sup>, EO<sup>35</sup>, SHADE<sup>39</sup>, CMA-ES<sup>36</sup>, LSHADE-SPACMA<sup>43</sup>, SCCS<sup>37</sup>, GWO-E<sup>40</sup>, SaDE<sup>41</sup>, JADE<sup>38</sup>, OEWOA<sup>42</sup> and FA-FPO<sup>44</sup>. On the other hand, the algorithms under comparison for CEC 2014 benchmark problems are MGSCA<sup>33</sup>, BDE<sup>34</sup>, CCS<sup>46</sup>, VNBA<sup>51</sup>, ISOS<sup>47</sup>, RW-GWO<sup>48</sup>, B-BBO<sup>49</sup>, LX-BBO<sup>50</sup>, PBIL<sup>45</sup> and IMEHO<sup>52</sup>.

The various parameters of all the above mentioned algorithms are selected from their recent literature and presented in Table 3. In the case of CV 1.0, the important parameter is switch probability ( $pa$ ) = 0.5. Apart from this, one more parameter  $\vec{\alpha}$  of GWO is added in CV 1.0 to control the *expl* and *expt* phases, which is linearly decreasing from 2 to 0. For NMRA, breeding probability ( $bp$ ) and mating factor ( $\lambda$ ) are two important parameters and value of these parameters are same as<sup>9</sup>. A detailed list of all the parameters is given in Table 3.

## Parametric analysis of MaCN

The parametric analysis of MaCN has been provided in this subsection. The MaCN algorithm has basically two parameters of major concern, namely the switch probability ( $pa$ ) of the CS algorithm and the mating factor ( $\lambda$ ) of NMRA. To perform analysis on these parameters, three different constant values (0.25, 0.50 & 0.75) and five different adaptive *iw* (*sa*, *exp*, *linear*, *chaotic* & *log*) are used for 7 uni-modal benchmarks (G1 to G7) and 5 multi-modal benchmarks (G8 to G12) of CEC 2005<sup>31</sup> test suite. The results are simulated for 30 dimension size, 500 iterations and presented in mean & standard deviation (*std*) of 51 runs as in Table 4. So the total number of function evaluations in this case are  $30 \times 500 = 15000$ . The dependence of these parameters on the performance of MaCN are discussed as:

**Analysis of CS parameter:** The important ( $pa$ ) parameter of CS algorithm controls *expl* and *expt* operations. Here, three different constant values and five different adaptive *iw* are associated with this parameter for analyzing the performance of MaCN. From the Table 4, it has been analyzed that parameter  $pa$  with *exp*, and *log iw* provide almost same and best results for all the benchmark functions. So, finally *exp iw*-based  $pa$  parameter has been selected for further simulations after performing detailed analysis for MaCN algorithm.

**Analysis of NMRA parameter:** The main parameter of NMRA is ( $\lambda$ ) and found useful in the implementation of *lsp* equation of the proposed MaCN algorithm. Here, ability of proposed MaCN algorithm has been analyzed for three constant values and five *iw* applied to this parameter and is given in Table 4. Here we find that results are similar for all the cases and efficiency of MaCN algorithm is not much affected by variation in  $\lambda$  parameter. However, finally, *sa iw* is considered for this parameter because *sa iw* helps the algorithm explore a particular area of search space in exploring certain sections.

## Dimension size analysis

The problem's dimension size (*Dim*) is important for evaluating the efficiency of any optimization procedure. The performance of MaCN with respect to CV 1.0 and NMRA is examined in this subsection for 5 dimension sizes (10, 50, 100, 200, and 500). Dimensional analysis was used to see if MaCN might provide an optimal solution of objective functions for higher dimensions (CEC 2005). The statistical findings for all sets of dimension sizes are in Table 5 as mean and *std* of 51 runs and 500 iterations. The following is a full study of these results for various dimension sizes:

**Dimension size 10:** The simulation results for *Dim* = 10 are shown in Table 5, and it was discovered that only MaCN delivers a solution close to the optimal value for G1, G2, G3, and G4. The MaCN results are zero and the same as the global minimal value in G5 and G8. Compared to CV 1.0 and NMRA, MaCN is more efficient for G6, G7, G11, and G12. Finally, NMRA and MaCN show the same performance for G9 and G10, making it competitive to choose the optimal algorithm for these functions. Apart from simulated results, convergence profiles are also drawn and shown in Figure 3. As a result, MaCN is considered the best algorithm in this scenario.

**Dimension Size 50:** Table 5 displays the statistical results for *Dim* = 50. MaCN is the best algorithm for G1, G2, G3, and G4, and no other algorithm can match it. MaCN provides a global minimum solution for G5. Compared to NMRA and CV 1.0, MaCN produces better for G6, G7, G11, and G12. Finally, the NMRA and MaCN values for G8, G9, and G10 are identical, with a zero standard deviation value. Figure 4 shows the convergence profiles for this dimension size. As a result, the MaCN results are again found to be appropriate here.

**Dimension Size 100:** Table 5 shows the results for this set of dimension sizes, and MaCN obtains mean values that are close to the ideal for G1 and G3. The MaCN results for functions G2 and G4 are practically identical. MaCN provides the minimal global solution for G5. Compared to NMRA and CV 1.0, MaCN performs much better for G6, G7, G11, and G12. Both NMRA and MaCN have zero results for G8 and G10. MaCN and NMRA results for the last function G9 are near-global minima values (i.e.0). As a result, MaCN is once again the best choice for *Dim* = 100 and convergence profiles shown in Figure 5 validate it.

**Dimension Size 200:** Table 5 shows the simulated results for *Dim* = 200, and here results by MaCN are exactly zero and the same as the optimal value of the functions for G1, G3, and G5. When compared to CV 1.0 and NMRA, MaCN is more capable for G2 and G4. The MaCN method is determined as best for G6, G7, G11, and G12. Both MaCN and NMRA identical solutions for G8 and G10. Both MaCN and NMRA produce the best and similar outcomes in the last for G9. Overall, MaCN outperformed the competition in this scenario.

**Dimension Size 500:** Table 5 shows the results for *Dim* = 500 and shows that MaCN finds the best results for G1, G3, and G5. MaCN has the best performance in the G2 and G4 cases. Only MaCN can approach optimum outcomes for G6, G7, G11, and G12. The findings of MaCN, CV 1.0, and NMRA for G8 and G10 are identical

Simulation results for different cases of CS switching probability parameter ( $pa$ )									
Function		$pa_{0.25}$	$pa_{0.50}$	$pa_{0.75}$	$pa_{sa}$	$pa_{exp}$	$pa_{linear}$	$pa_{chaotic}$	$pa_{log}$
G1	Mean	3.49E-269	3.63E-262	5.37E-256	1.37E-251	5.91E-264	4.51E-256	3.46E-256	1.25E-263
	Std	0	0	0	0	0	0	0	0
G2	Mean	1.20E-134	1.41E-131	1.29E-129	2.05E-126	9.76E-132	1.33E-128	1.02E-128	4.80E-132
	Std	3.77E-134	9.25E-131	4.85E-129	1.00E-125	6.22E-131	8.36E-128	4.25E-128	0
G3	Mean	6.33E-266	5.04E-263	3.11E-257	3.82E-251	1.07E-262	2.12E-255	1.95E-255	3.93E-264
	Std	0	0	0	0	0	0	0	0
G4	Mean	2.00E-134	3.41E-132	8.15E-130	4.88E-127	4.79E-132	1.13E-128	3.87E-129	1.60E-132
	Std	9.87E-134	1.59E-131	3.77E-129	2.19E-126	1.62E-131	4.55E-128	1.38E-128	4.65E-132
G5	Mean	0	0	0	0	0	0	0	0
	Std	0	0	0	0	0	0	0	0
G6	Mean	1.74E-31	4.75E-26	3.58E-19	2.01E-14	1.10E-25	1.72E-17	2.69E-18	1.08E-25
	Std	4.17E-31	9.13E-26	5.58E-19	4.22E-14	2.23E-25	4.91E-17	6.37E-18	2.65E-25
G7	Mean	1.16E-05	1.44E-05	1.61E-05	1.79E-05	1.43E-05	1.72E-05	1.36E-05	1.59E-05
	Std	9.49E-06	1.21E-05	1.05E-05	1.40E-05	1.48E-05	1.44E-05	1.05E-05	1.23E-05
G8	Mean	0	0	0	0	0	0	0	0
	Std	0	0	0	0	0	0	0	0
G9	Mean	8.87E-16	8.87E-16	8.87E-16	8.87E-16	8.87E-16	8.87E-16	8.87E-16	8.87E-16
	Std	0	0	0	0	0	0	0	0
G10	Mean	0	0	0	0	0	0	0	0
	Std	0	0	0	0	0	0	0	0
G11	Mean	1.18E-22	5.76E-19	9.08E-15	3.47E-12	5.25E-19	3.11E-14	1.34E-15	3.86E-19
	Std	2.83E-22	1.76E-18	3.46E-14	5.57E-12	1.25E-18	5.27E-14	3.37E-15	8.12E-19
G12	Mean	5.48E-28	3.06E-23	4.58E-18	1.09E-13	6.00E-23	1.20E-16	1.43E-17	3.88E-23
	Std	1.60E-27	9.52E-23	8.95E-18	1.85E-13	1.92E-22	2.61E-16	2.67E-17	9.04E-23
Simulation results for different cases of NMRA breeding factor parameter ( $\lambda$ )									
Function		$\lambda_{0.25}$	$\lambda_{0.50}$	$\lambda_{0.75}$	$\lambda_{sa}$	$\lambda_{exp}$	$\lambda_{linear}$	$\lambda_{chaotic}$	$\lambda_{log}$
G1	Mean	3.76E-262	1.03E-263	1.46E-264	6.77E-263	7.62E-263	2.85E-263	8.09E-259	1.92E-263
	Std	0	0	0	0	0	0	0	0
G2	Mean	1.13E-132	6.77E-132	2.69E-132	5.49E-132	3.17E-132	1.21E-132	6.68E-132	2.25E-132
	Std	4.42E-132	4.43E-131	7.94E-132	1.93E-131	9.89E-132	2.72E-132	2.86E-131	7.00E-132
G3	Mean	7.34E-264	1.34E-261	6.41E-264	2.40E-264	2.68E-263	2.38E-262	1.36E-264	8.60E-263
	Std	0	0	0	0	0	0	0	0
G4	Mean	5.11E-132	1.12E-132	4.88E-132	3.93E-132	8.25E-132	1.09E-132	3.79E-132	8.06E-133
	Std	2.82E-131	3.53E-132	2.95E-131	2.16E-131	4.26E-131	3.87E-132	1.46E-131	2.58E-132
G5	Mean	0	0	0	0	0	0	0	0
	Std	0	0	0	0	0	0	0	0
G6	Mean	2.66E-25	1.42E-25	3.88E-25	2.66E-25	5.96E-26	1.64E-25	8.88E-26	9.14E-26
	Std	7.55E-25	3.75E-25	9.40E-25	1.21E-24	1.18E-25	5.87E-25	2.94E-25	2.60E-25
G7	Mean	1.81E-05	1.79E-05	1.81E-05	1.68E-05	1.59E-05	1.68E-05	1.49E-05	1.46E-05
	Std	1.98E-05	1.25E-05	1.52E-05	1.49E-05	1.64E-05	1.08E-05	1.10E-05	1.48E-05
G8	Mean	0	0	0	0	0	0	0	0
	Std	0	0	0	0	0	0	0	0
G9	Mean	8.87E-16	8.87E-16	8.87E-16	8.87E-16	8.87E-16	8.87E-16	8.87E-16	8.87E-16
	Std	0	0	0	0	0	0	0	0
G10	Mean	0	0	0	0	0	0	0	0
	Std	0	0	0	0	0	0	0	0
G11	Mean	5.33E-19	5.61E-19	4.62E-19	1.43E-18	1.60E-18	5.47E-19	3.07E-19	1.57E-18
	Std	1.91E-18	1.53E-18	9.31E-19	2.74E-18	9.21E-18	1.16E-18	7.38E-19	6.12E-18
G12	Mean	6.76E-23	5.83E-23	7.83E-23	2.88E-23	6.97E-23	1.03E-22	4.53E-23	6.17E-23
	Std	2.12E-22	1.06E-22	2.84E-22	7.66E-23	1.94E-22	3.79E-22	1.04E-22	2.30E-22

Table 4. Parametric analysis of MaCN.

Function	Algorithm	Dim = 10		Dim = 50		Dim = 100		Dim = 200		Dim Size 500	
		Mean	Std	Mean	Std	Mean	Std	Mean	Std	Mean	Std
G1	CV 1.0	7.81E-108	5.55E-107	7.64E-87	4.88E-86	1.88E-79	1.34E-78	4.61E-79	2.15E-78	1.05E-76	7.03E-76
	NMRA	1.56E-83	1.09E-82	1.48E-85	1.05E-84	1.04E-85	5.85E-85	1.64E-83	1.03E-83	9.23E-86	4.70E-84
	MaCN	4.45E-257	0	5.12E-271	0	2.01E-289	0	0	0	0	0
G2	CV 1.0	2.57E-59	1.48E-58	1.16E-18	8.32E-18	1.96E+08	1.40E+09	3.92E+08	1.96E+09	1.37E+09	3.47E+09
	NMRA	2.49E-46	1.02E-45	7.75E-45	3.58E-44	1.71E-43	8.03E-43	2.60E-44	1.54E-43	4.25E-44	3.00E-43
	MaCN	1.22E-128	3.23E-128	2.17E-129	6.66E-129	1.15E-146	3.46E-146	1.22E-199	0	2.74E-293	0
G3	CV 1.0	5.22E-14	1.94E-13	1.50E+03	5.87E+02	9.48E+03	1.71E+03	4.06E+04	8.12E+03	3.09E+05	5.20E+04
	NMRA	8.28E-87	4.71E-86	1.00E-87	4.80E-87	9.14E-86	6.33E-85	7.13E-86	3.96E-85	5.42E-82	3.86E-81
	MaCN	3.32E-257	0	4.46E-254	0	1.02E-288	0	0	0	0	0
G4	CV 1.0	2.72E-45	1.76E-44	1.22E-33	6.45E-33	8.75E-30	6.15E-29	1.39E-28	4.58E-28	5.62E-24	2.80E-23
	NMRA	3.50E-45	1.08E-44	2.06E-44	6.86E-44	2.31E-44	1.37E-43	3.01E-45	9.54E-45	5.83E-45	2.12E-44
	MaCN	2.37E-128	9.74E-128	3.21E-130	7.84E-130	1.91E-146	1.04E-145	4.35E-199	0	2.37E-292	0
G5	CV 1.0	1.13E+00	1.17E+00	4.64E+01	6.86E-01	9.70E+01	5.85E-01	1.97E+02	4.60E-01	4.95E+02	3.16E-01
	NMRA	8.96E+00	1.81E-02	4.89E+01	2.05E-02	9.89E+01	2.55E-02	1.98E+02	2.77E-02	4.97E+02	1.81E-02
	MaCN	0	0	0	0	0	0	0	0	0	0
G6	CV 1.0	5.75E-07	2.76E-07	4.63E-01	2.07E-01	2.97E+00	6.80E-01	1.08E+01	1.89E+00	4.61E+01	6.18E+00
	NMRA	1.40E+00	6.96E-01	1.16E+01	6.91E-01	2.42E+01	5.03E-01	4.91E+01	7.11E-01	1.24E+02	5.92E-01
	MaCN	7.82E-22	1.80E-21	8.26E-13	1.52E-12	1.84E-14	2.60E-14	2.41E-14	4.74E-14	6.50E-28	1.20E-27
G7	CV 1.0	5.75E-04	4.60E-04	7.92E-04	6.06E-04	6.95E-04	5.45E-04	9.83E-04	7.55E-04	9.32E-04	6.28E-04
	NMRA	8.09E-04	8.34E-04	5.21E-04	4.67E-04	6.43E-04	5.83E-04	5.98E-04	5.72E-04	8.32E-04	8.74E-04
	MaCN	4.12E-05	3.25E-05	1.23E-05	9.90E-06	5.57E-06	4.76E-06	3.40E-06	2.74E-06	2.26E-06	1.41E-06
G8	CV 1.0	4.64E+00	5.07E+00	1.80E+02	1.25E+02	8.27E+01	2.29E+02	3.92E-02	2.79E-01	0	0
	NMRA	5.22E-01	3.73E+00	0	0	0	0	0	0	0	0
	MaCN	0	0	0	0	0	0	0	0	0	0
G9	CV 1.0	1.02E-15	6.96E-16	1.44E-15	1.30E-15	1.72E-15	1.52E-15	1.72E-15	1.52E-15	2.00E-15	1.66E-15
	NMRA	8.87E-16	0	8.87E-16	0	8.87E-16	0	8.87E-16	0	8.87E-16	0
	MaCN	8.87E-16	0	8.87E-16	0	8.87E-16	0	8.87E-16	0	8.87E-16	0
G10	CV 1.0	0	0	0	0	0	0	0	0	0	0
	NMRA	0	0	0	0	0	0	0	0	0	0
	MaCN	0	0	0	0	0	0	0	0	0	0
G11	CV 1.0	4.61E-07	2.94E-07	1.06E-02	4.00E-03	2.81E-02	7.70E-03	5.74E-02	1.79E-02	1.20E-01	2.52E-02
	NMRA	6.77E-01	3.41E-01	1.16E+00	1.51E-01	1.19E+00	8.62E-02	1.19E+00	4.54E-02	1.17E+00	1.51E-02
	MaCN	1.82E-16	3.10E-16	9.74E-11	1.99E-10	1.60E-12	3.05E-12	2.87E-12	4.49E-12	3.32E-21	5.25E-21
G12	CV 1.0	8.63E-04	3.00E-03	5.30E-01	2.12E-01	2.01E+00	5.18E-01	6.48E+00	1.51E+00	1.36E+09	3.46E+09
	NMRA	8.83E-01	1.93E-01	4.98E+00	2.90E-03	9.99E+00	3.00E-03	1.99E+01	2.20E-03	4.99E+01	2.50E-03
	MaCN	1.68E-19	6.47E-19	3.15E-11	7.37E-11	7.97E-13	8.14E-12	1.18E-12	2.44E-12	1.05E-25	1.96E-25

**Table 5.** Comparison of CV 1.0, NMRA and MaCN for five dimension sizes (10, 50, 100, 200 and 500).

and same as global optimal value. Finally, MaCN and NMRA values for G9 are identical and better than CV 1.0. As a result, MaCN is thought to be the best method for solving higher-dimensional problems.

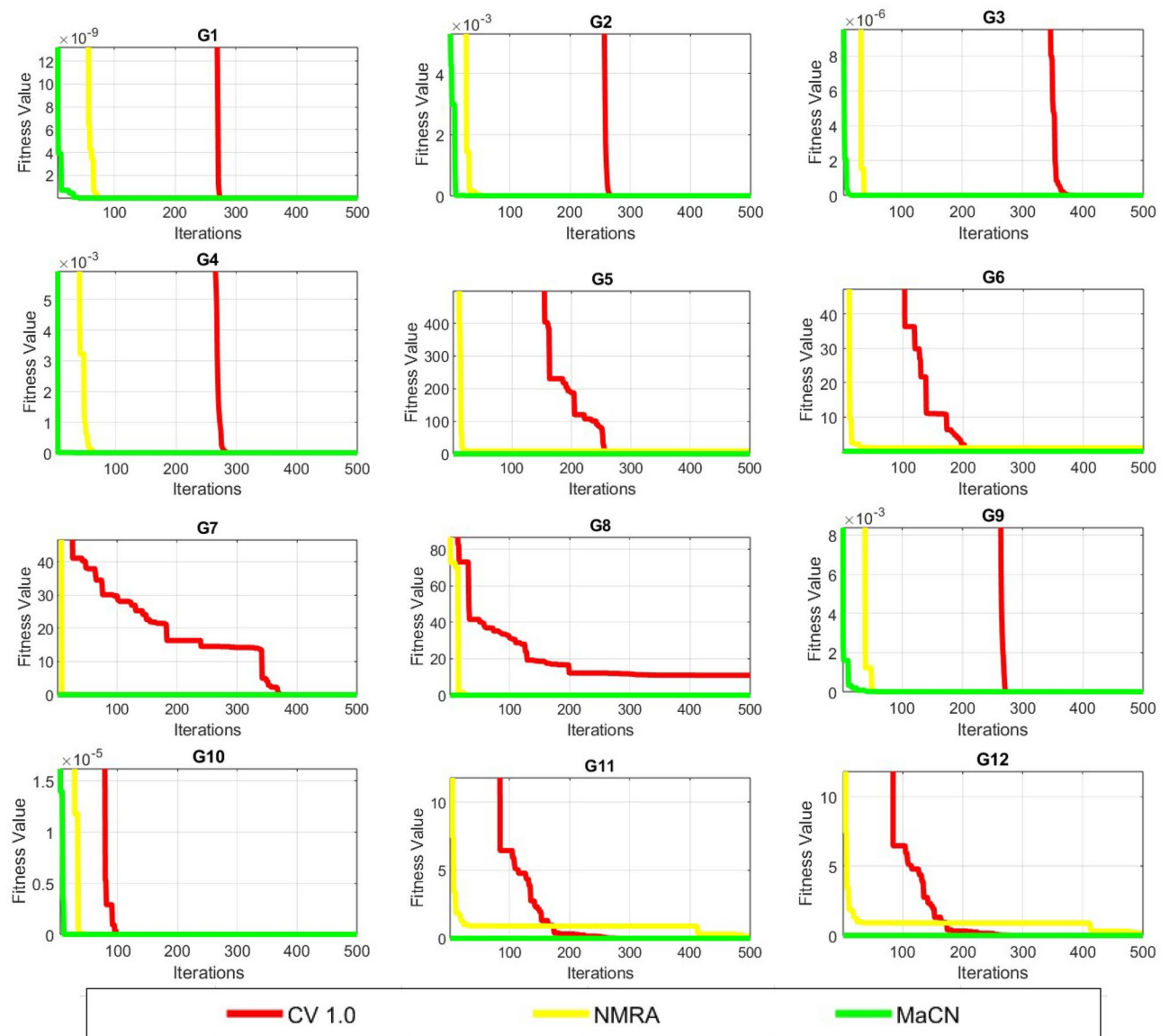
*Inferences:* From the results for lower dimension, the algorithm shows significant performance. But as the dimension size increases, the results degrade due to increase in the computational complexity. Overall, it can be said that with increase in dimension size, the results do vary a little but the overall performance do not degrade much.

### Performance evaluation for CEC 2005 test suite in comparison with other algorithms

The capability of proposed MaCN algorithm is tested in this subsection by doing comparison with various algorithms such as SHADE, FA-FPO, JADE, GWO-E and others. These algorithms are found to be very competitive and capable in solving complex problems of optimization. The selection of parameter values is provided in Table 3. Here, CEC 2005 test functions are used as benchmark for evaluating performance of MaCN with  $Dim = 30$ , and definition of these test functions are provided in Table 2.

#### Experimental testing

Table 6 contains results for all the algorithms. Only MaCN can give near-optimal global solutions for G1, G2, G3, and G4, as shown by the findings. MaCN achieves global minima for G5, while all others couldnot. MaCN outperforms G6 in terms of mean and std. The results of FA-FPO and MaCN in the situation of G7 are fairly competitive, but MaCN is the best in this scenario. FA-FPO, GWO-E, OEWOA, EO, MGSCA, and suggested



**Fig. 3.** Convergence profiles of CV 1.0, NMRA and MaCN for Dimension Size 10.

MaCN all produce comparable and ideal outcomes for G8. In the instance of G9, FA-FPO and MaCN function equally well. GWO-E, FA-FPO, EO, and MaCN obtain the best global value for G10. Finally, MaCN outperforms others for G11 and G12. MaCN is optimal for all functions, FA-FPO for three, OEWOA and MGSCA for one, and EO and GWO-E for two, according to the 12 test functions.

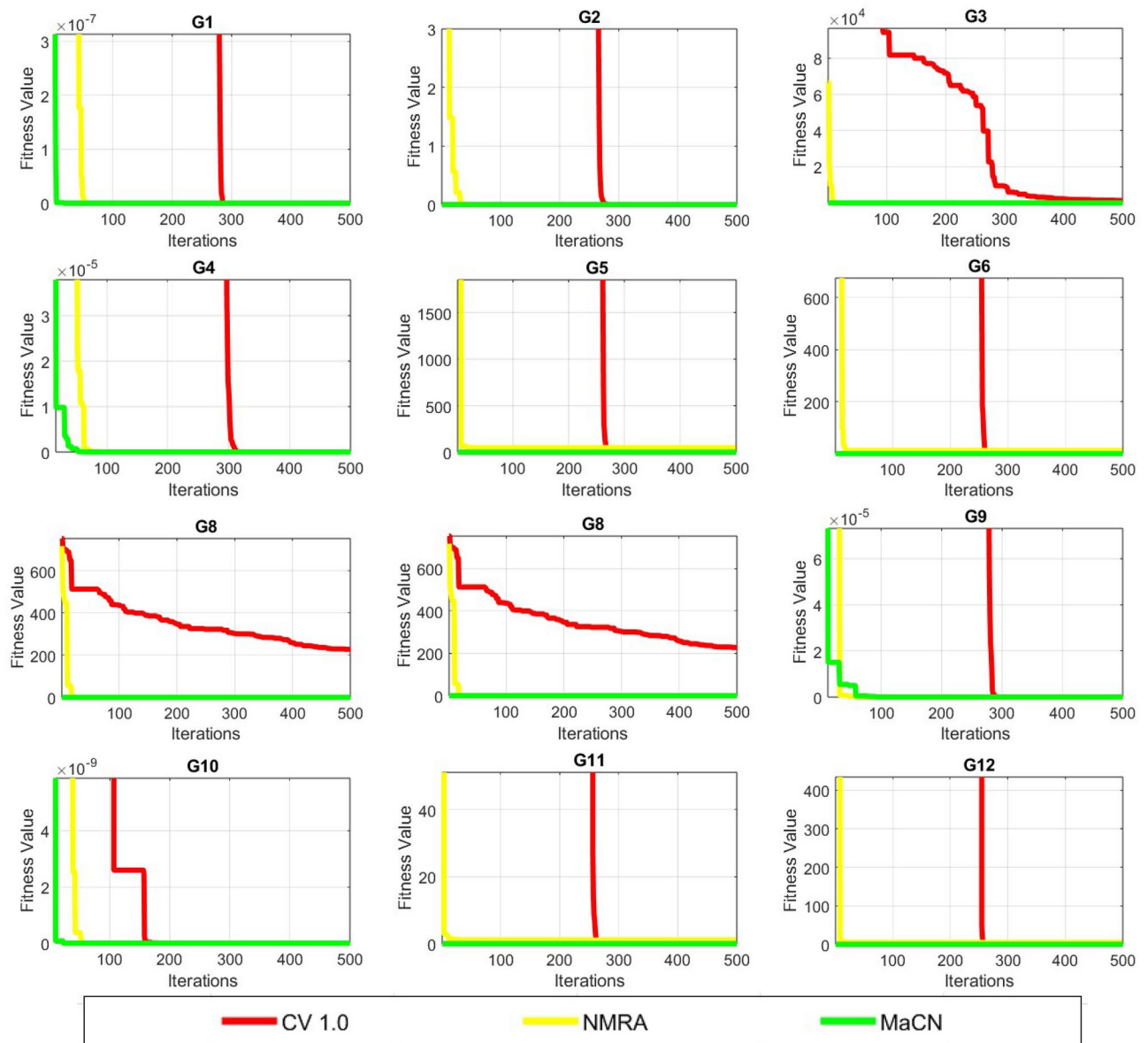
#### Statistical testing

Here wilcoxon's rank-sum test<sup>139</sup> and Friedman rank ( $f$ -rank)<sup>47</sup>, are used to statistically validate the MaCN algorithm's simulated findings. These tests helps to find the statistical significance of an algorithm and are described as:

**Wilcoxon's ran-sum test:** This test uses a  $win(w)/loss(l)/tie(t)$  strategy to find the best algorithm under consideration. A p-rank is assigned to each of the algorithm and the algorithm with the lowest rank is considered as the winner. Here  $win(w) = +$  means that the algorithm outperforms the proposed MaCN,  $loss(l) = -$  means MaCN outperforms the test algorithm, and  $tie(t) ==$  means both have the similar performance. The results for this test is given in Table 6, and MaCN scores the best among all in majority of the cases.

**Friedman rank test:** This test gives a rank ( $f$ -rank) to each of the algorithm ranging from 1 to the maximum number of algorithms under test. The algorithm with the least rank is treated as the best. Table 6 shows that among all the cases, the MaCN algorithm scores the first rank for the average and overall  $f$ -rank.





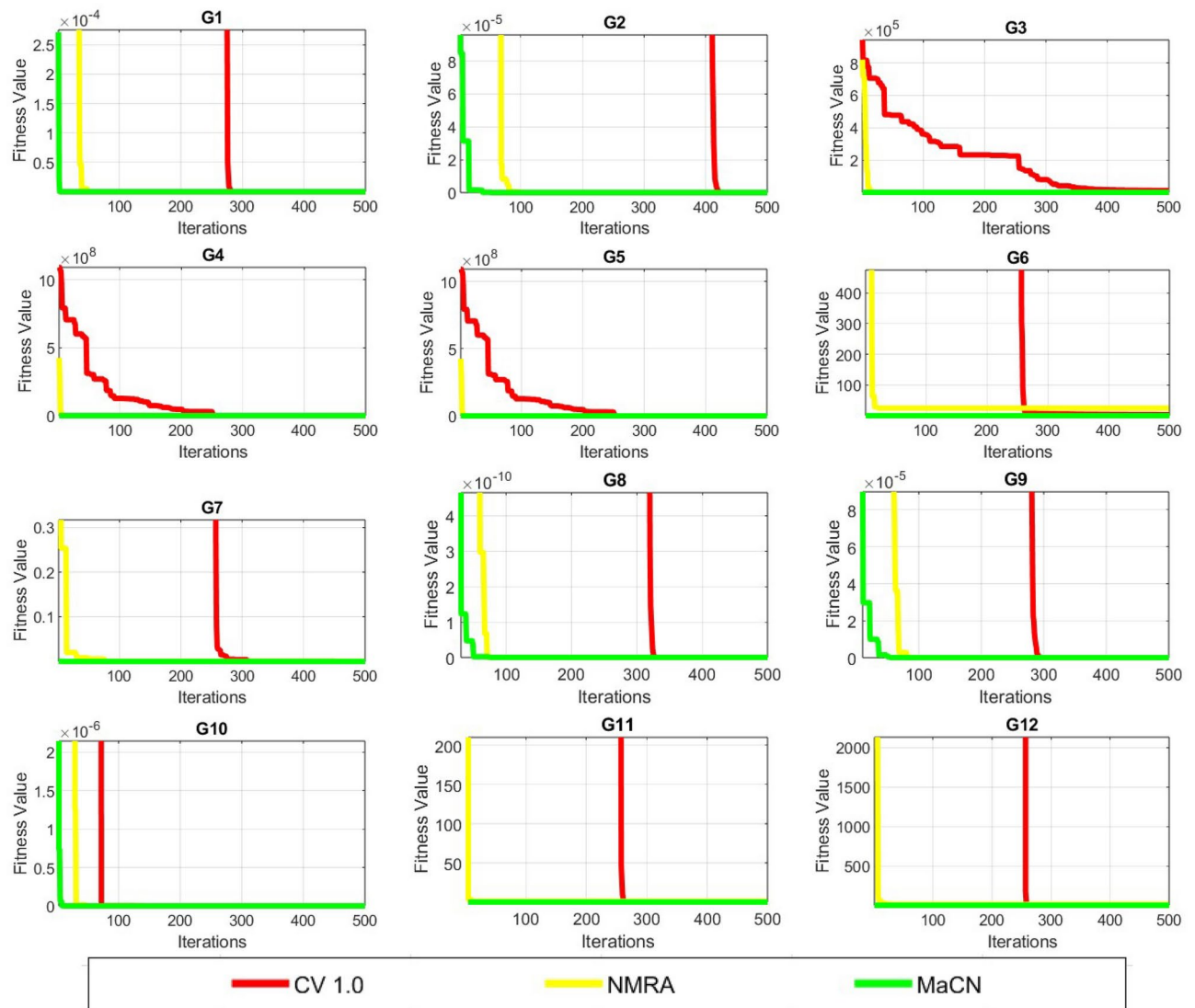
**Fig. 4.** Convergence profiles of CV 1.0, NMRA and MaCN for Dimension Size 50.

#### Convergence profiles and box-plots

To analyze the convergence behavior of CV 1.0, NMRA, and proposed MaCN, the convergence graphs are drawn for 7 uni-modal (G1 to G7) and 5 multi-modal (G8 to G12) functions of CEC 2005 benchmark suite as shown in Figure 6. From this figure, we see that MaCN converges faster as compared to CV 1.0 and NMRA for G1, G3, G4, G9, G10, G11 and G12. For G2, NMRA converges during the initial iterations, but MaCN and CV 1.0 converge later. For G5, G7, and G8, the convergence of MaCN and NMRA are almost similar while CV 1.0 converges at a slower rate during iterations. For function G6, MaCN attains a global minimal value in the early stages, but NMRA cannot converge towards the end. So, overall, it can be said that MaCN shows better convergence in most cases than CV 1.0 and NMRA. In addition to convergence profiles, Figure 7 presents box-plots that compare the fitness values of CV1, NMRA and the proposed MaCN. The results demonstrate that MaCN is more cost-effective in terms of fitness, as evidenced by its lower median fitness value compared to the other algorithms.

#### Comparison of proposed approach for CEC2014 test suite

To prove the effectiveness of proposed MaCN algorithm, it is further tested on challenging CEC 2014 test problems<sup>140</sup> and definition of these problems are available in<sup>132</sup>. For these benchmark functions, total function evaluations are set to  $10^4 \times Dim^{140}$ . Here, performance of MaCN is compared with different improved meta-heuristic algorithms such as VNBA, RW-GWO, LX-BBO, MGSCA and others. The parameter selection of all the algorithms under comparison are listed in Table 3.



**Fig. 5.** Convergence profiles of CV 1.0, NMRA and MaCN for Dimension Size 100.

MaCN's statistical findings for CEC 2014 benchmark issues are reported as mean error and *std* values for 51 independent algorithm runs with  $Dim = 30$ . Refer to 7 for a summary of these findings. ISOS performs well in the  $F_1$ ,  $F_2$ , and  $F_{24}$  categories, according to this table. MaCN's results are close to optimal in the instance of  $F_3$ . RW-GWO and MaCN both have good results for  $F_4$ , but RW-GWO is the best overall. LX-BBO has the best performance for  $F_5$  based on mean error values. MaCN is found to be the best given only mean values for  $F_6$ ,  $F_{10}$ ,  $F_{11}$ , and  $F_{16}$ . IMEHO's mean error value is the same as optimum value for  $F_7$ ,  $F_{13}$ ,  $F_{14}$ , and  $F_{15}$ . B-BBO outperforms its competitors in  $F_8$ . IMEHO produces good results in the cases of  $F_9$  and  $F_{26}$ . B-BBO and LX-BBO are the best and identical outcomes for  $F_{12}$ . The suggested algorithm performs well for  $F_{17}$ ,  $F_{18}$ ,  $F_{19}$ ,  $F_{20}$ ,  $F_{21}$ ,  $F_{22}$ ,  $F_{23}$ , and  $F_{30}$  in both mean error and *std* values. Finally, MaCN can reach global minima for *std* values for  $F_{25}$ ,  $F_{27}$ ,  $F_{28}$ , and  $F_{29}$ . Thus, ISOS outperforms RW-GWO for three functions, IMEHO for six, B-BBO and LX-BBO for two functions, and proposes MaCN for seventeen functions from the 30 benchmark tasks of the CEC 2014 test suite. The findings of various algorithms are also validated using the f-rank statistical test. After assigning a rank to each method under test, the average and overall f-rank are computed and displayed in Table 7. It can be seen that MaCN is ranked first and outperforms all of the competing algorithms.

### Real world problem: Frame structure design

The design of frame structures is one of the most significant challenges in structural engineering and offers a wide range of design flexibility<sup>141,142</sup>.

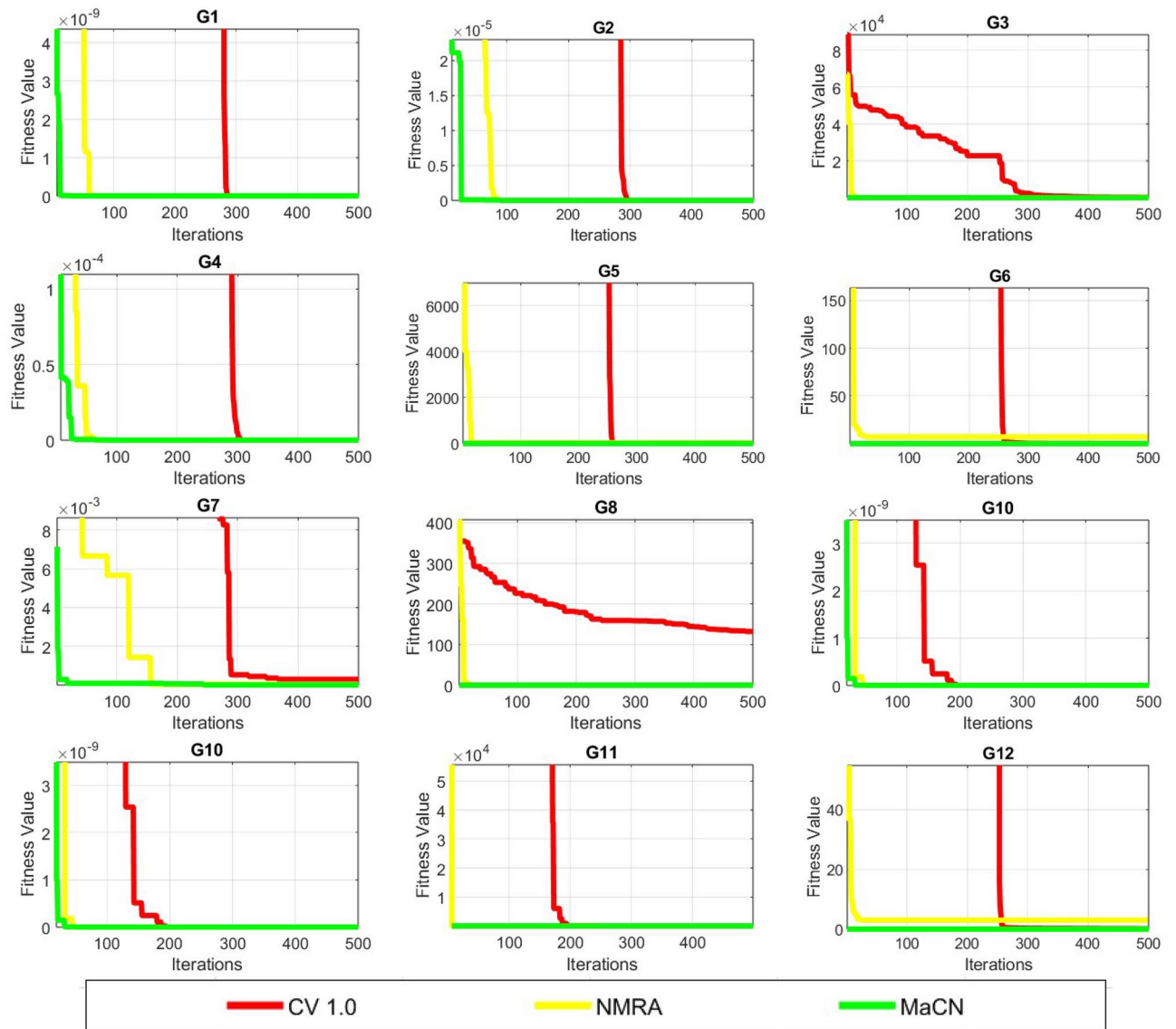
The general equation for optimal frame design is expressed as

$$\text{Find } S = [s_1, s_2, \dots, s_{dv}] \quad (19)$$

Function	JADE	SaDE	GWO-E	OEWOA	SCCS	FA-FPO	CMA-ES	SHADE	LSHADE-SPACMA	EO	BDE	MGSCA	MaCN
G1	mean	1.80E-60	4.50E-20	3.92E-67	7.75E-176	9.22E-69	1.51E-184	1.42E-18	2.23E-01	3.32E-40	3.86E-02	1.17E-104	2.52E-262
	std	8.40E-60	6.90E-20	1.11E-66	0	3.81E-68	0	3.13E-18	1.48E-01	6.78E-40	1.97E-01	6.08E-104	0
	p-rank	-	-	-	-	-	-	-	-	-	-	-	-
	f-rank	7	9	6	3	5	2	10	13	8	12	4	1
G2	mean	1.80E-25	1.90E-14	4.31E-36	1.86E-115	8.25E-41	5.04E-93	2.98E-07	2.11E+01	7.12E-23	6.97E-01	5.80E-68	9.00E-132
	std	8.8E-25	1.05E-14	6.57E-36	1.32E-114	4.19E-40	3.47E-93	1.78E+00	9.57E+00	6.36E-23	3.34E+00	1.34E-67	3.42E-131
	p-rank	-	-	-	-	-	-	-	-	-	-	-	-
	f-rank	7	9	6	2	5	3	10	13	8	12	4	1
G3	mean	5.70E-61	9.00E-37	3.75E-37	2.87E+04	4.31E-13	1.23E-183	1.59E-05	8.87E+01	8.06E-09	1.80E+03	7.92E-20	1.34E-262
	std	2.70E-60	5.43E-36	1.36E-36	1.02E+04	2.83E-30	0	2.21E-05	4.72E+01	1.60E-08	2.88E+03	2.68E-19	0
	p-rank	-	-	-	-	-	-	-	-	-	-	-	-
	f-rank	3	5	4	13	7	2	9	10	8	12	6	1
G4	mean	8.20E-24	7.40E-11	2.39E-25	1.06E+01	2.15E-17	9.97E-93	2.01E-06	2.11E+00	5.39E-10	4.80E+01	6.79E-14	6.92E-133
	std	4.00E-23	1.82E-10	6.80E-25	2.22E+01	1.06E-16	7.31E-93	1.25E-06	4.92E-01	1.38E-09	1.09E+01	2.08E-13	2.09E-132
	p-rank	-	-	-	-	-	-	-	-	-	-	-	-
	f-rank	4	7	3	12	5	2	9	11	8	13	6	1
G5	mean	8.00E-02	2.10E+01	2.65E+01	2.85E+01	5.90E+00	2.89E+01	3.67E+01	2.88E+01	2.53E+01	2.11E+04	2.68E+01	0
	std	5.60E-01	7.80E+00	5.19E-01	2.22E-01	9.13E-01	1.72E-02	3.34E+01	8.24E-01	1.69E-01	1.06E+05	9.70E-01	0
	p-rank	-	-	-	-	-	-	-	-	-	-	-	-
	f-rank	2	4	7	9	3	11	12	5	6	13	8	1
G6	mean	2.90E+00	9.30E+02	2.65E+01	1.62E+00	4.14E-08	5.88E+00	6.83E-19	2.48E-01	8.29E-06	4.37E+01	1.34E+00	9.55E-26
	std	1.20E+00	1.80E+02	5.19E-01	6.93E-01	5.22E-08	5.86E-01	6.71E-19	1.13E-01	5.02E-06	2.38E+02	4.67E-01	3.55E-25
	p-rank	-	-	-	-	-	-	-	-	-	-	-	-
	f-rank	9	13	11	8	4	10	2	3	5	12	7	1
G7	mean	6.40E-04	4.80E-03	9.90E-04	1.37E-03	1.33E-03	1.13E-04	2.75E-02	4.70E-03	1.17E-03	3.68E-01	1.77E-03	1.83E-05
	std	2.50E-04	1.20E-03	8.37E-04	2.85E-03	1.72E-03	8.94E-04	7.90E-03	1.90E-03	6.54E-04	9.56E-01	1.33E-03	1.78E-05
	p-rank	-	-	-	-	-	-	-	-	-	-	-	-
	f-rank	3	10	4	7	6	2	12	9	5	13	8	1
G8	mean	1.00E-04	1.20E-03	0	0	5.46E+00	0	2.53E+01	6.75E+01	0	5.50E+01	0	0
	std	6.00E-05	6.50E-04	0	0	5.62E+00	0	8.55E+00	1.00E+01	0	3.26E+01	0	0
	p-rank	-	-	-	-	-	-	-	-	-	-	-	-
	f-rank	7	8	1	1	9	1	11	10	1	12	1	1
G9	mean	8.20E-10	2.70E-03	5.58E-15	3.02E-15	8.88E-16	8.88E-16	1.55E+01	3.93E-01	8.34E-14	1.67E+01	8.69E+00	8.88E-16
	std	6.90E-10	5.10E-04	1.67E-15	2.27E-15	9.36E-32	0	7.92E+00	1.51E-02	2.53E-14	6.08E+00	1.01E+01	0
	p-rank	-	-	-	-	-	-	-	-	-	-	-	-
	f-rank	7	8	5	4	3	1	12	9	6	13	8	1
G10	mean	9.90E-08	7.80E-04	0	1.42E-02	3.33E-02	0	5.76E-15	8.94E-01	0	4.83E-01	3.21E-03	0
	std	6.00E-07	1.20E-03	0	1.00E-01	4.56E-02	0	6.18E-15	1.07E-01	0	1.40E+00	8.51E-03	0
	p-rank	-	-	-	-	-	-	-	-	-	-	-	-
	f-rank	6	7	1	10	11	1	5	9	1	12	8	1
Continued													

Function		JADE	SaDE	GWO-E	OEWOA	SCCS	FA-FPO	CMA-ES	SHADE	LSHADE-SPACMA	EO	BDE	MGSCA	MaCN
G11	mean	4.60E-17	1.90E-05	1.98E-02	1.06E-01	1.34E-02	8.32E-01	2.87E-16	3.46E-02	8.18E-04	7.97E-07	8.87E+04	7.07E-02	3.06E-19
	std	1.90E-16	9.20E-06	1.01E-02	4.97E-02	1.60E-02	1.78E-01	5.64E-16	8.75E-02	1.00E-03	7.69E-07	1.88E+05	3.16E-02	6.55E-19
	p-rank	–	–	–	–	–	–	–	–	–	–	–	–	–
	f-rank	2	5	8	11	7	12	3	9	6	4	13	10	1
G12	mean	2.00E-16	6.10E-05	2.50E-01	1.03E+00	2.01E-02	2.94E+00	3.66E-04	7.32E-04	1.02E-02	2.92E-02	4.05E+05	1.42E+00	2.06E-23
	std	6.50E-16	2.00E-05	1.63E-01	3.61E-01	7.23E-02	1.59E-01	2.00E-03	2.80E-03	1.03E-02	3.52E-02	1.33E+06	2.57E-01	6.52E-23
	p-rank	–	–	–	–	–	–	–	–	–	–	–	–	–
	f-rank	2	3	9	10	7	13	4	5	6	8	13	11	1
w/l/t		0/12/0	0/12/0	0/10/2	0/11/1	0/12/0	0/9/3	0/12/0	0/12/0	0/12/0	0/10/2	0/12/0	0/11/1	NA
Average f-rank		4.92	7.33	5.41	7.50	6.00	5.00	8.25	8.67	10.00	5.67	12.50	7.00	1.00
Overall f-rank		2	8	4	9	6	3	10	11	12	5	13	7	1

Table 6. Simulated results for CEC 2005 test suite.



**Fig. 6.** Convergence profiles of CV 1.0, NMRA and MaCN for Dimension Size 30.

$$\text{Fto minimize } f(S) = g(S) \times g_{\text{penalty}}(S) \quad (20)$$

For  $W$  sections,  $S$  is the design vector of cross-sectional areas;  $f(S)$  represents the merit functions;  $dv$  is the number of design variables;  $g(S)$  is the objective function defined as the volume or weight of the frame structure; and  $g_{\text{penalty}}(S)$  is a penalty function resulting from constraint violations on the structural response<sup>142</sup>.

The weight of the frame structure, represented as a function  $g(S)$ , is given by

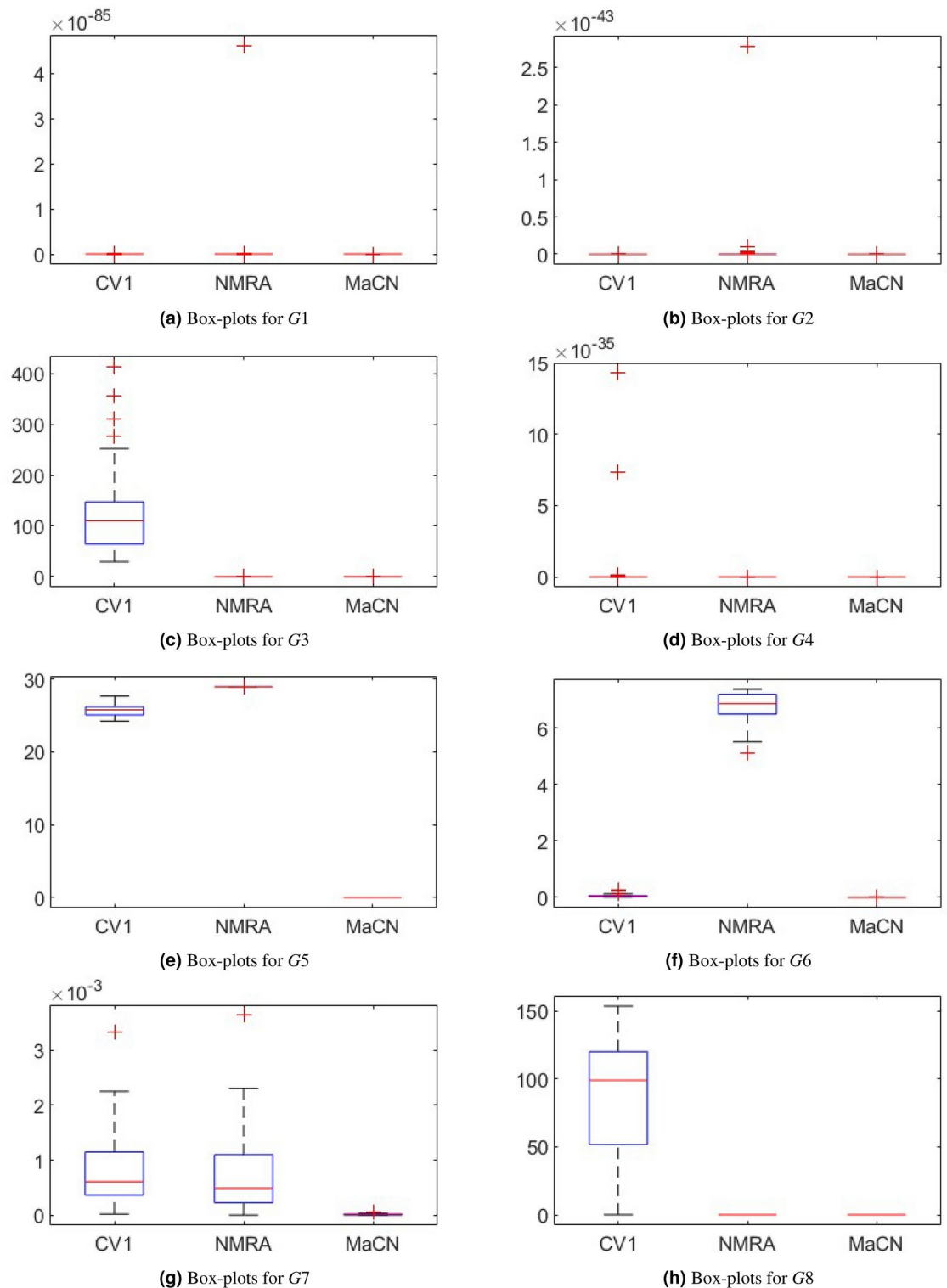
$$g(S) = \sum_{z=1}^{nm} \gamma_z \cdot S_z \cdot L_z \quad (21)$$

where  $nm$  denotes the total number of members comprising the frame;  $L_z$  represents the length of the  $z$ -th member in the frame; and  $\gamma_z$  is the density of the material in the  $z$ -th member.

The penalty function,  $g_{\text{penalty}}(S)$ , is defined as follows<sup>143</sup>:

$$g_{\text{penalty}}(S) = (1 + \epsilon_1 \cdot v)^{\epsilon_2}, \quad v = \sum_{z=1}^n \max[0, y_z] \quad (22)$$





**Fig. 7.** Box-plots of CV1, NMRA and MaCN for CEC 2005 test suite.

where  $n$  represents the number of constraints in the design problem,  $\epsilon_1$  and  $\epsilon_2$  are constants derived from  $expl$  and  $expt$ , and  $y_z$  denotes the displacement or stress constraint. If  $y_z$  is positive, its value is added to the constraint functions. These constraints comprise of

Element stresses

$$y_z^\sigma = 1 - \left| \frac{\sigma_z}{\sigma_z^a} \right| \leq 0, \quad z = 1, 2, \dots, nm \quad (23)$$

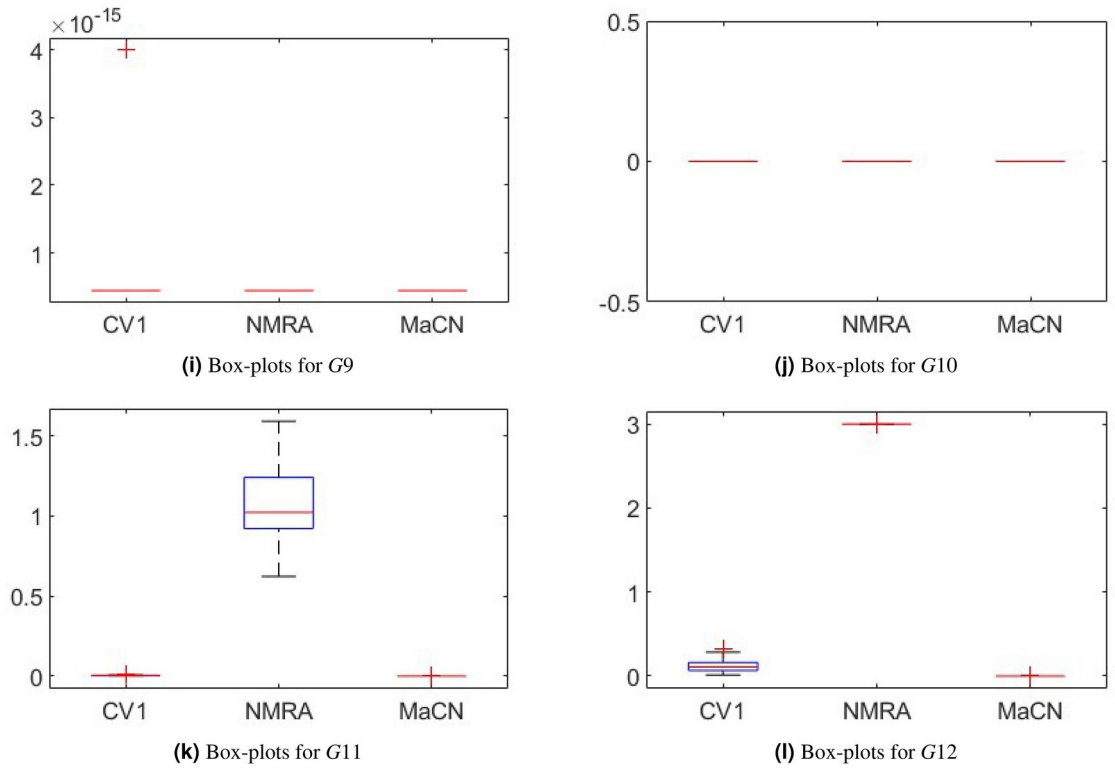


Fig. 7. (continued)

Maximum latent displacement

$$v^{\Delta} = R - \frac{\Delta T}{H} \leq 0 \quad (24)$$

Inter-story displacements

$$v_j^d = R_I - \frac{d_j}{h_j} \leq 0, \quad j = 1, 2, \dots, ns \quad (25)$$

where  $\sigma_z$  represents the stress in the  $z^{th}$  member, and  $\sigma_z^a$  is the allowable stress in the same member.  $\Delta T$  denotes the maximum latent displacement. The total number of stories is denoted by  $ns$ . The maximum drift index is represented by  $R$ , and  $d_j$  signifies the inter-story drift at the  $j^{th}$  floor. The height of the frame structure is  $H$ , and  $h_j$  is the height of the  $j^{th}$  story. The inter-story drift index permitted by AISC 2001, indicated by  $R_I$ , is set to  $1/300$  as per<sup>143</sup>. The constraints per the LRFD interaction formulas from AISC 2001 are given by:

$$y_z^Z = \begin{cases} 1 - \frac{P_u}{2\phi_c P_n} - \left( \frac{M_{ux}}{\phi_b M_{nx}} + \frac{M_{uy}}{\phi_b M_{ny}} \right) \leq 0; \text{ For } \frac{P_u}{\phi_c P_n} < 0.2 \\ 1 - \frac{P_u}{\phi_c P_n} - \frac{8}{9} \left( \frac{M_{ux}}{\phi_b M_{nx}} + \frac{M_{uy}}{\phi_b M_{ny}} \right) \leq 0; \text{ For } \frac{P_u}{\phi_c P_n} \geq 0.2 \end{cases} \quad (26)$$

where  $P_u$  represents the required axial strength, while  $P_n$  denotes the nominal axial strength in either tension or compression. The resistance factors are  $\phi_t = 0.9$  for tension and  $\phi_c = 0.85$  for compression. The flexural resistance reduction factor is  $\phi_b = 0.90$ . The terms  $M_{ux}$  and  $M_{uy}$  indicate the required flexural strengths in the  $x$  and  $y$  directions, respectively, while  $M_{nx}$  and  $M_{ny}$  represent the nominal flexural strengths in these directions. For a two-dimensional structure, the value of  $M_{ny}$  is set to 0.

The effective length factor  $K$  is essential for determining Euler and compression stresses. For bracing and beam members,  $K$  is set to 1. For column members,  $K$  is calculated using SAP2000. In a generalized case, the approximate effective length, accurate within  $-1.0\%$  to  $+2.0\%$ , is based on Dumonteil<sup>144</sup> and is given by:

$$K = \begin{cases} \sqrt{\frac{1.6G_A G_B + 4(G_A + G_B) + 7.5}{G_A + G_B + 7.5}}; & \text{For unbraced members} \\ \frac{3G_A G_B + 1.4(G_A + G_B) + 0.64}{3G_A G_B + 2(G_A + G_B) + 1.28}; & \text{For braced members} \end{cases} \quad (27)$$

Functions		LX-BBO <sup>50</sup>	B-BBO <sup>50</sup>	RW-GWO <sup>48</sup>	ISOS <sup>47</sup>	PBIL <sup>52</sup>	VNBA <sup>52</sup>	IMEHO <sup>52</sup>	CCS <sup>52</sup>	BDE <sup>33</sup>	MGSCA <sup>33</sup>	MaCN
$F_1$	mean	1.01E+07	6.51E+06	8.02E+06	<b>9.82E+05</b>	3.42E+08	2.43E+08	2.37E+06	1.46E+08	1.25E+07	2.92E+07	1.18E+06
	std	1.01E+07	1.31E+06	3.32E+06	7.05E+05	1.09E+08	5.93E+07	4.32E+06	3.27E+07	7.47E+03	2.07E+07	<b>5.51E+05</b>
	f-rank	6	4	5	1	11	10	3	9	7	8	2
$F_2$	mean	5.34E+04	2.35E+04	2.23E+05	<b>5.27E+00</b>	4.08E+10	1.92E+10	5.49E+03	2.60E+09	9.25E+03	2.26E+09	1.00E+10
	std	2.14E+04	9.99E+03	5.51E+05	1.72E+01	3.39E+09	4.23E+09	4.87E+03	5.22E+08	6.19E+04	1.69E+09	<b>0</b>
	f-rank	5	4	6	1	11	10	2	7	3	8	9
$F_3$	mean	1.63E+04	6.03E+03	3.16E+02	4.79E+02	9.18E+04	2.93E+04	1.40E+02	2.70E+03	5.27E+02	1.77E+04	<b>1.25E+01</b>
	std	1.70E+04	3.15E+03	4.34E+02	6.24E+02	1.75E+04	1.39E+04	1.58E+02	7.74E+04	1.11E+03	6.63E+03	<b>3.43E+00</b>
	f-rank	8	7	3	4	11	10	2	6	5	9	1
$F_4$	mean	9.99E+01	1.02E+02	<b>3.41E+01</b>	5.98E+01	3.42E+03	1.60E+03	1.24E+02	3.22E+02	5.76E+02	2.76E+02	5.85E+01
	std	2.84E+01	3.13E+01	<b>1.81E+01</b>	3.56E+01	7.56E+02	3.63E+02	4.77E+01	4.09E+01	4.29E+01	6.56E+01	2.63E+01
	f-rank	4	5	1	3	11	10	6	8	9	7	2
$F_5$	mean	<b>3.06E+00</b>	3.74E+00	2.05E+01	2.03E+01	2.10E+01	2.10E+01	2.10E+01	2.10E+01	2.01E+01	2.03E+01	2.02E+01
	std	7.85E-01	4.91E-01	7.46E-02	6.67E-02	5.56E-02	<b>5.43E-02</b>	5.99E-02	8.81E-02	1.33E-01	1.44E-01	2.58E-01
	f-rank	1	2	7	4	9	8	10	11	3	6	5
$F_6$	mean	1.70E+01	1.99E+01	9.83E+00	1.05E+01	3.81E+01	3.30E+01	1.21E+01	2.51E+01	2.38E+01	1.94E+01	<b>9.65E+00</b>
	std	3.12E+00	2.70E+00	3.49E+00	2.39E+00	<b>1.16E+00</b>	2.58E+00	2.72E+00	2.01E+00	4.39E+00	2.88E+00	1.88E+00
	f-rank	5	7	2	3	11	10	4	9	8	6	1
$F_7$	mean	1.75E-01	7.81E-02	2.51E-01	1.54E-02	3.41E+02	1.10E+02	<b>0</b>	2.31E+01	1.51E+00	1.99E+01	5.90E-03
	std	8.56E-02	4.43E-02	1.42E-01	1.83E-02	2.74E+01	1.81E+01	1.19E-01	3.52E+00	6.07E+00	1.18E+01	<b>6.30E-03</b>
	f-rank	5	4	6	3	11	10	1	9	7	8	2
$F_8$	mean	5.53E+01	<b>4.71E-01</b>	4.38E+01	1.47E+01	3.01E+02	1.74E+02	3.30E+01	2.90E+02	6.12E+01	1.07E+02	3.30E+01
	std	3.78E+02	<b>6.78E-01</b>	8.47E+00	3.34E+00	1.03E+01	1.61E+01	9.19E+00	2.23E+01	2.60E+01	2.14E+01	1.18E+01
	f-rank	6	1	5	2	11	9	3	10	7	8	4
$F_9$	mean	7.66E+01	9.10E+01	6.33E+01	2.54E+02	3.69E+02	2.50E+02	<b>3.20E+01</b>	2.90E+02	1.10E+02	1.39E+02	1.39E+02
	std	1.60E+01	1.54E+01	1.30E+01	1.33E+01	1.69E+01	2.04E+01	<b>1.15E+01</b>	2.38E+01	4.69E+01	2.60E+01	1.52E+01
	f-rank	3	4	2	9	11	8	1	10	5	7	6
$F_{10}$	mean	1.25E+04	6.68E+03	9.61E+02	1.78E+03	6.26E+03	3.50E+03	2.26E+03	8.55E+03	1.75E+03	2.82E+03	<b>6.65E+02</b>
	std	1.16E+02	4.58E+02	2.72E+02	<b>4.09E+01</b>	3.05E+02	3.47E+02	5.72E+02	4.91E+02	7.28E+02	6.83E+02	3.04E+02
	f-rank	11	9	2	4	8	7	5	10	3	6	1
$F_{11}$	mean	1.23E+04	6.71E+03	2.68E+03	1.48E+03	7.10E+03	6.80E+03	2.86E+03	8.83E+03	3.90E+03	3.30E+03	<b>2.60E+00</b>
	std	3.41E+02	5.17E+02	3.68E+02	4.54E+02	<b>2.97E+02</b>	3.79E+02	5.38E+02	5.50E+02	7.38E+02	6.26E+02	4.46E+02
	f-rank	11	7	3	2	9	8	4	10	6	5	1
$F_{12}$	mean	<b>1.10E-02</b>	<b>1.10E-02</b>	5.44E-01	3.55E-01	1.01E+01	1.01E+01	1.01E+01	1.01E+01	3.77E-01	6.33E-01	3.24E-01
	std	<b>1.74E-18</b>	<b>1.74E-18</b>	1.65E-01	5.72E-02	3.38E-01	3.51E-01	5.26E-01	1.09E+00	1.71E-01	3.36E-01	1.57E-01
	f-rank	1	1	6	4	8	9	10	11	5	7	3
$F_{13}$	mean	6.55E-01	6.78E-01	2.80E-01	3.77E-01	0	0	<b>0</b>	0	5.13E-01	5.51E-01	2.63E-01
	std	1.56E-01	7.98E-02	6.30E-02	7.10E-02	2.55E-01	3.63E-01	6.24E-02	1.75E-01	1.41E-01	8.94E-02	<b>5.61E-02</b>
	f-rank	10	11	6	7	3	4	1	2	8	9	5
$F_{14}$	mean	6.20E-01	3.93E-01	4.23E-01	2.71E-01	1.00E+02	6.00E+01	<b>0</b>	1.00E+01	4.41E-01	2.34E+00	1.83E-01
	std	2.96E-01	1.55E-01	2.15E-01	5.12E-02	1.15E+01	1.22E+01	9.85E-02	1.88E+00	2.46E-01	3.31E+00	<b>2.11E-02</b>
	f-rank	7	4	5	3	11	10	1	9	6	8	2
$F_{15}$	mean	1.55E+01	1.88E+01	8.81E+00	1.06E+01	6.84E+05	2.39E+03	<b>0</b>	8.00E+01	3.78E+01	8.72E+01	5.97E+00
	std	5.49E+00	5.64E+00	1.51E+00	3.71E+00	2.85E+05	1.22E+03	<b>1.34E+00</b>	3.02E+01	9.26E+01	1.01E+02	1.94E+00
	f-rank	5	6	3	4	11	10	1	8	7	9	2
$F_{16}$	mean	1.07E+01	1.06E+01	1.04E+01	9.21E+01	2.02E+01	2.02E+01	2.02E+01	2.00E+01	1.25E+01	1.16E+01	<b>1.04E+01</b>
	std	5.83E-01	6.25E-01	6.10E-01	7.30E-01	2.12E-01	3.66E-01	7.64E-01	<b>1.74E-01</b>	5.91E-01	6.91E-01	5.14E-01
	f-rank	4	3	2	11	8	9	10	7	6	5	1
$F_{17}$	mean	1.49E+06	1.27E+06	5.71E+05	1.75E+05	9.74E+06	2.53E+06	7.69E+04	1.15E+07	2.80E+04	9.56E+05	<b>5.63E+00</b>
	std	9.34E+05	5.46E+05	4.10E+05	1.62E+05	2.79E+06	3.34E+06	8.38E+04	4.59E+06	2.24E+04	7.62E+05	<b>3.15E+00</b>
	f-rank	8	7	5	4	10	9	3	11	2	6	1
$F_{18}$	mean	2.89E+03	8.22E+02	6.51E+03	3.89E+03	6.16E+08	1.66E+08	3.30E+03	1.10E+08	3.54E+04	1.47E+05	<b>5.23E+02</b>
	std	4.27E+03	1.01E+03	4.62E+02	5.15E+03	1.68E+08	1.03E+08	3.52E+03	4.66E+07	1.62E+05	9.00E+05	<b>2.11E+02</b>
	f-rank	3	2	6	5	11	10	4	9	7	8	1
Continued												

Functions		LX-BBO <sup>50</sup>	B-BBO <sup>50</sup>	RW-GWO <sup>48</sup>	ISOS <sup>47</sup>	PBIL <sup>52</sup>	VNBA <sup>52</sup>	IMEHO <sup>52</sup>	CCS <sup>52</sup>	BDE <sup>33</sup>	MGSCA <sup>33</sup>	MaCN
$F_{19}$	mean	5.17E+03	7.80E+03	1.14E+01	7.79E+01	1.90E+02	1.20E+02	1.05E+01	4.00E+01	1.11E+01	2.27E+01	<b>6.26E+00</b>
	std	5.67E+03	4.65E+03	2.03E+00	1.78E+00	3.42E+01	3.82E+01	1.74E+00	5.90E+00	1.08E+01	1.43E+01	<b>6.38E-01</b>
	f-rank	10	11	4	7	9	8	2	6	3	5	1
$F_{20}$	mean	2.61E+04	1.62E+04	6.27E+02	4.98E+03	3.58E+04	1.68E+04	2.10E+02	1.03E+06	3.02E+03	4.23E+03	<b>1.49E+02</b>
	std	1.57E+04	4.11E+03	1.12E+03	3.40E+03	1.76E+04	6.57E+03	8.17E+01	9.05E+05	7.25E+03	3.81E+03	<b>3.04E+01</b>
	f-rank	9	7	3	6	10	8	2	11	4	5	1
$F_{21}$	mean	1.11E+06	1.22E+06	2.57E+05	8.91E+04	2.52E+06	2.30E+06	2.70E+04	5.66E+06	5.08E+04	2.33E+05	<b>1.05E+00</b>
	std	7.95E+05	7.96E+05	1.76E+05	1.06E+05	1.17E+06	1.35E+06	1.83E+04	2.73E+06	1.22E+05	2.38E+05	<b>5.92E+00</b>
	f-rank	7	8	6	4	10	9	2	11	3	5	1
$F_{22}$	mean	1.88E+03	1.66E+02	2.07E+02	2.75E+02	1.02E+03	8.40E+02	2.10E+02	1.34E+03	6.81E+02	3.39E+02	<b>7.20E+01</b>
	std	2.03E+02	2.45E+02	2.09E+02	1.45E+02	1.88E+02	1.28E+02	1.01E+02	1.88E+02	2.11E+02	1.78E+02	<b>4.91E+01</b>
	f-rank	3	2	4	6	10	9	5	11	8	7	1
$F_{23}$	mean	4.11E+02	3.42E+02	3.14E+02	3.14E+02	6.00E+02	3.90E+02	3.20E+02	3.50E+02	3.14E+02	3.28E+02	<b>2.00E+02</b>
	std	6.43E+01	2.84E+01	2.76E-01	1.60E+01	6.70E+01	2.47E+01	4.78E-01	7.66E+00	1.20E-01	4.02E+00	<b>0</b>
	f-rank	10	7	3	4	11	9	5	8	2	6	1
$F_{24}$	mean	1.47E+04	3.41E+04	2.02E+02	2.01E+02	4.01E+02	2.30E+02	2.40E+02	2.20E+02	2.46E+02	2.01E+02	2.00E+02
	std	8.37E+03	2.35E+04	3.03E-03	<b>1.50E-03</b>	1.42E+01	2.53E+01	6.46E+00	2.51E+00	5.69E+00	1.55E-03	1.60E-03
	f-rank	10	11	4	1	9	6	7	5	8	2	3
$F_{25}$	mean	5.29E+02	6.53E+02	2.03E+02	2.00E+02	2.40E+02	2.10E+02	2.11E+02	2.20E+02	2.08E+02	2.11E+02	2.00E+02
	std	4.36E+01	6.01E+01	1.17E+00	8.07E-01	6.00E+00	1.06E+01	2.08E+00	4.44E+00	4.51E+00	2.82E+00	<b>0</b>
	f-rank	10	11	3	2	9	5	6	8	4	7	1
$F_{26}$	mean	2.12E+00	3.64E+01	1.01E+02	1.01E+02	1.01E+02	1.01E+02	1.00E+02	1.01E+02	1.02E+02	1.02E+02	1.27E+02
	std	3.46E+00	5.62E+01	7.36E-02	9.55E-02	2.09E-01	4.30E-01	<b>6.00E-02</b>	2.06E-01	1.17E+00	1.53E-01	4.48E+01
	f-rank	10	11	2	3	5	6	1	4	8	7	9
$F_{27}$	mean	<b>1.95E+02</b>	3.02E+02	4.08E+02	5.43E+02	1.08E+03	1.29E+03	5.80E+02	5.30E+02	8.82E+02	8.19E+02	2.00E+02
	std	1.04E+02	1.60E+02	6.07E+00	1.35E+02	2.80E+02	3.30E+01	1.41E+02	7.92E+01	2.03E+02	9.17E+01	<b>0</b>
	f-rank	2	3	4	6	10	11	7	5	9	8	1
$F_{28}$	mean	1.94E+03	2.12E+03	4.34E+02	9.68E+02	1.39E+03	1.67E+03	9.71E+02	1.44E+03	1.29E+03	9.68E+02	<b>2.00E+02</b>
	std	1.04E+02	4.44E+02	8.45E+00	4.12E+01	1.33E+02	2.32E+02	2.43E+02	9.46E+02	2.88E+02	1.06E+02	<b>0</b>
	f-rank	10	11	2	3	7	9	5	8	6	4	1
$F_{29}$	mean	1.98E+07	3.09E+07	2.14E+02	5.70E+05	5.70E+06	7.47E+06	1.21E+03	1.20E+06	4.81E+06	1.19E+06	<b>2.00E+02</b>
	std	3.95E+06	6.91E+06	2.37E+00	2.14E+06	3.33E+06	1.20E+06	2.16E+02	7.03E+05	4.82E+06	3.25E+06	<b>0</b>
	f-rank	10	11	2	4	8	9	3	6	7	5	1
$F_{30}$	mean	6.95E+06	1.38E+07	6.69E+02	2.38E+05	1.49E+05	1.89E+05	4.08E+03	7.66E+04	1.74E+04	1.93E+04	<b>2.00E+02</b>
	std	1.03E+07	1.08E+07	2.14E+02	1.10E+03	5.55E+04	1.03E+05	1.44E+03	3.36E+04	3.17E+04	8.25E+03	<b>4.85E+00</b>
	f-rank	10	11	2	9	7	8	3	6	4	5	1
Average f-rank		6.80	6.40	3.80	4.30	9.37	8.60	3.97	8.17	5.67	6.50	2.37
Overall f-rank		8	6	2	4	11	10	3	9	5	7	1

**Table 7.** Results of MaCN algorithm for CEC 2014 test functions.

where  $G_A$  and  $G_B$  are the stiffness ratios of the columns to girders at the two end joints A and B of the column section, respectively.

In this subsection, MaCN's performance has been evaluated for the complex real problem of steel frame structure<sup>143145</sup>. The weight minimization in this problem is the main objective of the optimization algorithm. The optimized results of MaCN are compared with other algorithms for three frame structures such as 1 – bay 8 – story, 3 – bay 15 – story and 3 – bay 24 – story. To obtain statistical results for these frame design problems, the algorithm is simulated for 20 independent runs. Although these frame structure problems are rarely used, due to various challenges that have been observed in describing the problem's clear objective function according to design codes. Here, the main aim of doing comparison among the optimization algorithms is to check the algorithm's robustness in terms of accuracy, and stopping criteria are maximum iterations. The description of three steel frame problems and the analysis of the results are given in consecutive subsections.

#### 1-bay 8-story

The fabrication of 1 – bay 8 – story frame structure follows the condition of using a single beam during two successive stories, starting from the bottom of the frame. After that, two successive stories have been categorized into a single section of the column. Figure 8 describes the structure of this problem along with various loads that have been implemented on this structure. This frame design problem is considered a constrained optimization problem with one constraint variable, such as lateral drift at the peak point. The value of this lateral drift has to

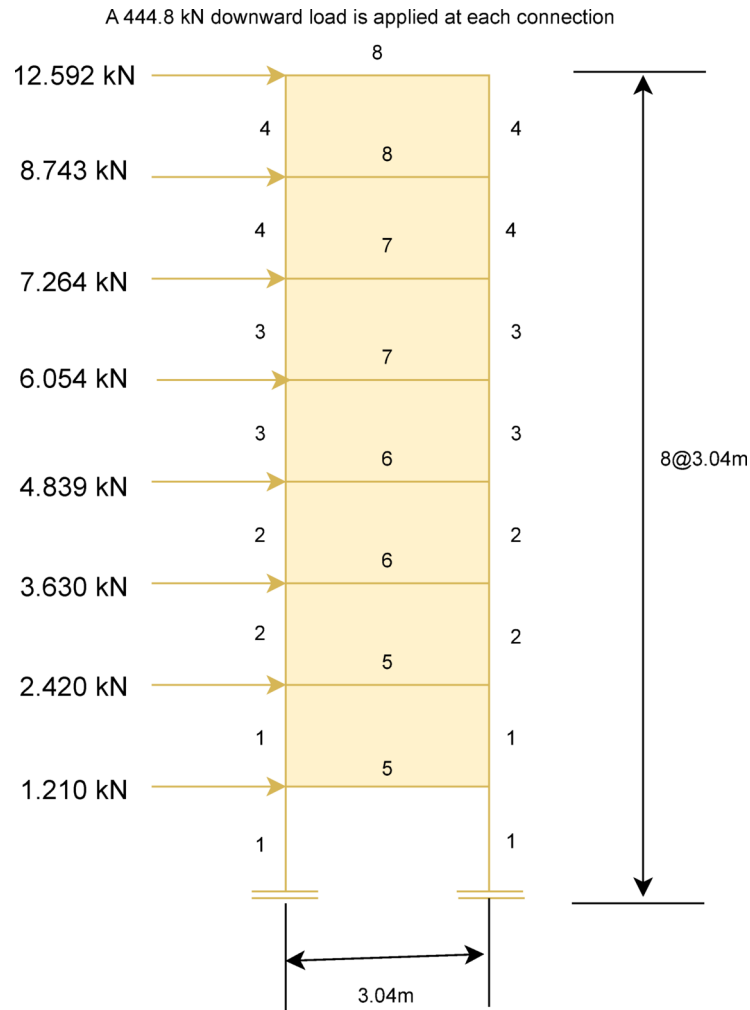


Fig. 8. Structure of 1-bay 8-story frame with loading (adapted from<sup>143</sup>).

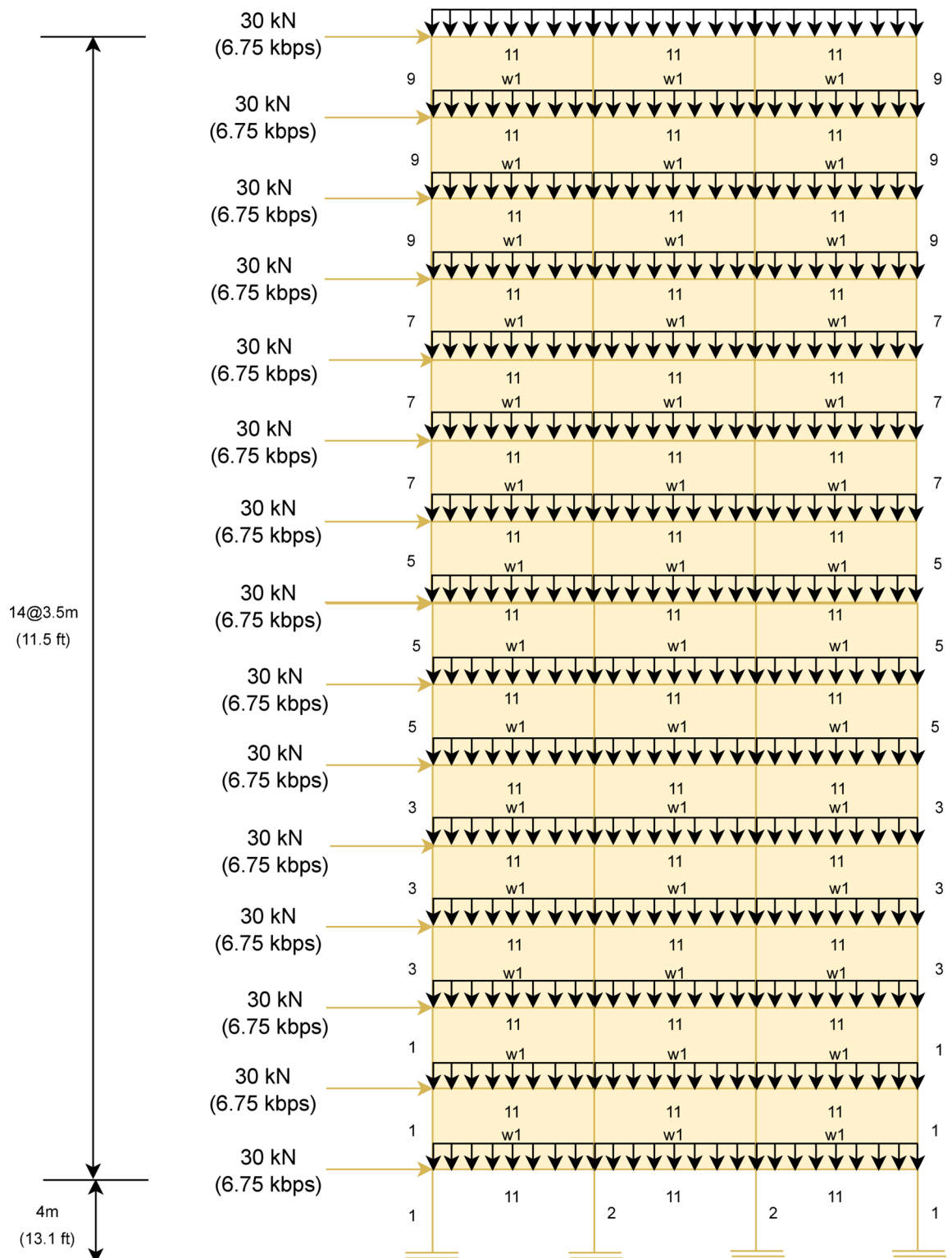
Groups	Optimal W-shaped sections								
	SFLAIWO	DE	PSOACO	PSOPC	ES-DE	ACO	GA	HGAPSO	MaCN
	150	143	148	148	143	147	146	149	
1	W18X40	W16X36	W18X35	W18X35	W18X40	W21X44	W18X35	W18X35	W21X44
2	W18X35	W16X36	W16X32	W14X26	W18X35	W18X35	W18X35	W18X35	W16X31
3	W14X22	W14X22	W14X22	W16X26	W14X22	W18X35	W18X35	W14X22	W14X22
4	W12X14	W12X22	W12X16	W14X16	W12X14	W12X22	W18X26	W12X16	W12X14
5	W18X35	W18X35	W21X48	W24X62	W18X46	W18X40	W18X46	W16X31	W14X22
6	W18X35	W16X31	W18X40	W18X35	W18X35	W16X26	W16X31	W21X44	W18X40
7	W18X35	W18X40	W16X31	W16X31	W18X35	W16X26	W16X26	W18X35	W18X40
8	W14X22	W14X30	W16X36	W12X30	W12X19	W12X14	W12X16	W16X26	W14X26
Weight (kN)	31.08	32.76	32.29	34.21	31.77	31.05	32.83	31.24	30.70

Table 8. Optimization results for the 1-bay 8-story frame.

be lower than 5.08 cm, and the elastic modulus ( $E$ ) of the structure is set to 200 GPa. Further, all the structural elements are combined into various categories for the generation of 4 sections of columns and 4 sections of the beam. The cross section area for all these elements must be selected from 267  $W$  – shaped sections.

*Inferences from results:* Table 8 provides the optimized results of MaCN for 1 – bay 8 – story frame structure problem and comparison has been performed with respect to other algorithms namely DE<sup>143</sup>, ES-DE<sup>143</sup>, genetic algorithm (GA)<sup>146</sup>, ant colony optimization (ACO)<sup>147</sup>, PSOPC<sup>148</sup>, PSOACO<sup>148</sup>, hybrid GA with particle swarm optimization (HGAPSO)<sup>149</sup> and SFLAIWO<sup>150</sup>. From the results, it has been analyzed that proposed MaCN is





### 3-bay 15-story

The structure of 3 – bay 15 – story steel frame is schematically shown in Figure 9. This figure also describes the various groups of elements and incorporates various loads to the frame structure. This frame design problem mainly comes with two constraints of optimization, the first constraint is related to displacement and the second constraint deals with the strength of the material provided by the American Institute of Steel Construction (AISC). In the present work, the value of frame top story's sway should be kept lower than 23.5 cm, the value of material modulus of elasticity ( $E$ ) is equal to 200 GPa and the value of yield stress ( $S_y$ ) is kept constant at 248.2 MPa which are same as<sup>143</sup>. After that, the effective length of frame members for the sway-permitted frame is determined as  $L_x \geq 0$  and for out of a plane is defined as  $L_y = 1$ . Here, it should be taken care that all groups of elements are decided from 267  $W$  sections, and every column of the frame is taken as non-braced with its length. This non-braced length of every beam is calculated as  $1/5^{th}$  length of the span.

**Inferences from results:** The optimized results obtained by various algorithms for 3 – bay 15 – story steel frame problem is presented in Table 9. Here twelve improved algorithms are used for comparison with respect to the proposed MaCN algorithm. These algorithms are hybrid harmony search, particle swarm and ant colony optimization (HPSACO)<sup>151</sup>, hybridization of big bang-big crunch algorithm (HBB-BC)<sup>152</sup>, imperialist competitive algorithm (ICA)<sup>153</sup>, DE<sup>143</sup>, ES-DE<sup>143</sup>, accelerated version of water evaporation optimization (AWEO)<sup>141</sup>, enhanced vibrating particle system algorithm (EVPS)<sup>141</sup>, simplified dolphin echolocation (SDE)<sup>141</sup>, SFLAIWO<sup>150</sup>, morlet wavelet mutation based colliding bodies optimization (MWQI-CBO)<sup>154</sup>, set-theoretical multi-phase shuffle shepherd optimization algorithm (STMP-SSOA)<sup>155</sup> and tribe-interior search algorithm (Tribe-ISA)<sup>156</sup>. From the results presented in Table 9, MaCN is found to be best algorithm for structure design of steel frame with optimal weight of 361.14kN. The optimal weight generated by MaCN is lighter than 5% from the weight (379.21kN) generated by second most promising algorithm SFLAIWO. Hence, MaCN is again capable to provide superior performance for this problem because heavier optimal weights are given by all other algorithms under test.

### 3-bay 24-story

The design of 3 – bay 24 – story steel frame was firstly described by<sup>157</sup> and comprised a total of 168 members. These members are made up by using a total number of 96 columns and 72 beams. Figure 10 shows the schematic of this steel frame along with topology and various types of loads utilized on this frame structure. Here, it should be noted that the steel frame design must follow all the specifications provided by LRFD of AISC. This frame design has a displacement constraint treated as an optimization constraint under an inter-story drift with an index less than 1/300. The value of elastic modulus ( $E$ ) and yield of stress ( $S_y$ ) is set to 205 GPa and 230.3 MPa, respectively.

Further, the effective length of frame members is calculated with factor  $L_x \geq 0$  in the sway-permitted frame and  $L_y = 1$  for out of the plane. In order to fabricate the frame, some conditions have to be followed in which 1<sup>st</sup> and 3<sup>rd</sup> bay on all floors other than the roof's beam must be handled by a single section of the beam and create 4, beam groups. Apart from that, one group is associated with outer columns, and another group is associated with inner columns of the frame over 3 following stories. So, it can be said that this problem has 16 column groups and 4 beam groups for the total number of 20 design variables.

**Inferences from results:** For 3 – bay 24 – story frame design problem, optimized results of MaCN along with other algorithms namely ACO<sup>158</sup>, DE<sup>143</sup>, HBB-BC<sup>152</sup>, harmony search (HS)<sup>144</sup>, improved ACO (IACO)<sup>147</sup>, ICA<sup>153</sup>, hybrid bang-bing crunch PSO (HBBPSO)<sup>159</sup>, ES-DE<sup>143</sup>, AWEO<sup>141</sup>, EVPS<sup>141</sup>, SFLAIWO<sup>150</sup>, improved electro-search (IES) algorithm<sup>160</sup> and Tribe-ISA<sup>156</sup> are provided in Table 10. Here, EVPS provided the best optimal weight of 905.67kN which is marginal 0.3% lighter than proposed MaCN optimal weight 908.41kN. In the present scenario, it has been found that structural weights reported in literature by other algorithms are heavier than MaCN except EVPS. So, overall EVPS and MaCN are found to be capable for providing a solution near to global optimal solution.

## Discussion of results

This section provides an extensive summary of the results, along with some advantages of the proposed MaCN algorithm over others. It also discusses the specific drawbacks and some future insights on how we can mitigate them in the future.

## Summary of results

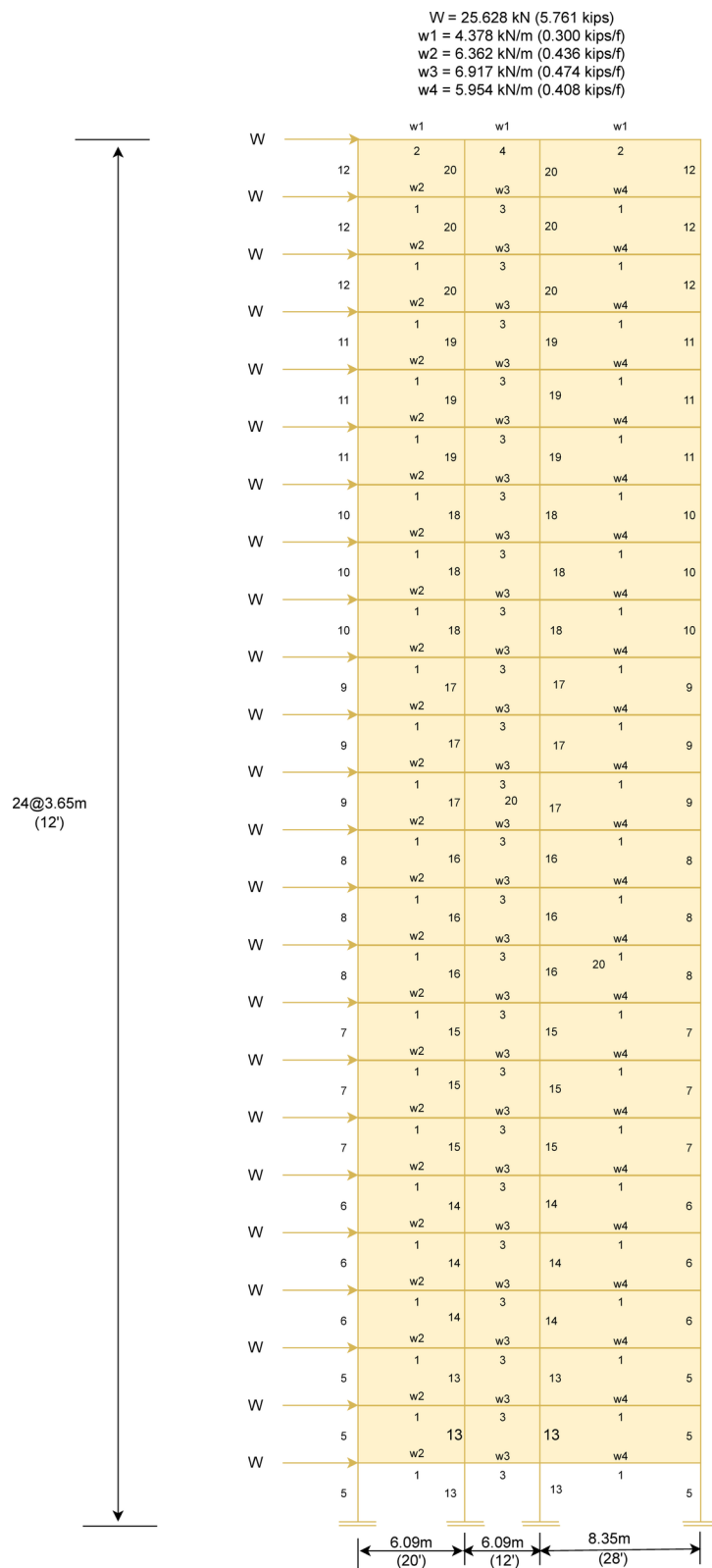
In summary, the proposed MaCN resulted in a set of excellent and stimulating results in this field to solve complex mathematical and engineering design problems. These results reinforce the goal of developing a new way to find solutions that are better than the available solutions through an advanced method of searching for optimal solutions.

In addition, the strategies used can offer a more satisfying equilibrium between the search strategies (*expl* and *expt*), especially in the last phase. Such techniques help the cases in which the search space is constrained, and unnecessary *expl* can reduce the convergence speed-up of an algorithm without changing the quality of solutions. Moreover, the proposed MaCN got all the core advantages of CS, NMRA, bare-bones search operators, and parametric adaptations together.

This is further complemented by the use of numerical benchmarks and engineering frame design problems. From the experimental results, it has been found that for CEC 2005, MaCN has superior performance over JADE, SaDE, CMA-ES, SHADE, LSHADE-SPACMA, MGSCA, FA-FPO, GWO-E and OEWAO. All of these comparative algorithms are hybrid versions of well-known algorithms and have been proposed recently. In CEC 2014 problems, performs better compared to LX-BBO, ISOS, VNBA, MGSCA, RW-GWO, B-BBO, IMEHO, CCS, BDE and other; again proving the superiority of the proposed algorithm. In addition to these comparisons,

Optimal W-shaped sections													
	HPSACO	ICA	HBB-BC	DE	AWEQ	ES-DE	EVPS	SDE	SFLAIWO	MWQI-CBO	STMP-SSOA	Tribe-ISA	
Groups	151	153	152	143	141	143	141	141	150	154	155	156	MaCN
1	W21X111	W24X117	W24X117	W21X122	W18X143	W18X106	W14X99	W14X90	W14X90	W14X90	W16X89	W14X109	W21X55
2	W18X158	W21X147	W21X132	W33X141	W24X162	W36X150	W27X161	W36X170	W26X146	W36X170	W36X170	W24X146	W30X90
3	W10X88	W27X84	W12X95	W14X82	W24X84	W12X79	W24X84	W27X84	W18X76	W27X84	W12X79	W18X86	W21X57
4	W30X116	W27X114	W18X119	W30X108	W33X118	W27X114	W24X104	W24X104	W24X104	W24X104	W27X114	W18X97	W8X67
5	W21X83	W14X74	W21X93	W30X108	W12X65	W30X90	W14X61	W14X61	W12X72	W14X61	W24X68	W14X74	W12X45
6	W24X103	W18X86	W18X97	W12X79	W18X97	W10X88	W30X90	W30X90	W18X86	W30X90	W18X86	W18X86	W14X61
7	W21X55	W12X96	W18X76	W14X61	W12X50	W18X71	W14X48	W14X48	W12X58	W14X48	W14X48	W24X68	W16X36
8	W27X114	W24X68	W18X65	W18X71	W21X68	W18X65	W12X65	W12X65	W14X61	W14X61	W14X61	W21X55	W14X34
9	W10X33	W10X39	W18X60	W6X25	W8X28	W8X28	W6X25	W6X25	W6X25	W14X34	W12X30	W8X24	W5X19
10	W18X46	W12X40	W10X39	W24X62	W16X40	W12X40	W12X40	W12X40	W16X36	W8X35	W10X39	W10X33	W8X28
11	W21X44	W21X44	W21X48	W21X48	W21X44	W21X48	W21X44	21X44	W21X44	W21X44	W21X44	W21X48	W18X28
Weight(kN)	426.36	417.47	434.54	423.83	429.46	415.06	389.77	387.89	379.21	386.63	389.08	399.27	361.14

Table 9. Optimization results for the 3-bay 15-story frame.



**Fig. 10.** Structure of 3-bay 24-story frame with loading (adapted from<sup>143</sup>).

the statistical results for 1 – bay 8 – story, 3 – bay 15 – story, and 3 – bay 24 – story show that MaCN is better than SFLAIWO, PSOACO, PSOPC, ES-DE, HGAPSO, EVPS, MWQL-CBO, STMP-SSOA, Tribe-ISA, HBB-BC, AWEO, ICA and others. It is included in better solutions and more accelerated convergence. These

Optimal W-shaped sections														
Groups	ACO	DE	Tribe-ISA	HS	IES	HBB-BC	ICA	IACO	HBBPSO	ES-DE	AWEO	EVPS	SFLAIWO	
	158	143	160	144	150	152	153	147	159	143	141	141	156	MaCN
1	W30X90	W30X90	W27X84	W30X90	W30X90	W30X90	W30X99	W30X90	W30X90	W30X90	W30X90	W30X90	W30X90	W30X90
2	W8X18	W21X48	W21X50	W10X22	W6X15	W21X18	W21X50	W16X26	W21X55	W21X55	W8X18	W6X15	W21X48	W18X60
3	W24X55	W21X44	W24X68	W18X40	W24X55	W18X46	W24X55	W18X35	W21X48	W21X48	W24X55	W24X55	W21X48	W24X55
4	W8X21	W27X129	W8X21	W12X16	W6X9	W8X21	W8X28	W14X22	W27X24	W10X45	W26X8.5	W6X8.5	W21X48	W16X36
5	W14X145	W14X176	W14X109	W14X176	W14X159	W14X176	W14X109	W14X145	W14X176	W14X145	W14X193	W14X159	W12X19	W14X159
6	W14X132	W14X120	W14X109	W14X176	W14X132	W14X159	W14X159	W14X132	W14X90	W14X109	W14X120	W14X145	W14X176	W14X132
7	W14X132	W14X132	W14X109	W14X132	W14X109	W14X109	W14X120	W14X120	W14X99	W14X99	W14X132	W14X90	W14X109	W14X109
8	W14X132	W14X132	W14X74	W14X109	W14X99	W14X90	W14X90	W14X109	W14X99	W14X145	W14X82	W14X74	W14X109	W14X90
9	W14X68	W14X109	W14X90	W14X82	W14X68	W14X82	W14X74	W14X48	W14X74	W14X109	W14X61	W14X74	W14X90	W14X68
10	W14X53	W14X53	W14X53	W14X74	W14X61	W14X74	W14X68	W14X48	W14X74	W14X48	W14X38	W14X38	W14X48	W14X61
11	W14X43	W14X61	W14X34	W14X34	W14X30	W14X38	W14X30	W14X34	W14X38	W14X38	W14X34	W14X30	W14X30	W14X30
12	W14X43	W14X30	W14X30	W14X22	W14X22	W14X30	W14X38	W14X30	W14X34	W14X30	W14X22	W14X22	W14X34	W14X30
13	W14X145	W14X99	W14X132	W14X145	W14X90	W14X159	W14X159	W14X159	W14X145	W14X99	W14X82	W14X99	W14X90	W14X90
14	W14X145	W14X132	W14X132	W14X132	W14X99	W14X132	W14X132	W14X120	W14X132	W14X132	W14X109	W14X90	W14X120	W14X99
15	W14X120	W14X109	W14X120	W14X109	W14X90	W14X109	W14X99	W14X109	W14X109	W14X109	W14X82	W14X99	W14X99	W14X90
16	W14X90	W14X74	W14X120	W14X82	W14X74	W14X82	W14X82	W14X99	W14X90	W14X68	W14X82	W14X90	W14X90	W14X82
17	W14X90	W14X82	W14X74	W14X61	W14X68	W14X68	W14X68	W14X82	W14X74	W14X68	W14X68	W14X68	W14X61	W14X68
18	W14X61	W14X82	W14X61	W14X48	W14X43	W14X48	W14X48	W14X53	W14X48	W14X68	W14X68	W14X61	W14X53	W14X43
19	W14X30	W14X48	W14X38	W14X30	W14X34	W14X34	W14X34	W14X38	W14X38	W14X61	W14X43	W14X43	W14X34	W14X43
20	W14X26	W14X82	W14X22	W14X22	W14X22	W14X26	W14X22	W14X26	W14X22	W14X22	W14X34	W14X22	W14X22	W14X22
Weight(kN)	980.63	997.56	927.15	956.13	929.10	960.90	946.25	967.33	941.55	945.15	927.59	909.67	911.78	908.41

Table 10. Optimization results for the 3-bay 24-story frame.

results are complemented by statistical tests, which further demonstrate the superiority of the proposed MaCN in finding better candidate solutions relative to others.

### Limitations of the proposed approach

In view of all practical advantages, there are also some limitations. The integrated method using three strategies effectively enhances the quality of candidate solutions. Increases the performance of conventional CS, while requiring more time to achieve the optimal solution. Therefore, there must be a careful trade-off between accuracy and performance when addressing real problems.

Although the population reduces over subsequent iterations and this helps in reducing the overall complexity of the algorithm, an initial and a final population needs to be defined to start the exploration process and finally avoid premature convergence due to a very small population in the end. Thus, handling population is still a concern for the proposed approach, and more rigorous studies must be conducted to adapt it.

In addition to that, evaluating fitness functions can be computationally expensive and noisy, further complicating the optimization process. An effective application of MaCN will require problem-specific customizations and significant domain knowledge to design appropriate representations and operators. Furthermore, there is no guarantee of finding the global optimum and its stochastic nature can result in different outcomes across multiple runs.

### Insightful Implications

Despite various limitations, MaCN can be a valuable addition to the optimization toolbox. It can be particularly useful for solving complex, non-linear, and poorly understood problems where traditional methods might fail. By understanding and mitigating the limitations of MaCN through hybrid approaches, dynamic algorithmic tuning, and problem-specific adaptations, its effectiveness can be improved in various application domains. The flexibility of MaCN allows for applications in fields ranging from artificial intelligence and machine learning to engineering design and bioinformatics. It can be used for the optimization of neural network architectures, leading to advancements in deep learning, and facilitate robust design in engineering by efficiently navigating vast and complex design spaces. In addition, MaCN inspires new ways to approach problem solving by emphasizing the importance of diversity, adaptability, and decentralized control, which can lead to more resilient and adaptive systems in various applications.

### Conclusion

A novel version of CS, namely MaCN was proposed to alleviate the drawbacks of basic CS. The proposed MaCN is based on hybridizing the CS with NMRA to overcome local search problems. It is also enhanced with self-adaptive properties to improve *expt* ability. The main idea here is to use iterative division and population division, along with a reducing *popsiz*e for better search operation with improved properties and less computational complexity. In addition, a bare-bones search operator is used to further enhance *expl* search ability. The adaptive *iw* is also added to optimize the switching probability benefits to obtain the appropriate stability between the search methods (i.e., *expl* and *expt*). The proposed MaCN algorithm is examined to solve the CEC2005 and CEC2014 benchmark test suite and three real-world steel frame design problems (that is, 1-bay 8-story, 3-bay 15-story and 3-bay 24-story). The comparative studies on CEC 2005 and CEC 2014 benchmarks show that MaCN is competitive with respect to JADE, SHADE, LSHADE-SPACMA, SaDE, LX-BBO, IMEHO, among others. In addition to that, experimental and statistical results on industrial engineering frame structure show its superiority compared to PSOPC, SFLAIWO, PSOACO, ES-DE, and others. The results showed that the proposed MaCN obtained encouraging and promising results in solving the CEC competition benchmark test functions compared to other state-of-the-art comment methods. Moreover, it demonstrated its high performance in solving real-world frame design problems by getting excellent results in solving these kinds of complex problem.

For future research, the proposed method can be investigated deeply to see the effect of each component and enhance it by other search operators. We can also incorporate various aspects such as archive based initialization, storing a history of solutions in the algorithm for better search capabilities, and others. An important aspect to look into will be the integration of MaCN with other hybrid approaches and see how these algorithms behave for complex real world problems. Moreover, the proposed methods can be used to solve feature selection, text clustering, image segmentation, task scheduling-based cloud computing; text classification, photovoltaic parameter estimation, constrained optimization problems, text summarization, big data application, image edge detection, networks applications, and other industrial engineering problems.

### Data availability

The data presented in this study are available on request from the corresponding author.

Received: 16 January 2025; Accepted: 2 May 2025

Published online: 04 June 2025

### References

1. Kaveh, A., Talatahari, S. & Khodadadi, N. Stochastic paint optimizer: theory and application in civil engineering. *Engineering with Computers* 1–32 (2020).
2. Abualigah, L. & Diabat, A. Advances in sine cosine algorithm: a comprehensive survey. *Artificial Intelligence Review* 1–42 (2021).
3. Yang, X.-S. Flower pollination algorithm for global optimization. In *International conference on unconventional computing and natural computation*, 240–249 (Springer, 2012).
4. Storn, R. & Price, K. Differential evolution—a simple and efficient heuristic for global optimization over continuous spaces. *Journal of global optimization* 11, 341–359 (1997).



5. Mirjalili, S., Mirjalili, S. M. & Lewis, A. Grey wolf optimizer. *Advances in engineering software* **69**, 46–61 (2014).
6. Abualigah, L., Abd Elaziz, M., Sumari, P., Geem, Z. W. & Gandomi, A. H. Reptile search algorithm (rsa): A nature-inspired meta-heuristic optimizer. *Expert Systems with Applications* **191**, 116158 (2022).
7. Heidari, A. A. et al. Harris hawks optimization: Algorithm and applications. *Future generation computer systems* **97**, 849–872 (2019).
8. Abualigah, L. M. & Diabat, A. A novel hybrid antlion optimization algorithm for multi-objective task scheduling problems in cloud computing environments. *Clust. Comput.* **24**, 205–223 (2021).
9. Salgotra, R. & Singh, U. The naked mole-rat algorithm. *Neural Computing and Applications* **31**, 8837–8857 (2019).
10. Jiang, Y., Luo, Q., Wei, Y., Abualigah, L. et al. An efficient binary gradient-based optimizer for feature selection. *Mathematical Biosciences and Engineering* **18** (2021).
11. Abualigah, L., Diabat, A., Mirjalili, S., Abd Elaziz, M. & Gandomi, A. H. The arithmetic optimization algorithm. *Computer methods in applied mechanics and engineering* **376**, 113609 (2021).
12. Abualigah, L. et al. Aquila optimizer: A novel meta-heuristic optimization algorithm. *Computers & Industrial Engineering* **157**, 107250 (2021).
13. Lin, Q. et al. A novel artificial bee colony algorithm with local and global information interaction. *Applied Soft Computing* **62**, 702–735 (2018).
14. Brajević, I. et al. Hybrid sine cosine algorithm for solving engineering optimization problems. *Mathematics* **10**, 4555 (2022).
15. Özbay, F. A., Özbay, E. & Gharehchopogh, F. S. An improved artificial rabbits optimization algorithm with chaotic local search and opposition-based learning for engineering problems and its applications in breast cancer problem. *CMES-Computer Modeling in Engineering & Sciences* **141** (2024).
16. Özbay, F. A. A modified seahorse optimization algorithm based on chaotic maps for solving global optimization and engineering problems. *Engineering Science and Technology, an International Journal* **41**, 101408 (2023).
17. Özbay, F. A. & Özbay, E. A new approach for gender detection from voice data: Feature selection with optimization methods. *J Fac Eng Archit Gazi Univ* **38**, 1179–1192 (2023).
18. Bakır, H. Enhanced artificial hummingbird algorithm for global optimization and engineering design problems. *Advances in Engineering Software* **194**, 103671 (2024).
19. Bakır, H. A novel artificial hummingbird algorithm improved by natural survivor method. *Neural Computing and Applications* **36**, 16873–16897 (2024).
20. Bakır, H. Dynamic fitness-distance balance-based artificial rabbits optimization algorithm to solve optimal power flow problem. *Expert Systems with Applications* **240**, 122460 (2024).
21. Bakır, H., Duman, S., Guvenc, U. & Kahraman, H. T. Improved adaptive gaining-sharing knowledge algorithm with fdb-based guiding mechanism for optimization of optimal reactive power flow problem. *Electrical Engineering* **105**, 3121–3160 (2023).
22. Salgotra, R. & Singh, U. Application of mutation operators to flower pollination algorithm. *Expert Systems with Applications* **79**, 112–129 (2017).
23. Karaboga, D. & Basturk, B. On the performance of artificial bee colony (abc) algorithm. *Applied soft computing* **8**, 687–697 (2008).
24. Nelder, J. A. & Mead, R. A simplex method for function minimization. *The computer journal* **7**, 308–313 (1965).
25. Yang, X.-S. & Deb, S. Cuckoo search via lévy flights. In *2009 World congress on nature & biologically inspired computing (NaBIC)*, 210–214 (IEEE, 2009).
26. Salgotra, R., Singh, U. & Saha, S. New cuckoo search algorithms with enhanced exploration and exploitation properties. *Expert Systems with Applications* **95**, 384–420 (2018).
27. Salgotra, R., Singh, U. & Saha, S. Improved cuckoo search with better search capabilities for solving cec2017 benchmark problems. In *2018 IEEE Congress on Evolutionary Computation (CEC)*, 1–7 (IEEE, 2018).
28. Bansal, J. C. et al. Inertia weight strategies in particle swarm optimization. In *2011 Third world congress on nature and biologically inspired computing*, 633–640 (IEEE, 2011).
29. Kennedy, J. Bare bones particle swarms. In *Proceedings of the 2003 IEEE Swarm Intelligence Symposium. SIS'03 (Cat. No. 03EX706)*, 80–87 (IEEE, 2003).
30. Hallam, J. W., Akman, O. & Akman, F. Genetic algorithms with shrinking population size. *Computational Statistics* **25**, 691–705 (2010).
31. Suganthan, P. N. et al. Problem definitions and evaluation criteria for the cec 2005 special session on real-parameter optimization. *KanGAL report* **2005005**, 2005 (2005).
32. Elsayed, S. M., Sarker, R. A., Essam, D. L. & Hamza, N. M. Testing united multi-operator evolutionary algorithms on the cec2014 real-parameter numerical optimization. In *2014 IEEE congress on evolutionary computation (CEC)*, 1650–1657 (IEEE, 2014).
33. Gupta, S., Deep, K. & Engelbrecht, A. P. A memory guided sine cosine algorithm for global optimization. *Engineering Applications of Artificial Intelligence* **93**, 103718 (2020).
34. Bhandari, A. K. A novel beta differential evolution algorithm-based fast multilevel thresholding for color image segmentation. *Neural Computing and Applications* **32**, 4583–4613 (2020).
35. Faramarzi, A., Heidarinejad, M., Stephens, B. & Mirjalili, S. Equilibrium optimizer: A novel optimization algorithm. *Knowledge-Based Systems* **191**, 105190 (2020).
36. Hansen, N., Müller, S. D. & Koumoutsakos, P. Reducing the time complexity of the derandomized evolution strategy with covariance matrix adaptation (cma-es). *Evolutionary computation* **11**, 1–18 (2003).
37. Khalilpourazari, S. & Pasandideh, S. H. R. Sine-cosine crow search algorithm: theory and applications. *Neural Computing and Applications* **1–18** (2019).
38. Zhang, J. & Sanderson, A. C. Jade: adaptive differential evolution with optional external archive. *IEEE Transactions on evolutionary computation* **13**, 945–958 (2009).
39. Tanabe, R. & Fukunaga, A. Success-history based parameter adaptation for differential evolution. In *2013 IEEE congress on evolutionary computation*, 71–78 (IEEE, 2013).
40. Salgotra, R., Singh, U. & Sharma, S. On the improvement in grey wolf optimization. *Neural Computing and Applications* **1–40** (2019).
41. Brest, J., Zumer, V. & Maucec, M. S. Self-adaptive differential evolution algorithm in constrained real-parameter optimization. In *2006 IEEE international conference on evolutionary computation*, 215–222 (IEEE, 2006).
42. Salgotra, R., Singh, U. & Saha, S. On some improved versions of whale optimization algorithm. *Arabian Journal for Science and Engineering* **44**, 9653–9691 (2019).
43. Mohamed, A. W., Hadi, A. A., Fattouh, A. M. & Jambi, K. M. Lshade with semi-parameter adaptation hybrid with cma-es for solving cec 2017 benchmark problems. In *2017 IEEE Congress on evolutionary computation (CEC)*, 145–152 (IEEE, 2017).
44. Yousri, D. & Mirjalili, S. Fractional-order cuckoo search algorithm for parameter identification of the fractional-order chaotic, chaotic with noise and hyper-chaotic financial systems. *Engineering Applications of Artificial Intelligence* **92**, 103662 (2020).
45. Baluja, S. Population-based incremental learning. a method for integrating genetic search based function optimization and competitive learning. Tech. Rep., Carnegie-Mellon Univ Pittsburgh Pa Dept Of Computer Science (1994).
46. Wang, G.-G., Deb, S., Gandomi, A. H., Zhang, Z. & Alavi, A. H. Chaotic cuckoo search. *Soft Computing* **20**, 3349–3362 (2016).
47. Tejani, G. G., Savsani, V. J., Patel, V. K. & Mirjalili, S. Truss optimization with natural frequency bounds using improved symbiotic organisms search. *Knowledge-Based Systems* **143**, 162–178 (2018).
48. Gupta, S. & Deep, K. A novel random walk grey wolf optimizer. *Swarm and evolutionary computation* **44**, 101–112 (2019).

49. Ma, H. & Simon, D. Blended biogeography-based optimization for constrained optimization. *Engineering Applications of Artificial Intelligence* **24**, 517–525 (2011).
50. Garg, V. & Deep, K. Performance of laplacian biogeography-based optimization algorithm on cec 2014 continuous optimization benchmarks and camera calibration problem. *Swarm and Evolutionary Computation* **27**, 132–144 (2016).
51. Wang, G.-G., Lu, M. & Zhao, X.-J. An improved bat algorithm with variable neighborhood search for global optimization. In *2016 IEEE Congress on Evolutionary Computation (CEC)*, 1773–1778 (IEEE, 2016).
52. Li, W., Wang, G.-G. & Alavi, A. H. Learning-based elephant herding optimization algorithm for solving numerical optimization problems. *Knowledge-Based Systems* 105675 (2020).
53. Rosner, B., Glynn, R. J. & Ting Lee, M.-L. Incorporation of clustering effects for the wilcoxon rank sum test: a large-sample approach. *Biometrics* **59**, 1089–1098 (2003).
54. Pereira, D. G., Afonso, A. & Medeiros, F. M. Overview of friedman's test and post-hoc analysis. *Communications in Statistics-Simulation and Computation* **44**, 2636–2653 (2015).
55. Payne, R. B. & Sorensen, M. D. *The cuckoos*, vol. 15 (Oxford University Press, 2005).
56. Brown, C. T., Liebovitch, L. S. & Glendon, R. Lévy flights in dove juv/hoansi foraging patterns. *Human Ecology* **35**, 129–138 (2007).
57. Pavlyukevich, I. Lévy flights, non-local search and simulated annealing. *Journal of Computational Physics* **226**, 1830–1844 (2007).
58. Shlesinger, M. F. Search research. *Nature* **443**, 281–282 (2006).
59. Gherboudj, A., Layeb, A. & Chikhi, S. Solving 0–1 knapsack problems by a discrete binary version of cuckoo search algorithm. *International Journal of Bio-Inspired Computation* **4**, 229–236 (2012).
60. Ouyang, X., Zhou, Y., Luo, Q. & Chen, H. A novel discrete cuckoo search algorithm for spherical traveling salesman problem. *Applied mathematics & information sciences* **7**, 777 (2013).
61. Ouaraab, A., Ahiod, B. & Yang, X.-S. Discrete cuckoo search algorithm for the travelling salesman problem. *Neural Computing and Applications* **24**, 1659–1669 (2014).
62. Shi, X. H., Liang, Y. C., Lee, H. P., Lu, C. & Wang, Q. Particle swarm optimization-based algorithms for tsp and generalized tsp. *Information processing letters* **103**, 169–176 (2007).
63. Tuba, M., Subotic, M. & Stanarevic, N. Modified cuckoo search algorithm for unconstrained optimization problems. In *Proceedings of the 5th European conference on European computing conference*, 263–268 (World Scientific and Engineering Academy and Society (WSEAS), 2011).
64. El Aziz, M. A. & Hassanien, A. E. Modified cuckoo search algorithm with rough sets for feature selection. *Neural Computing and Applications* **29**, 925–934 (2018).
65. Rani, K. N. A., MALEK, M., Fareq, A. & Siew-Chin, N. Nature-inspired cuckoo search algorithm for side lobe suppression in a symmetric linear antenna array. *Radioengineering* **21** (2012).
66. Giridhar, M. S., Sivanagaraju, S., Suresh, C. V. & Umapathi Reddy, P. Analyzing the multi objective analytical aspects of distribution systems with multiple multi-type compensators using modified cuckoo search algorithm. *International Journal of Parallel, Emergent and Distributed Systems* **32**, 549–571 (2017).
67. Tawfik, A. S., Badr, A. A. & Abdel-Rahman, I. F. One rank cuckoo search algorithm with application to algorithmic trading systems optimization. *International journal of computer applications* **64** (2013).
68. Rao, M. S. & Venkaiah, N. A modified cuckoo search algorithm to optimize wire-edm process while machining inconel-690. *Journal of the Brazilian Society of Mechanical Sciences and Engineering* **39**, 1647–1661 (2017).
69. Yang, X.-S. & Deb, S. Engineering optimisation by cuckoo search. *arXiv preprint arXiv:1005.2908* (2010).
70. Zhou, Y., Zheng, H., Luo, Q. & Wu, J. An improved cuckoo search algorithm for solving planar graph coloring problem. *Applied Mathematics & Information Sciences* **7**, 785 (2013).
71. Lin, J.-H., Lee, I.-H. et al. Emotional chaotic cuckoo search for the reconstruction of chaotic dynamics. In *source: 11th WSEAS Int. Conf. on Computational Intelligence, Man-Machine Systems and Cybernetics (CIMMACS'12)*, 123–128 (2012).
72. Kamoon, A. M. & Patra, J. C. A novel enhanced cuckoo search algorithm for contrast enhancement of gray scale images. *Applied Soft Computing* **85**, 105749 (2019).
73. Zhou, Y. & Zheng, H. A novel complex valued cuckoo search algorithm. *The Scientific World Journal* **2013** (2013).
74. Zheng, H. & Zhou, Y. A novel cuckoo search optimization algorithm based on gauss distribution. *Journal of Computational Information Systems* **8**, 4193–4200 (2012).
75. Boushaki, S. I., Kamel, N. & Bendjehaba, O. A new quantum chaotic cuckoo search algorithm for data clustering. *Expert Systems with Applications* **96**, 358–372 (2018).
76. Chandrasekaran, K. & Simon, S. P. Multi-objective scheduling problem: hybrid approach using fuzzy assisted cuckoo search algorithm. *Swarm and Evolutionary Computation* **5**, 1–16 (2012).
77. Zhang, M., Wang, H., Cui, Z. & Chen, J. Hybrid multi-objective cuckoo search with dynamical local search. *Memetic Computing* **10**, 199–208 (2018).
78. Binh, H. T. T. et al. Improved cuckoo search and chaotic flower pollination optimization algorithm for maximizing area coverage in wireless sensor networks. *Neural computing and applications* **30**, 2305–2317 (2018).
79. Daniel, E., Anitha, J. & Gnanaraj, J. Optimum laplacian wavelet mask based medical image using hybrid cuckoo search-grey wolf optimization algorithm. *Knowledge-Based Systems* **131**, 58–69 (2017).
80. Shehab, M., Khader, A. T., Laouchedi, M. & Alomari, O. A. Hybridizing cuckoo search algorithm with bat algorithm for global numerical optimization. *The Journal of Supercomputing* **75**, 2395–2422 (2019).
81. Abdel-Basset, M., Wang, G.-G., Sangaiah, A. K. & Rushdy, E. Krill herd algorithm based on cuckoo search for solving engineering optimization problems. *Multimedia Tools and Applications* **78**, 3861–3884 (2019).
82. Nawi, N. M., Khan, A. spsampsps Rehman, M. Z. A new cuckoo search based levenberg-marquardt (cslm) algorithm. In *international conference on computational science and its applications*, 438–451 (Springer, 2013).
83. Kanagaraj, G., Ponnambalam, S. & Jawahar, N. A hybrid cuckoo search and genetic algorithm for reliability-redundancy allocation problems. *Computers & Industrial Engineering* **66**, 1115–1124 (2013).
84. Kanagaraj, G., Ponnambalam, S. & Lim, W. C. E. Application of a hybridized cuckoo search-genetic algorithm to path optimization for pcb holes drilling process. In *2014 IEEE International Conference on Automation Science and Engineering (CASE)*, 373–378 (IEEE, 2014).
85. Lim, W., Kanagaraj, G. & Ponnambalam, S. A hybrid cuckoo search-genetic algorithm for hole-making sequence optimization. *Journal of Intelligent Manufacturing* **27**, 417–429 (2016).
86. Wang, G. et al. A hybrid meta-heuristic de/cs algorithm for ucav path planning. *Journal of Information and Computational Science* **9**, 4811–4818 (2012).
87. Zhang, Z., Ding, S. & Jia, W. A hybrid optimization algorithm based on cuckoo search and differential evolution for solving constrained engineering problems. *Engineering Applications of Artificial Intelligence* **85**, 254–268 (2019).
88. Wang, G. et al. A hybrid metaheuristic de/cs algorithm for ucav three-dimension path planning. *The Scientific World Journal* **2012** (2012).
89. Nancharaiah, B. & Mohan, B. C. Hybrid optimization using ant colony optimization and cuckoo search in manet routing. In *2014 International Conference on Communication and Signal Processing*, 1729–1734 (IEEE, 2014).
90. Babukartik, R. & Dhavachelvan, P. Hybrid algorithm using the advantage of aco and cuckoo search for job scheduling. *International Journal of Information Technology Convergence and Services* **2**, 25 (2012).

91. Sheikholeslami, R., Zecchin, A. C., Zheng, F. & Talatahari, S. A hybrid cuckoo-harmony search algorithm for optimal design of water distribution systems. *Journal of Hydroinformatics* **18**, 544–563 (2016).
92. Wang, G.-G., Gandomi, A. H., Zhao, X. & Chu, H. C. E. Hybridizing harmony search algorithm with cuckoo search for global numerical optimization. *Soft Computing* **20**, 273–285 (2016).
93. Dejam, S., Sadeghzadeh, M. & Mirabedini, S. J. Combining cuckoo and tabu algorithms for solving quadratic assignment problems. *Journal of Academic and Applied Studies* **2**, 1–8 (2012).
94. Layeb, A. A novel quantum inspired cuckoo search for knapsack problems. *International Journal of bio-inspired Computation* **3**, 297–305 (2011).
95. Jovanovic, R., Kais, S. & Alharbi, F. H. Cuckoo search inspired hybridization of the nelder-mead simplex algorithm applied to optimization of photovoltaic cells. *arXiv preprint arXiv:1411.0217* (2014).
96. Abdel-Baset, M. & Hezam, I. M. Solving linear least squares problems based on improved cuckoo search algorithm. *Mathematical Sciences Letter* **5**, 199–202 (2016).
97. Long, W., Cai, S., Jiao, J., Xu, M. & Wu, T. A new hybrid algorithm based on grey wolf optimizer and cuckoo search for parameter extraction of solar photovoltaic models. *Energy Conversion and Management* **203**, 112243 (2020).
98. Giveki, D., Salimi, H., Bahmanyar, G. & Khademian, Y. Automatic detection of diabetes diagnosis using feature weighted support vector machines based on mutual information and modified cuckoo search. *arXiv preprint arXiv:1201.2173* (2012).
99. Zaw, M. M. & Mon, E. E. Web document clustering using cuckoo search clustering algorithm based on levy flight. *International Journal of Innovation and Applied Studies* **4**, 182–188 (2013).
100. Tiwari, V. Face recognition based on cuckoo search algorithm. *image* **7**, 9 (2012).
101. Bhandari, A., Soni, V., Kumar, A. & Singh, G. Cuckoo search algorithm based satellite image contrast and brightness enhancement using dwt-svd. *ISA transactions* **53**, 1286–1296 (2014).
102. Gandomi, A. H., Yang, X.-S. & Alavi, A. H. Cuckoo search algorithm: a metaheuristic approach to solve structural optimization problems. *Engineering with computers* **29**, 17–35 (2013).
103. Kumar, A. & Chakarverty, S. Design optimization for reliable embedded system using cuckoo search. In *2011 3rd International Conference on Electronics Computer Technology*, vol. 1, 264–268 (IEEE, 2011).
104. Madic, M. & Radovanovic, M. Application of cuckoo search algorithm for surface roughness optimization in co2 laser cutting. *Annals of the Faculty of Engineering Hunedoara* **11**, 39 (2013).
105. Sudabattula, S. & Kowsalya, M. Optimal allocation of wind based distributed generators in distribution system using cuckoo search algorithm. *Procedia Computer Science* **92**, 298–304 (2016).
106. Piechocki, J., Ambroziak, D., Palkowski, A. & Redlarski, G. Use of modified cuckoo search algorithm in the design process of integrated power systems for modern and energy self-sufficient farms. *Applied Energy* **114**, 901–908 (2014).
107. Tran, C. D., Dao, T. T., Vo, V. S. & Nguyen, T. T. Economic load dispatch with multiple fuel options and valve point effect using cuckoo search algorithm with different distributions. *International Journal of Hybrid Information Technology* **8**, 305–316 (2015).
108. Pandey, A. C., Rajpoot, D. S. & Saraswat, M. Twitter sentiment analysis using hybrid cuckoo search method. *Information Processing & Management* **53**, 764–779 (2017).
109. Katarya, R. & Verma, O. P. An effective collaborative movie recommender system with cuckoo search. *Egyptian Informatics Journal* **18**, 105–112 (2017).
110. Dhabal, S. & Venkateswaran, P. An efficient gbest-guided cuckoo search algorithm for higher order two channel filter bank design. *Swarm and Evolutionary Computation* **33**, 68–84 (2017).
111. Chitara, D., Niazi, K. R., Swarnkar, A. & Gupta, N. Cuckoo search optimization algorithm for designing of a multimachine power system stabilizer. *IEEE Transactions on Industry Applications* **54**, 3056–3065 (2018).
112. Dong, Y., Zhang, Z. & Hong, W.-C. A hybrid seasonal mechanism with a chaotic cuckoo search algorithm with a support vector regression model for electric load forecasting. *Energies* **11**, 1009 (2018).
113. Sun, G. et al. Coverage optimization of vlc in smart homes based on improved cuckoo search algorithm. *Computer Networks* **116**, 63–78 (2017).
114. Nguyen, T. T. & Vo, D. N. Modified cuckoo search algorithm for multiobjective short-term hydrothermal scheduling. *Swarm and evolutionary computation* **37**, 73–89 (2017).
115. Sun, G. et al. Thinning of concentric circular antenna arrays using improved discrete cuckoo search algorithm. In *2017 IEEE Wireless Communications and Networking Conference (WCNC)*, 1–6 (IEEE, 2017).
116. Aslam, S. et al. An efficient home energy management scheme using cuckoo search. In *International Conference on P2P, Parallel, Grid, Cloud and Internet Computing*, 167–178 (Springer, 2017).
117. Cheng, J., Wang, L. & Xiong, Y. An improved cuckoo search algorithm and its application in vibration fault diagnosis for a hydroelectric generating unit. *Engineering Optimization* **50**, 1593–1608 (2018).
118. Zhou, X., Liu, Y., Li, B. & Li, H. A multiobjective discrete cuckoo search algorithm for community detection in dynamic networks. *Soft Computing* **21**, 6641–6652 (2017).
119. Zhang, X., Wan, Q. & Fan, Y. Applying modified cuckoo search algorithm for solving systems of nonlinear equations. *Neural Computing and Applications* **31**, 553–576 (2019).
120. Nguyen, T. T., Nguyen, T. T. & Le, B. Optimization of electric distribution network configuration for power loss reduction based on enhanced binary cuckoo search algorithm. *Computers & Electrical Engineering* **90**, 106893 (2021).
121. Alqahtani, F., Al-Makhadmeh, Z., Tolba, A. & Said, W. Internet of things-based urban waste management system for smart cities using a cuckoo search algorithm. *Cluster Computing* **23**, 1769–1780 (2020).
122. Mohanty, P. K. An intelligent navigational strategy for mobile robots in uncertain environments using smart cuckoo search algorithm. *Journal of Ambient Intelligence and Humanized Computing* **11**, 6387–6402 (2020).
123. Sadeghi, F. & Avokh, A. Load-balanced data gathering in internet of things using an energy-aware cuckoo-search algorithm. *International Journal of Communication Systems* **33**, e4385 (2020).
124. Cai, X. et al. An under-sampled software defect prediction method based on hybrid multi-objective cuckoo search. *Concurrency and Computation: Practice and Experience* **32**, e5478 (2020).
125. Ghobaei-Arani, M., Rahmadian, A. A., Aslanpour, M. S. & Dashti, S. E. Csa-wsc: cuckoo search algorithm for web service composition in cloud environments. *Soft Computing* **22**, 8353–8378 (2018).
126. Zhao, J., Wong, P. K., Xie, Z., Ma, X. & Hua, X. Design and control of an automotive variable hydraulic damper using cuckoo search optimized pid method. *International Journal of Automotive Technology* **20**, 51–63 (2019).
127. Pankaj, B. S., Naidu, M. N., Vasan, A. & Varma, M. R. Self-adaptive cuckoo search algorithm for optimal design of water distribution systems. *Water Resources Management* **34**, 3129–3146 (2020).
128. Shehab, M., Khader, A. T. & Al-Betar, M. A. A survey on applications and variants of the cuckoo search algorithm. *Applied Soft Computing* **61**, 1041–1059 (2017).
129. Salgotra, R., Singh, U., Saha, S. & Gandomi, A. H. Self adaptive cuckoo search: Analysis and experimentation. *Swarm and Evolutionary Computation* **60**, 100751 (2021).
130. Wolpert, D. H. & Macready, W. G. No free lunch theorems for optimization. *IEEE transactions on evolutionary computation* **1**, 67–82 (1997).
131. Salgotra, R., Singh, U., Saha, S. & Gandomi, A. H. Improving cuckoo search: Incorporating changes for cec 2017 and cec 2020 benchmark problems. In *2020 IEEE Congress on Evolutionary Computation (CEC)*, 1–7 (IEEE, 2020).

132. Salgotra, R., Singh, U., Singh, S. & Mittal, N. A hybridized multi-algorithm strategy for engineering optimization problems. *Knowledge-Based Systems* **217**, 106790 (2021).
133. Al-Hassan, W., Fayek, M. & Shaheen, S. Psoa: An optimized particle swarm technique for solving the urban planning problem. In *2006 International Conference on Computer Engineering and Systems*, 401–405 (IEEE, 2006).
134. Chen, G., Huang, X., Jia, J. & Min, Z. Natural exponential inertia weight strategy in particle swarm optimization. In *2006 6th World Congress on Intelligent Control and Automation*, vol. 1, 3672–3675 (IEEE, 2006).
135. Xin, J., Chen, G. & Hai, Y. A particle swarm optimizer with multi-stage linearly-decreasing inertia weight. In *2009 International Joint Conference on Computational Sciences and Optimization*, vol. 1, 505–508 (IEEE, 2009).
136. Feng, Y., Teng, G.-F., Wang, A.-X. & Yao, Y.-M. Chaotic inertia weight in particle swarm optimization. In *Second International Conference on Innovative Computing, Information and Control (ICICIC 2007)*, 475–475 (IEEE, 2007).
137. Gao, Y.-L., An, X.-h. & Liu, J.-m. A particle swarm optimization algorithm with logarithm decreasing inertia weight and chaos mutation. In *2008 International Conference on Computational Intelligence and Security*, vol. 1, 61–65 (IEEE, 2008).
138. Yousri, D., Abd Elaziz, M. & Mirjalili, S. Fractional-order calculus-based flower pollination algorithm with local search for global optimization and image segmentation. *Knowledge-Based Systems* 105889 (2020).
139. Derrac, J., García, S., Molina, D. & Herrera, F. A practical tutorial on the use of nonparametric statistical tests as a methodology for comparing evolutionary and swarm intelligence algorithms. *Swarm and Evolutionary Computation* **1**, 3–18 (2011).
140. Liang, J., Qu, B. & Suganthan, P. Problem definitions and evaluation criteria for the cec 2014 special session and competition on single objective real-parameter numerical optimization. *Computational Intelligence Laboratory, Zhengzhou University, Zhengzhou China and Technical Report, Nanyang Technological University, Singapore* **635** (2013).
141. Kaveh, A., Vaez, S. R. H. & Hosseini, P. Simplified dolphin echolocation algorithm for optimum design of frame. *Smart Struct Syst* **21**, 321–333 (2018).
142. Salgotra, R. & Gandomi, A. H. A novel multi-hybrid differential evolution algorithm for optimization of frame structures. *Scientific Reports* **14**, 4877 (2024).
143. Talatahari, S., Gandomi, A. H., Yang, X.-S. & Deb, S. Optimum design of frame structures using the eagle strategy with differential evolution. *Engineering Structures* **91**, 16–25 (2015).
144. Degertekin, S. O. Optimum design of steel frames using harmony search algorithm. *Structural and multidisciplinary optimization* **36**, 393–401 (2008).
145. Gandomi, A. H., spsampsps Yang, X.-S. Benchmark problems in structural optimization. In *Computational optimization, methods and algorithms*, 259–281 (Springer, 2011).
146. Camp, C., Pezeshk, S. & Cao, G. Optimized design of two-dimensional structures using a genetic algorithm. *Journal of structural engineering* **124**, 551–559 (1998).
147. Kaveh, A. & Talatahari, S. An improved ant colony optimization for the design of planar steel frames. *Engineering Structures* **32**, 864–873 (2010).
148. Kaveh, A. & Talatahari, S. A discrete particle swarm ant colony optimization for design of steel frames. *ASIAN JOURNAL OF CIVIL ENGINEERING (BUILDING AND HOUSING)* (2008).
149. Kaveh, A. & Malakoutirad, S. Hybrid genetic algorithm and particle swarm optimization for the force method-based simultaneous analysis and design. *IRANIAN JOURNAL OF SCIENCE AND TECHNOLOGY TRANSACTION B-ENGINEERING* (2010).
150. Kaveh, A., Talatahari, S. & Khodadadi, N. The hybrid invasive weed optimization-shuffled frog-leaping algorithm applied to optimal design of frame structures. *Periodica Polytechnica Civil Engineering* **63**, 882–897 (2019).
151. Kaveh, A., spsampsps Talatahari, S. Hybrid algorithm of harmony search, particle swarm and ant colony for structural design optimization. In *Harmony search algorithms for structural design optimization*, 159–198 (Springer, 2009).
152. Kaveh, A. & Talatahari, S. A discrete big bang-big crunch algorithm for optimal design of skeletal structures. *ASIAN JOURNAL OF CIVIL ENGINEERING (BUILDING AND HOUSING)* (2010).
153. Kaveh, A. & Talatahari, S. Optimum design of skeletal structures using imperialist competitive algorithm. *Computers & structures* **88**, 1220–1229 (2010).
154. Kaveh, A., Ghazaan, M. I. & Saadatmand, F. Colliding bodies optimization with morlet wavelet mutation and quadratic interpolation for global optimization problems. *Engineering with Computers* 1–25 (2021).
155. Kaveh, A., Kamalinejad, M. & Hamedani, K. B. Enhanced versions of the shuffled shepherd optimization algorithm for the optimal design of skeletal structures. In *Structures*, vol. 29, 1463–1495 (Elsevier, 2021).
156. Talatahari, S. & Azizi, M. Optimum design of building structures using tribe-interior search algorithm. In *Structures*, vol. 28, 1616–1633 (Elsevier, 2020).
157. Davison, J. H. & Adams, P. F. Stability of braced and unbraced frames. *Journal of the Structural Division* **100**, 319–334 (1974).
158. Camp, C. V., Bichon, B. J. & Stovall, S. P. Design of steel frames using ant colony optimization. *Journal of Structural Engineering* **131**, 369–379 (2005).
159. Kaveh, A., Talatahari, S. & Alami, M. A new hybrid meta-heuristic for optimum design of frame structures. *ASIAN JOURNAL OF CIVIL ENGINEERING (BUILDING AND HOUSING)* (2012).
160. Bigham, A. & Gholizadeh, S. Topology optimization of nonlinear single-layer domes by an improved electro-search algorithm and its performance analysis using statistical tests. *Structural and multidisciplinary optimization* **62**, 1821–1848 (2020).

## Author contributions

Conceptualization, R.S.; methodology, S.S. and P.V.; software, P.V. and L.A.; validation, S.S.; writing-original draft preparation, S.S. and R.S.; writing-review and editing, L.A., A.H.G.

## Funding

Open access funding provided by Óbuda University.

## Declarations

## Competing interests

On behalf of all authors, the corresponding author states that there is no conflict of interest.

## Additional information

**Correspondence** and requests for materials should be addressed to R.S. or A.H.G.

**Reprints and permissions information** is available at [www.nature.com/reprints](http://www.nature.com/reprints).

**Publisher's note** Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.



**Open Access** This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons licence, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons licence, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons licence and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this licence, visit <http://creativecommons.org/licenses/by/4.0/>.

© The Author(s) 2025